

Photonic crystals, PHYS-605

Ecole doctorale photonique

Romuald Houdré

Summer semester 2017

V Measurement techniques

Contents

* **1 Introduction, overview.**

Introduction
History of photonic crystals
The key concepts

* **2 Theory**

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FDTD
Transfer matrices, FEM and other methods

* **3 Basic properties**

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High quality factor cavities
Dispersion diagram and equifrequency surfaces
Superprism, negative refraction
Selfcollimation
Fourier analysis of Bloch waves

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* **6 Applications**

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Point defect photonic crystal lasers
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Integration with microfluidics systems
Biology
Slow light
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Subwavelength structures
Slotted waveguides
Optical trapping
Sensors
Dynamic control
Non-reciprocal structures
Novel materials (chalcogenide, diamond, GaN,...)
Thermal photovoltaic
Topological transitions
...

Goal

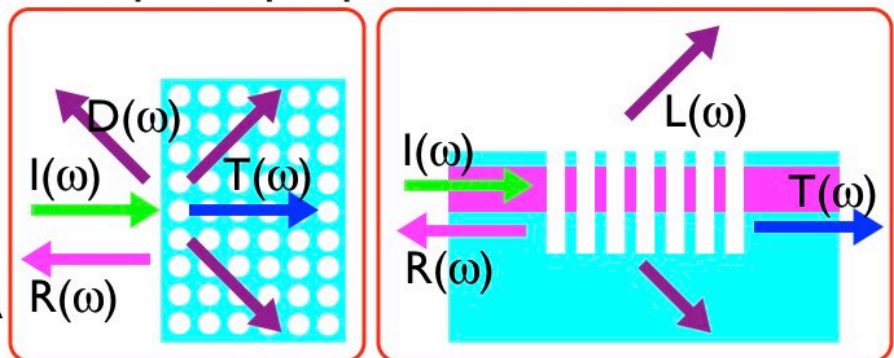
Once our photonic crystal structure has been (painfully) fabricated and characterised (SEM etc...)

How can we measure its optical properties, it was designed for ?

Which optical properties ?

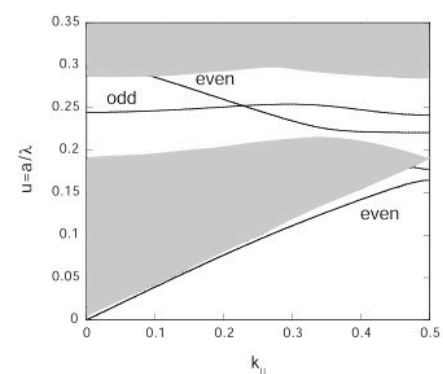
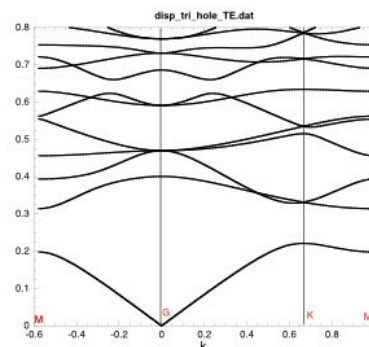
* Optical response

- Transmission, T
- Reflection, R
- Diffraction, D
- Absorption, A
- Losses, $L = I - T - R - D - A$



* Band structure

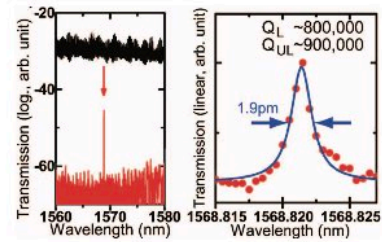
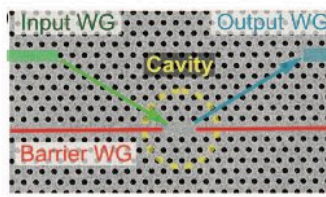
- Dispersion curve
- Group index



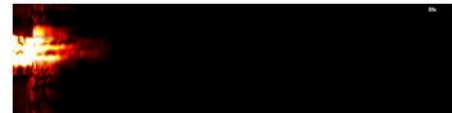
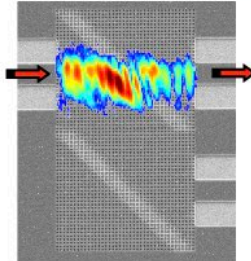
* Non-linear properties

Which optical properties ?

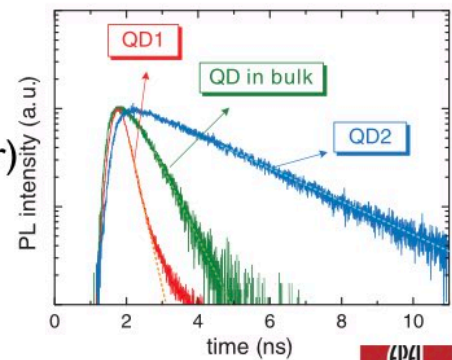
- * Localised state
 - Optical cavity
 - Resonance frequencies
 - Quality factor



- * Light propagation inside the photonic crystal



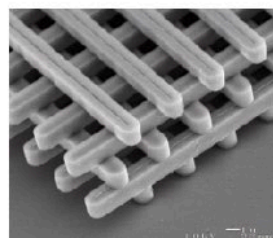
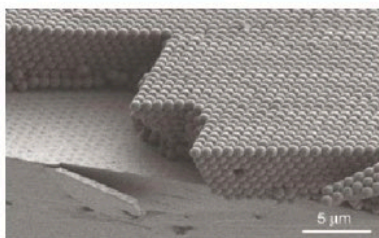
- * Dynamic properties (time resolved)
- * Emission properties (spontaneous, amplified, laser)
- * Wavelength
 - Visible / near infra-red
 - Far infra-red
 - Microwave



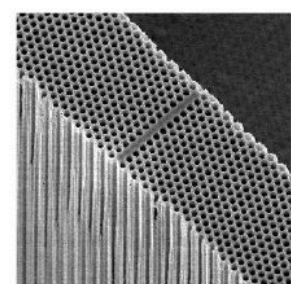
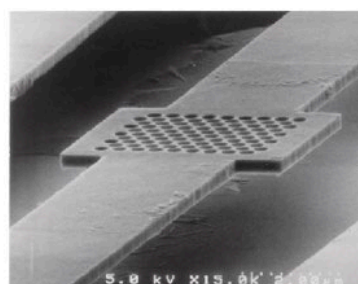
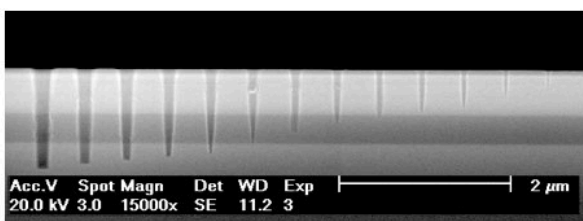
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Which photonic crystal structure ?

- * 3D photonic crystal



- * 2D photonic crystal



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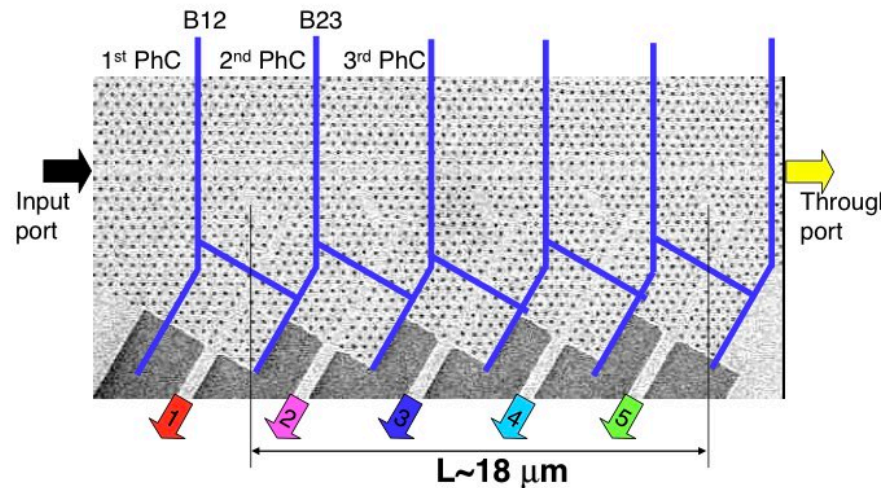
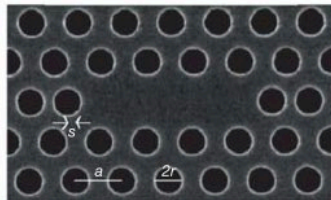
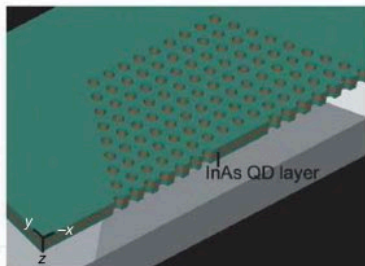
Which photonic crystal structure ?

* Material

- Dielectric / Semiconductor
- Metal

* Use

- Physics
- Device



Techniques outline

Lithographic tuning

External light source

- * Reflectivity
- * End fire

Internal light source

- * Internal light source
- * Luminescence spectroscopy

Advanced techniques

- * Local probe, SNOM
- * Time resolved
- * Fourier imaging

Lithographic tuning

Scaling laws

$$r \rightarrow r' = r \cdot s$$

$$\varepsilon(r) \rightarrow \varepsilon(r')$$

$$k \rightarrow k' = k / s$$

$$\omega \rightarrow \omega' = \omega / s$$

$$H(r) \rightarrow H(r')$$

$$E(r) \rightarrow E(r')$$

Reduced units

Energy :
$$u = \frac{a}{\lambda} = \frac{\omega a}{2\pi c}$$

Wave vector :
$$\tilde{k} = \frac{ka}{2\pi}$$

a : lattice parameter

Lithographic tuning

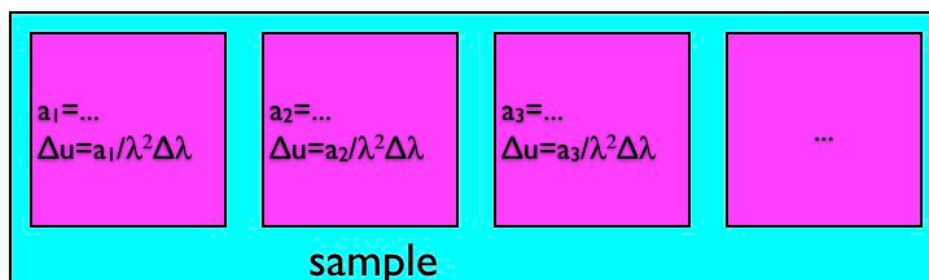
Wavelength, energy scan

Reduced energy :
$$u = \frac{a}{\lambda} = \frac{\omega a}{2\pi c}$$

either scan u by changing the lattice constant. Often more convenient.

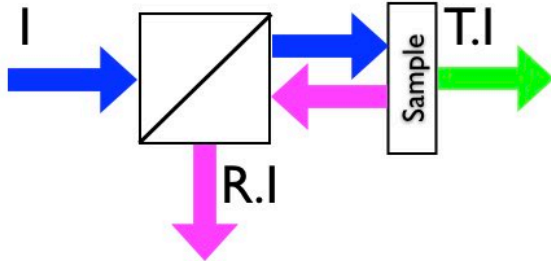
a : lattice parameter

either scan u by changing the wavelength

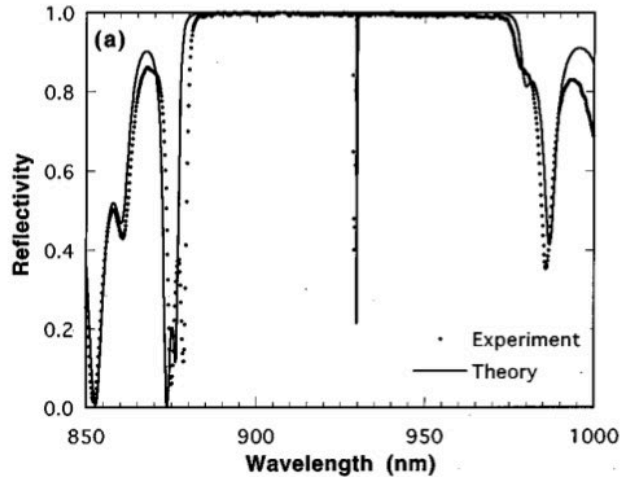
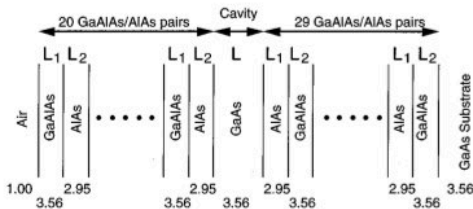


External source Reflectivity & transmission measurements

Simple R&T measurements to probe the photonic bandgap



Similar to the measurement of a dielectric multi-layer sample



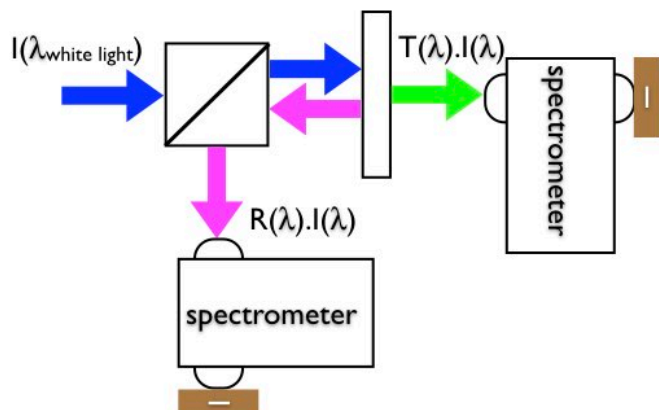
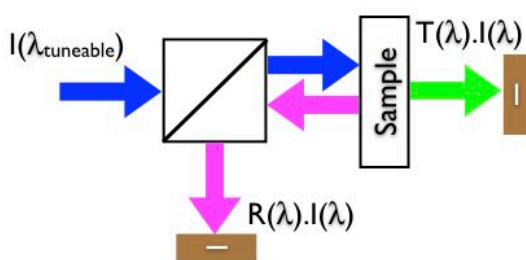
Planar GaAs/AlAs Fabry-Perot cavity

R.P. Stanley et al., Appl. Phys. Lett., 65, 1883, (1994)

External source Reflectivity & transmission measurements

Spectral resolution

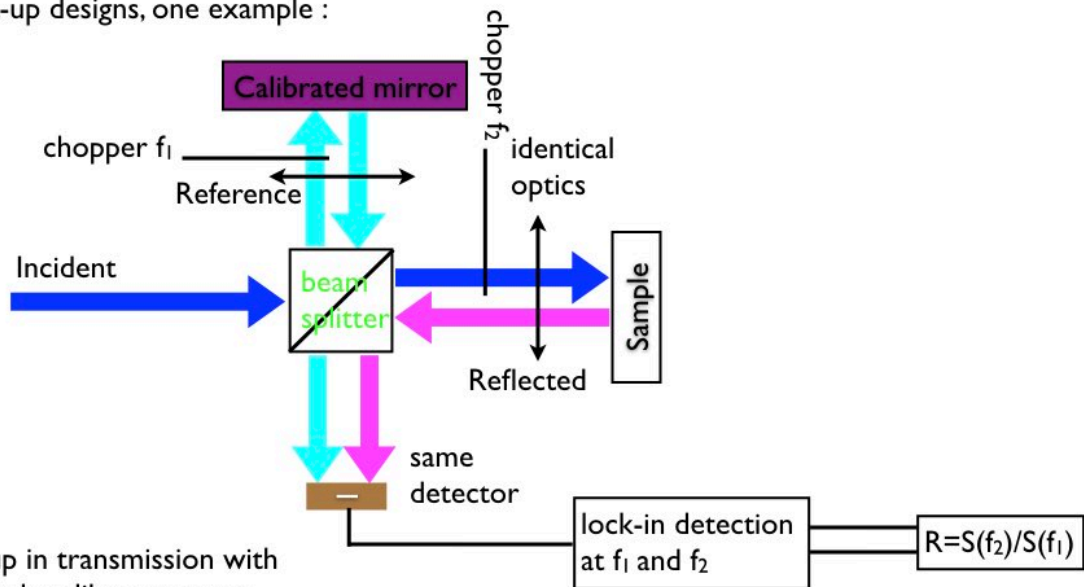
In a linear regime, light source can be a wavelength tuneable source or a white light source and spectral resolution is performed afterwards



External source Reflectivity & transmission measurements

Quantitative measurements require a good measurement of the reference (incoming intensity)

Many set-up designs, one example :



Similar set-up in transmission with a Mach-Zehnders like geometry

External source Reflectivity & transmission measurements

Quantitative measurement

Note: it is not easy to measure directly reflectivity coefficients close to unity

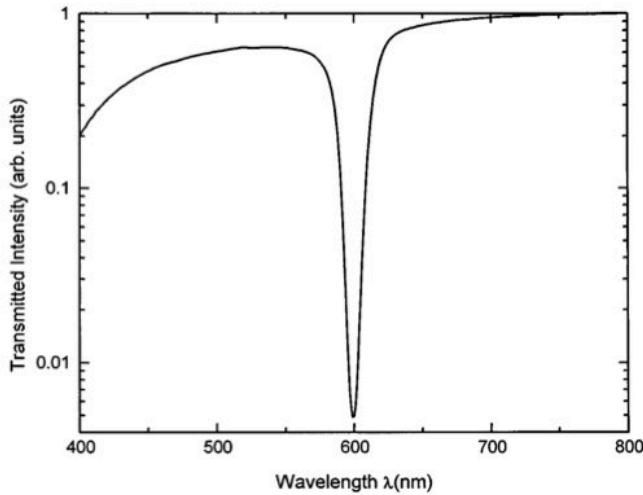
This would imply being able to discriminate between e.g. $R=0.999$ and $R=0.997$

It is much more convenient to use the mirror to build a high Q optical cavity and deduce R from Q

External source

Reflectivity & transmission measurements

Simple R&T measurements to probe the photonic bandgap



Note that:

- $T=0$ does not prove $R=1$
- No angular investigation (full bandgap ?)
- Polarisation ?

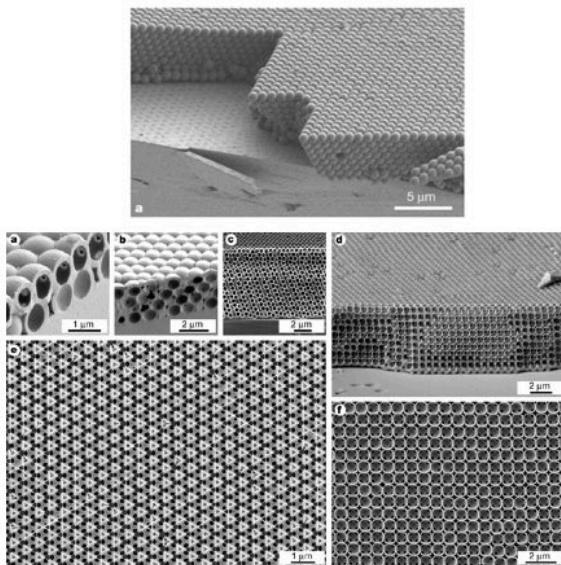
First measurements performed on opals of $0.1 \mu\text{m}$ polystyrene microspheres

I. Inanç Tarhan et al., Opt. Lett., 20, 1571, (1995)

External source

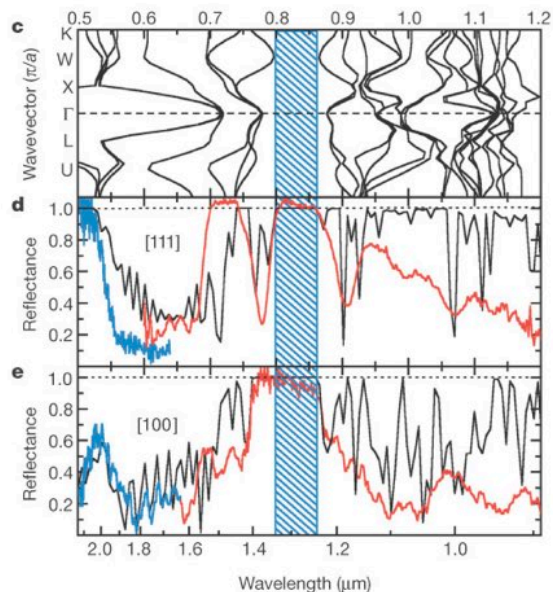
Reflectivity & transmission measurements

Simple R&T measurements to probe the photonic bandgap



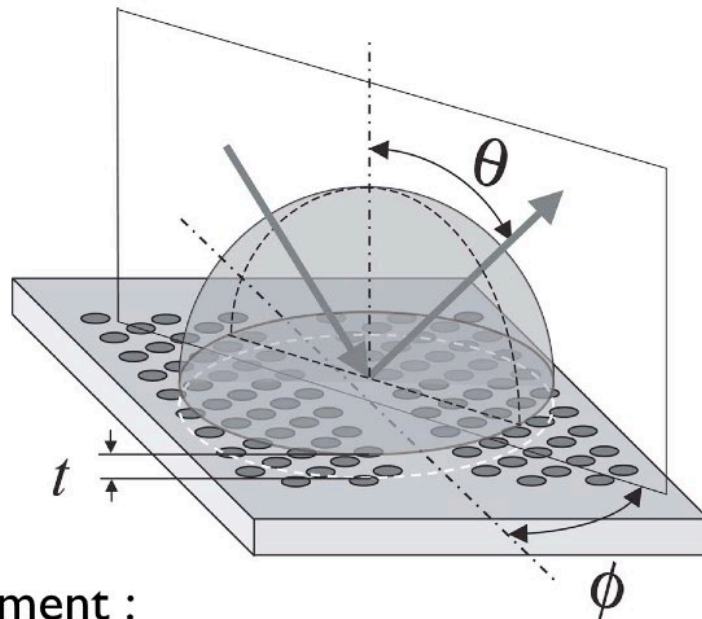
inverted opal

Y.A. Vlasov et al., Nature, 414, 289, (2001)



External source Angular reflectivity

Principle



Measurement :

- Intensity vs. angle(s) at constant wavelength
- Intensity vs. wavelength at constant angle(s)

Light is reflected according to the grating diffraction law

Conservation of the in-plane component of the wavevector

$$k_{||}^{ref} = k_{||}^{inc} + G = k_{||}^{inc} + \sum_i m_i G_i$$

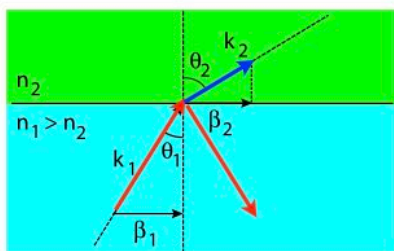
G : vector of the reciprocal lattice

$m_i = 0$: specular reflection

$m_i \neq 0$: diffraction

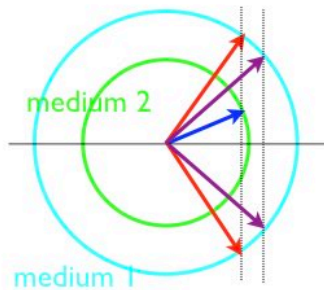
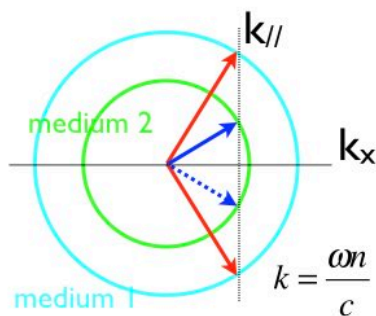
As such, it will provide information on the reciprocal lattice but not the band structure (?)

- For some specific set of incident k and wavelength, light can couple to a mode into the photonic crystal
- Giving rise to a dip in the reflected intensity spectrum (Wood anomaly)
- Will provide information on the band structure $k(\omega)$
- Simple picture :



$$\frac{\sin \theta_1}{\sin \theta_2} = \frac{n_2}{n_1} \quad \text{in-plane } k \text{ conservation}$$

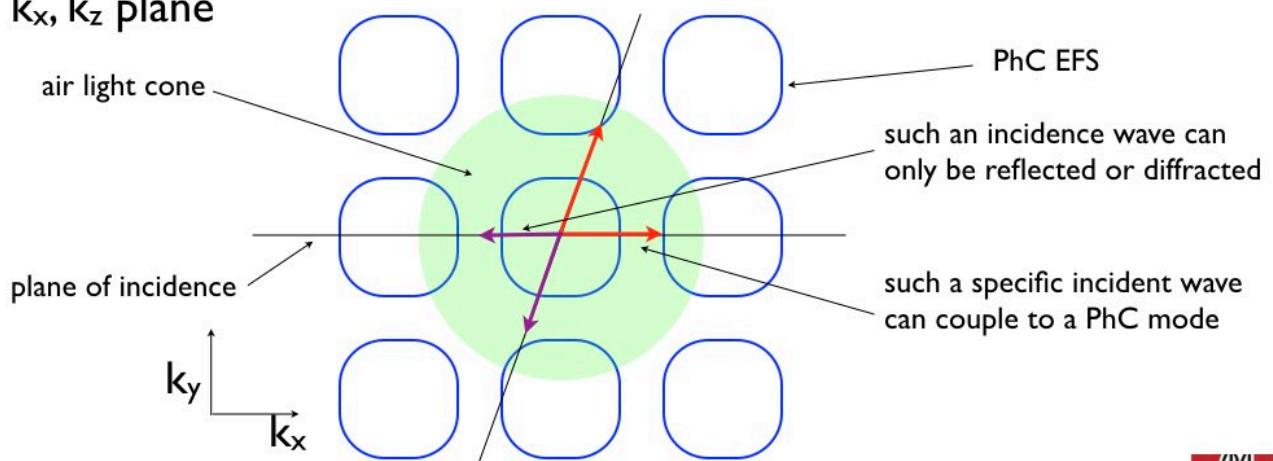
$$k_0 n_1 \sin \theta_1 = k_0 n_2 \sin \theta_2 \quad \beta_1 = \beta_2$$

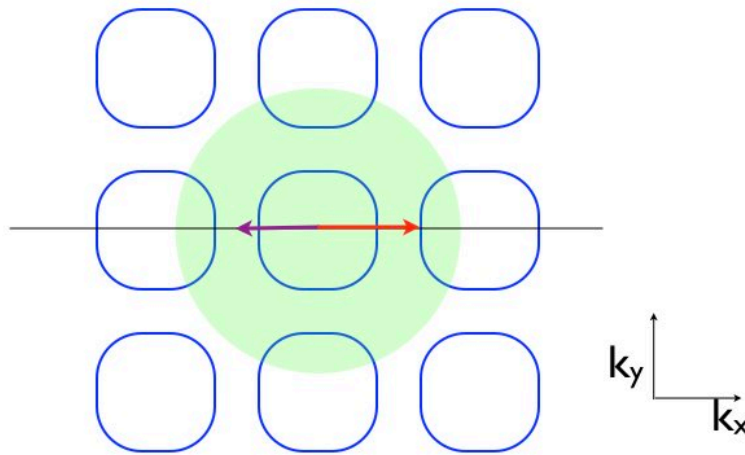
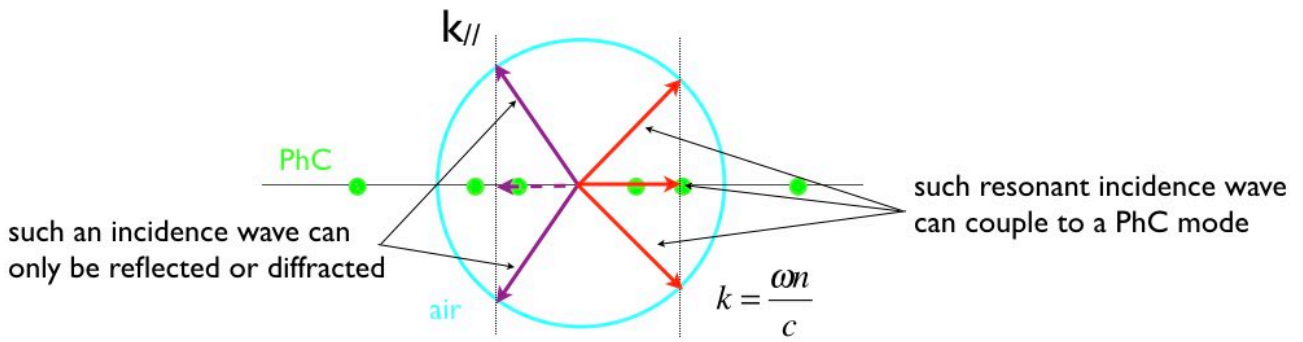


Total internal reflection :

- * $k < n_2 \omega / c$: coupling 1 to 2 possible
- * $k > n_2 \omega / c$: coupling 1 to 2 impossible

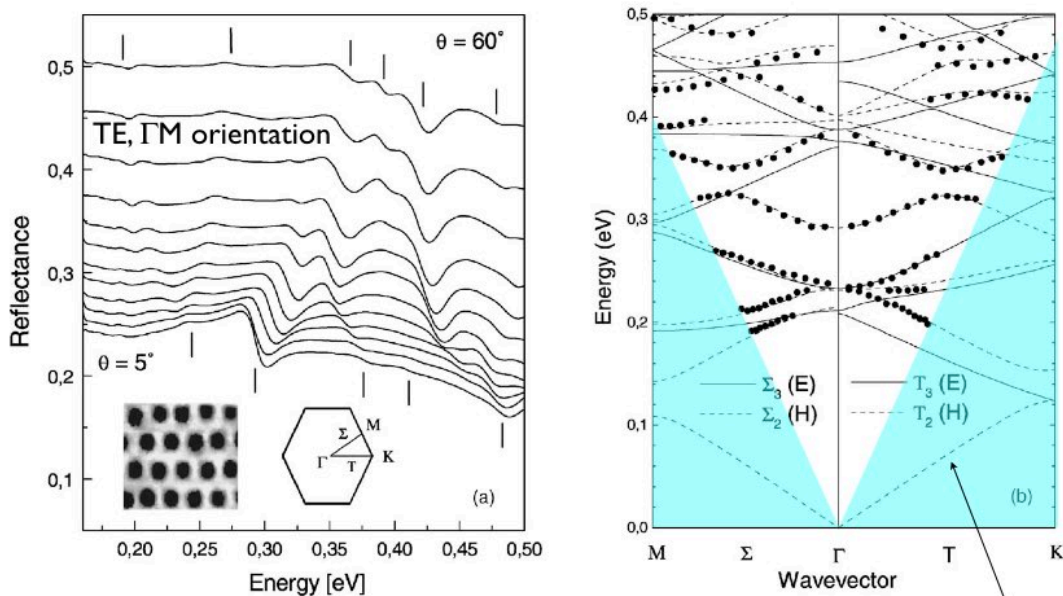
- In the case of a bi-dimensional medium 2, the equi-frequency surface is reduced to a curve in the plane k_x, k_y , i.e. points in the k_x, k_z plane





In real life experiment are not so straightforward to interpret due to the complex shape of the reflectivity spectrum

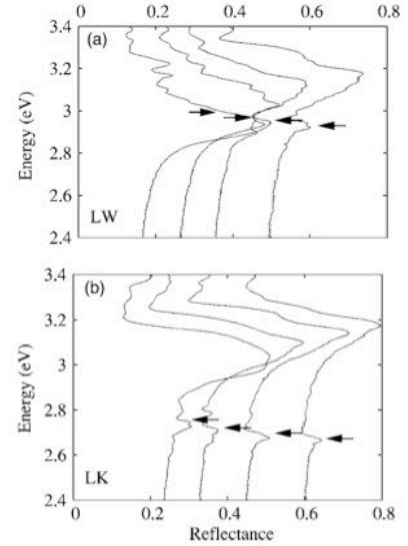
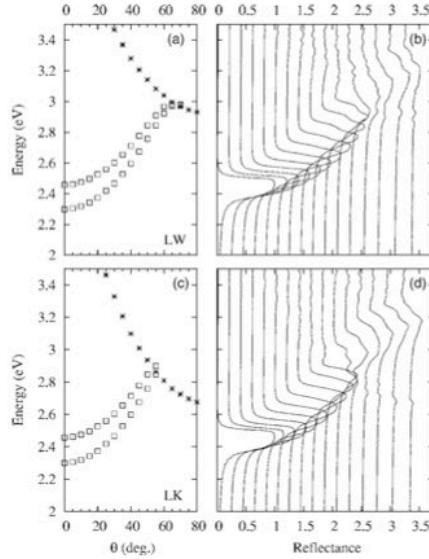
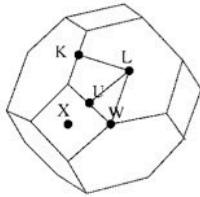
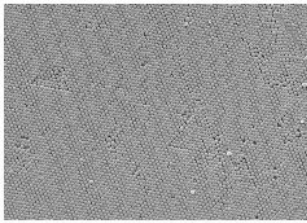
Macroporous silicon



M. Galli et al., Phys. Rev. B, 65, 113111, (2002)

For 3D structures, the measurement probes mainly the density of states and its associated singularities

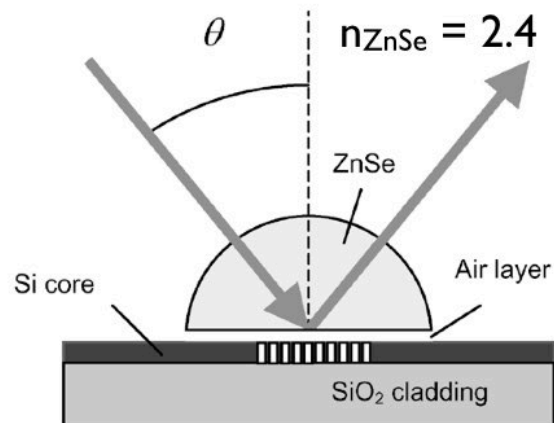
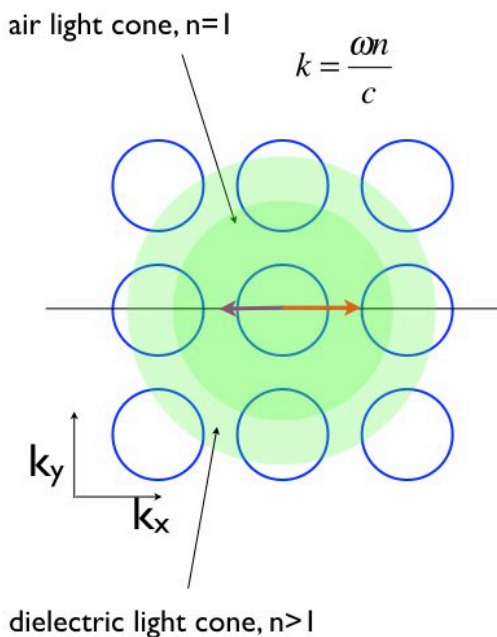
Artificial opals



E. Pavarini. et al., Phys. Rev. B, 72, 045102, (2005)

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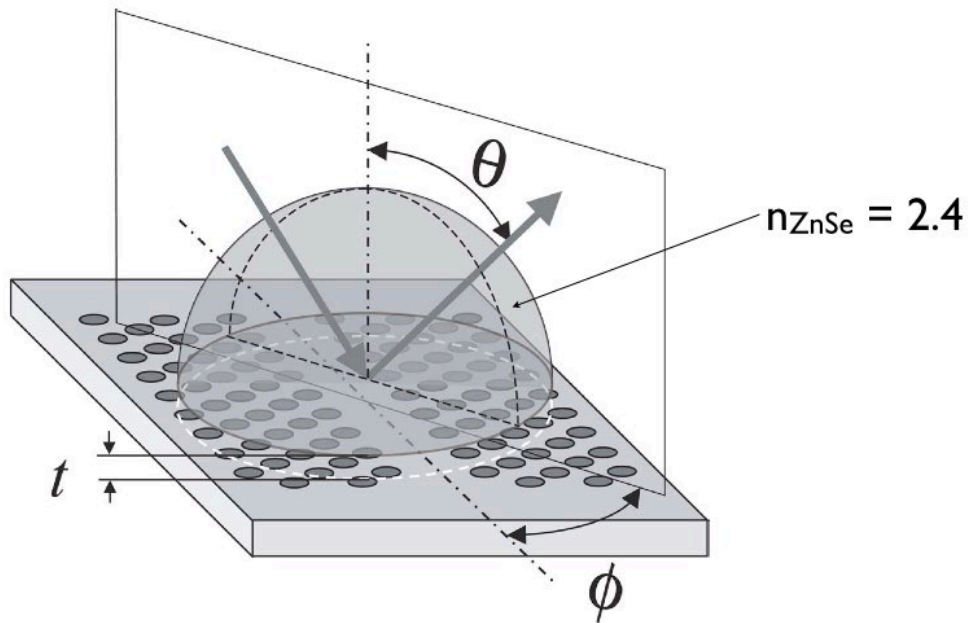
Measurement above the light line limit Extension to larger k-values



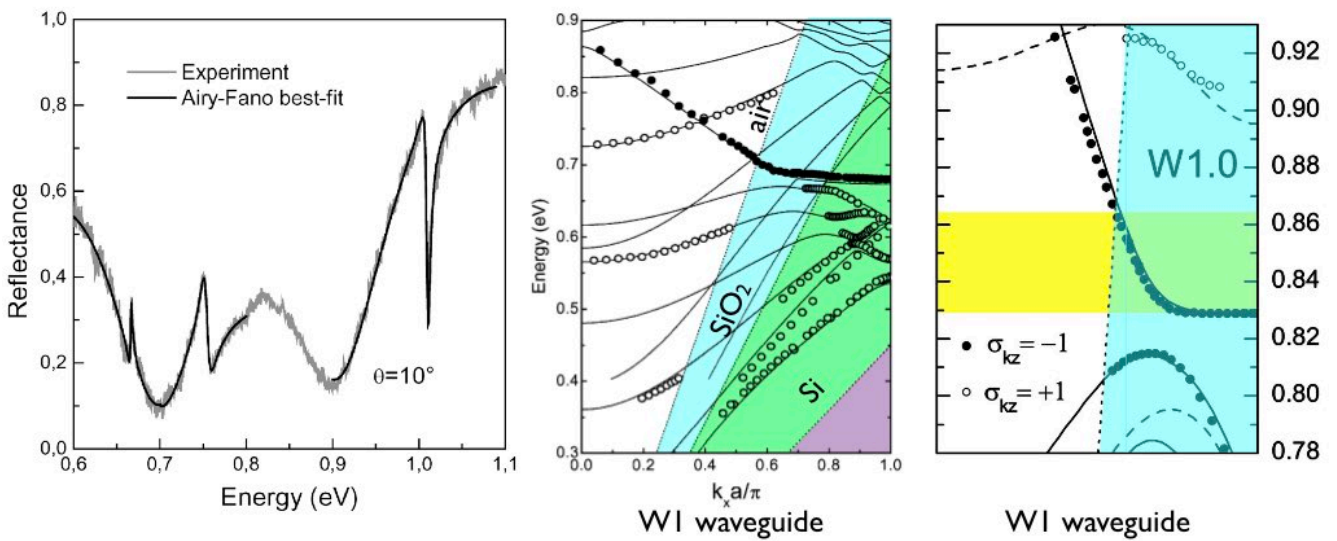
M. Galli et al., Phys. Rev. B, 70, 081307, (2004), M. Galli et al., Phys. Rev. B, 72, 125322, (2005)

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Measurement above the light line limit Extension to larger k-values



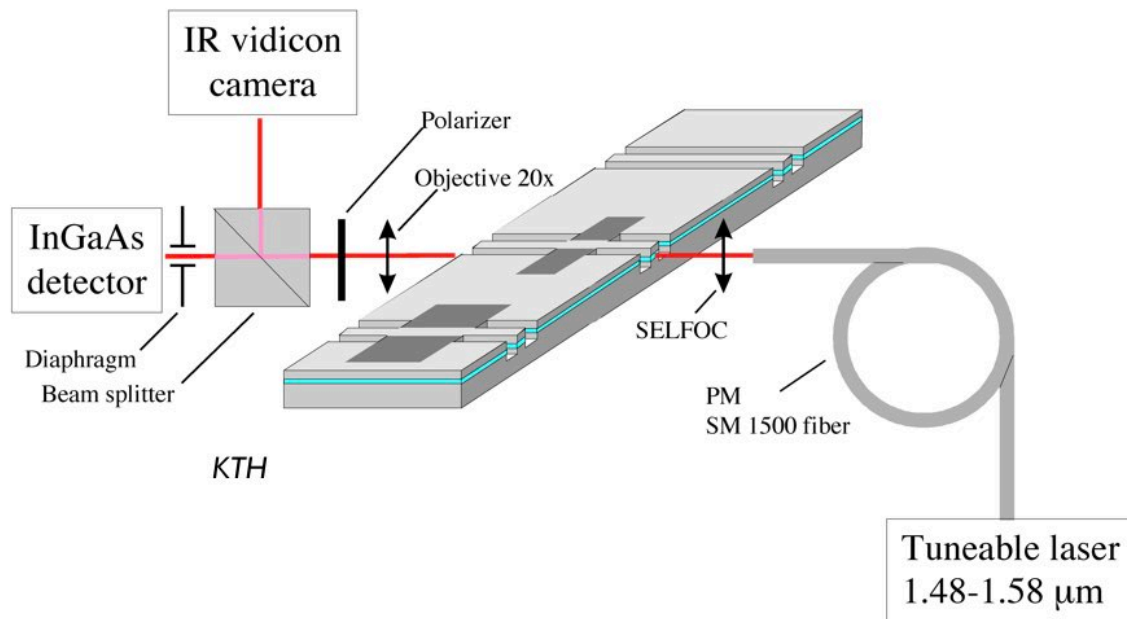
Measurement above the light line limit Extension to larger k-values



- Experiment is difficult
- Resolution is limited by the sphere astigmatism and field of view
- Analysis is delicate
- Experiment does not discriminate between true propagating slow modes and localised defect modes

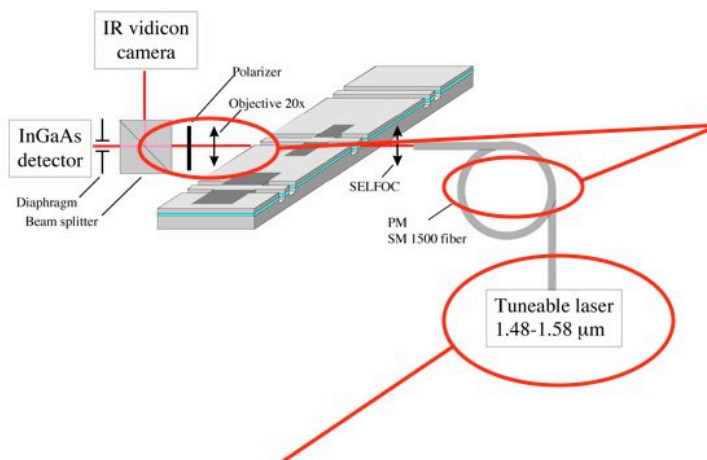
External source End-Fire

Principle



External source End-Fire

Principle



Light input or output :

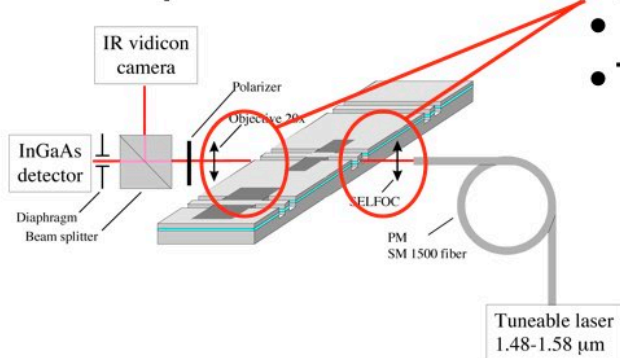
- Optical fiber, single mode
- Free space

Light source :

- Tuneable source, laser
- Broadband source, white light, LED, super-luminescent LED, ...

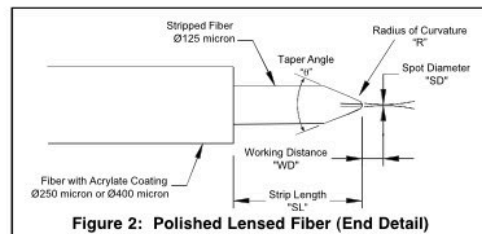
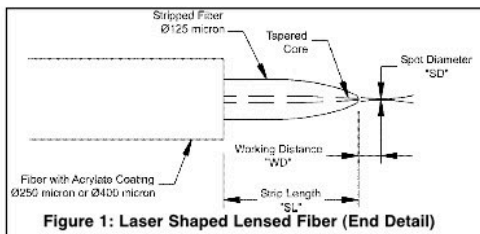
External source End-Fire

Principle



Light coupling in/out :

- Microscope objective, free space
- Tapered, microlensed fiber



External source End-Fire

Principle

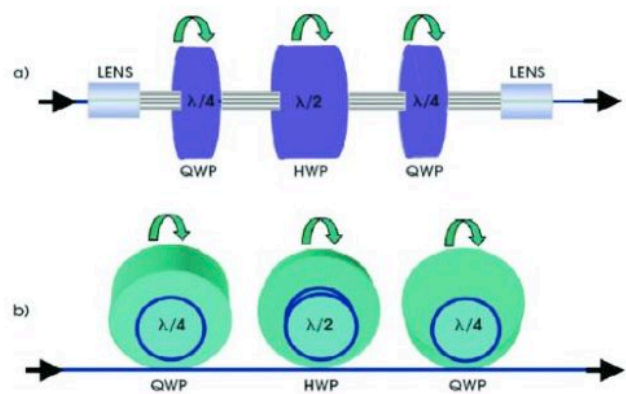
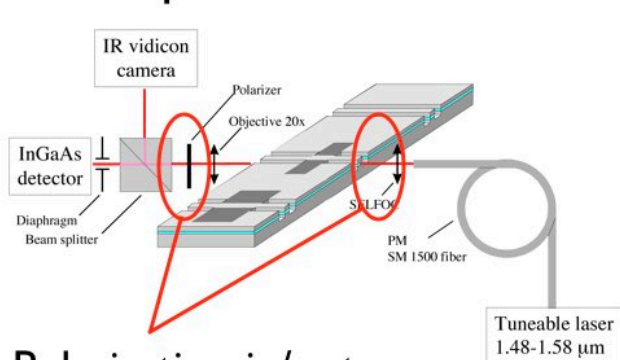


Figure 6. Polarization control using, a) multiple wave plates and, b) using multiple coiled fiber.

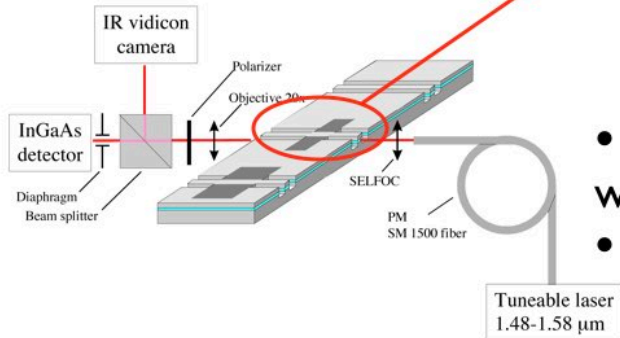
Newport App. Note 20

Polarisation in/out :

- Polarisation maintaining fibers
- Polarisation control
- Polarisation analysis
- Polariser, $\lambda/2$ and $\lambda/4$ retarding plates
- Coiled fibers
- Often reduced to a TE/TM control / analysis

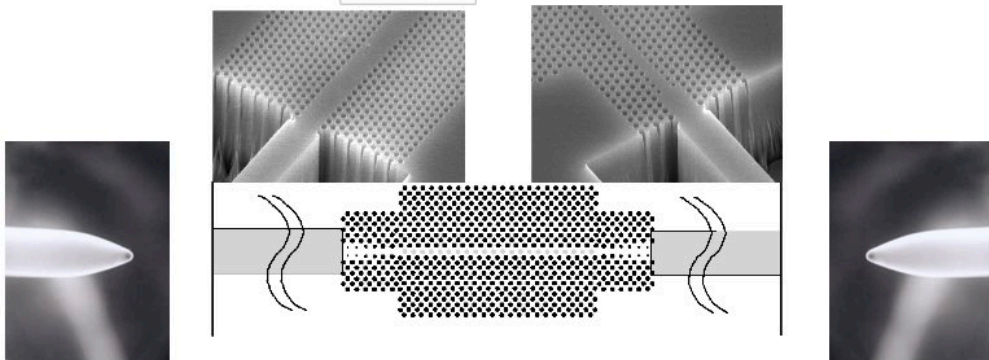
External source End-Fire

Principle



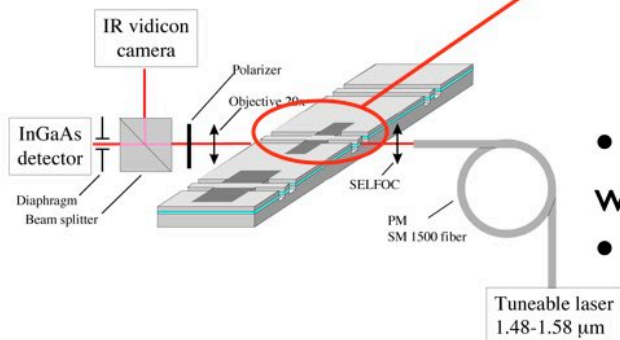
Sample :

- Access waveguide
 - Deep / shallow etched ridge waveguide
- Taper access waveguide / PhC waveguide
- PhC device



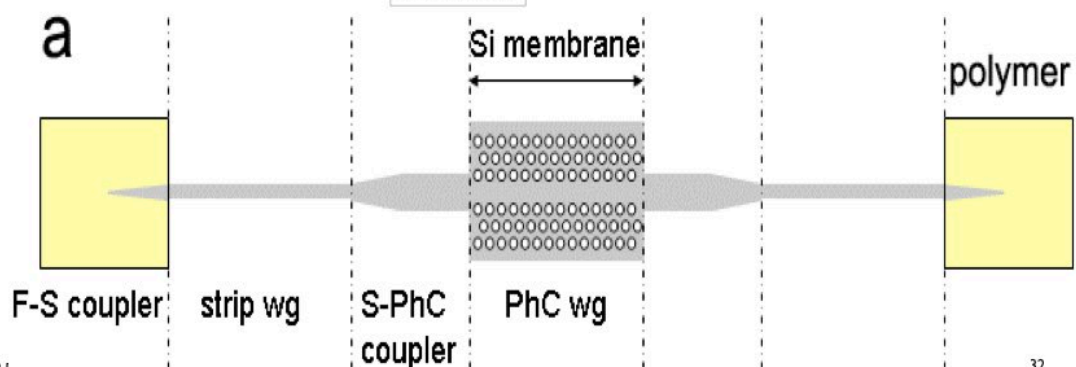
External source End-Fire

Principle



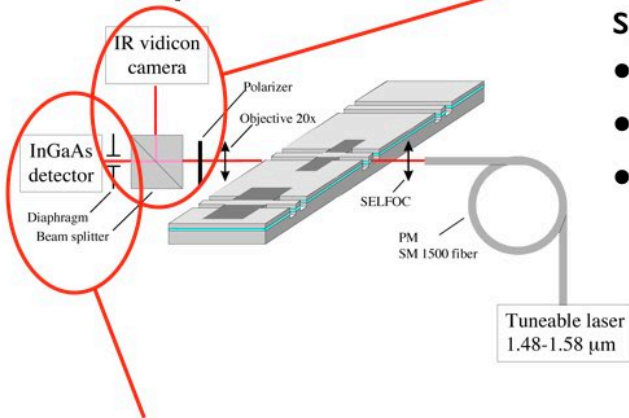
Sample :

- Access waveguide
 - Deep / shallow etched ridge waveguide
- Taper access waveguide / PhC waveguide
- PhC device



External source End-Fire

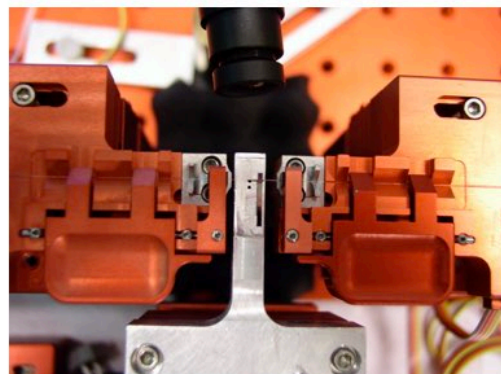
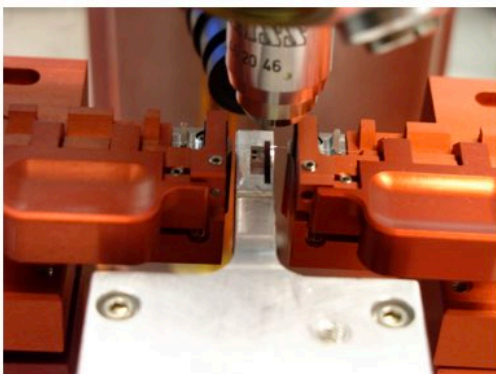
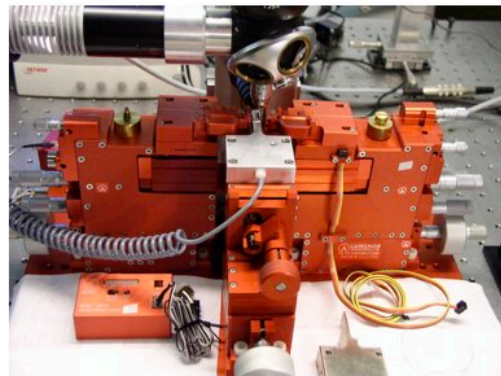
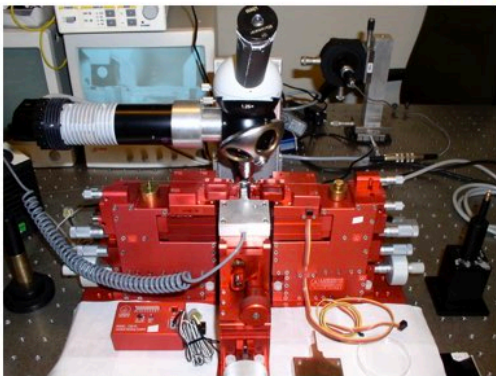
Principle



Detector

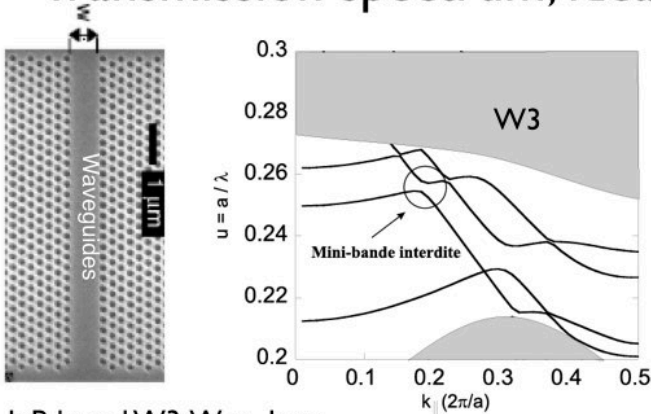
- Si
- InGaAs
- + spectrometer

External source End-Fire



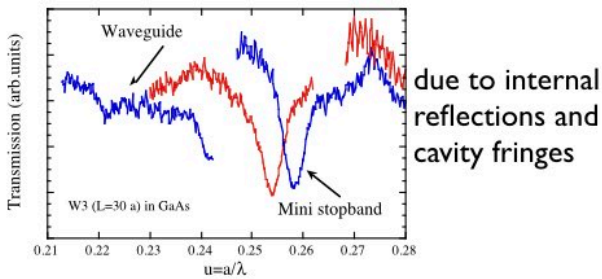
End-Fire

Transmission spectrum, ideal case

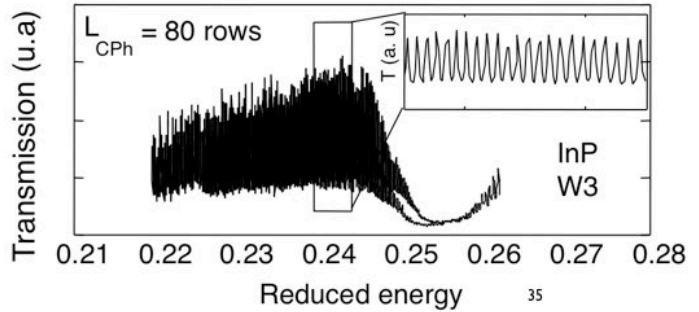
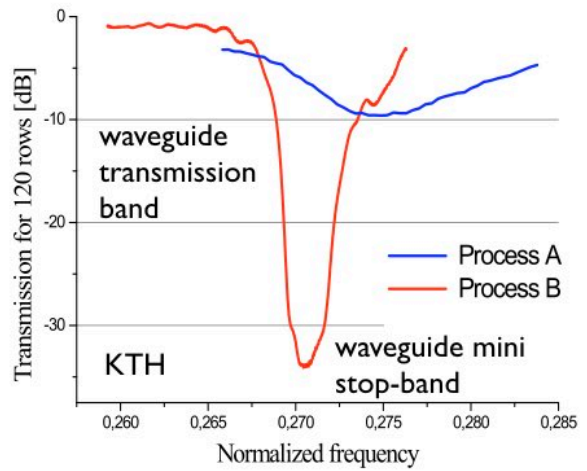


InP-based W3:W ≈ 1 μm

but more commonly :

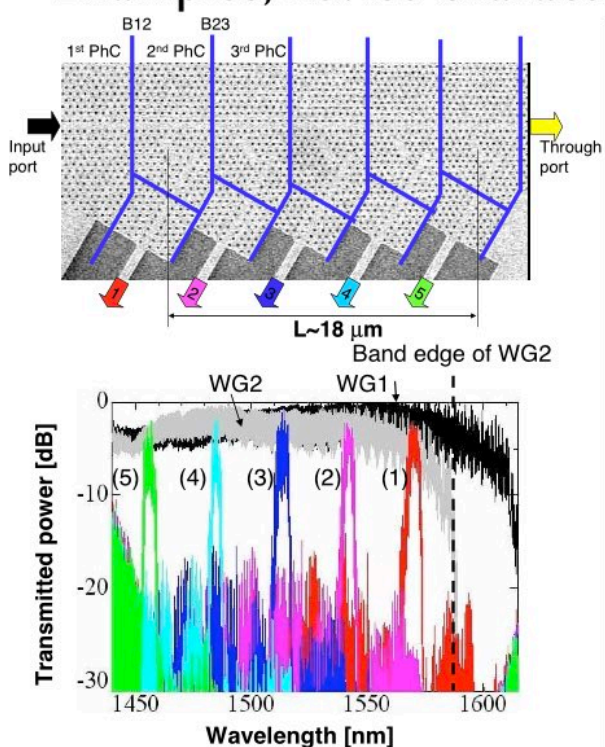


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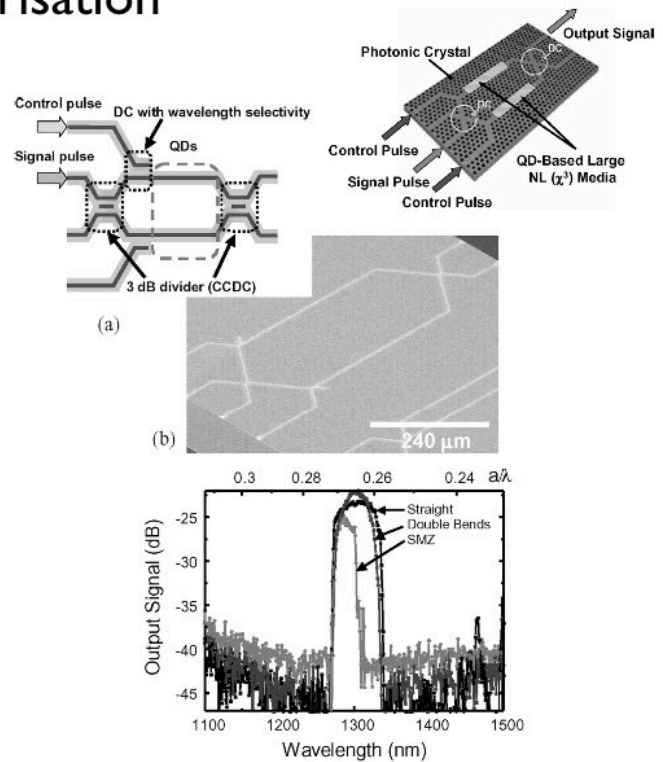
End-Fire

Examples, device characterisation



A. Shinya et al., *Opt. Exp.*, 14, 12394, (2006)

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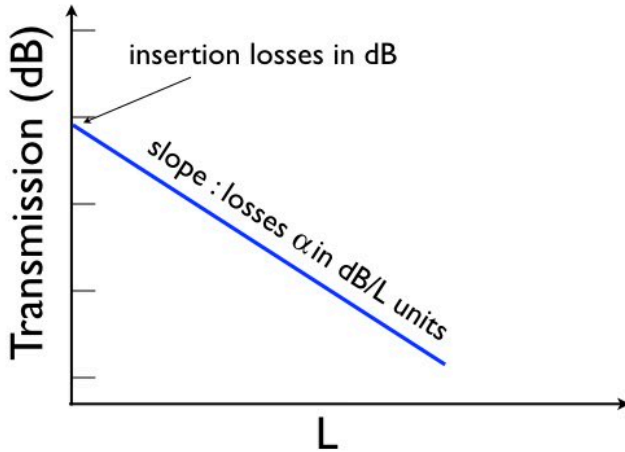
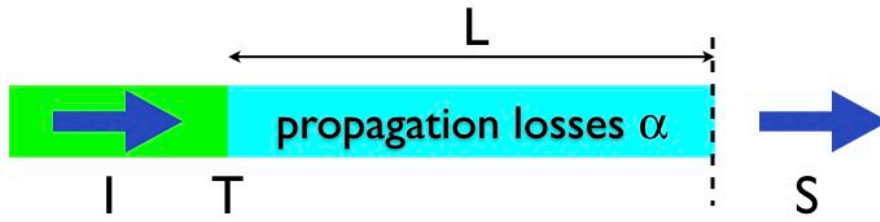
Y. Sugimoto et al., *J. Sel. Area. Comm.*, 23, 1308, (2005)

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Measurement of R,T and propagation losses

Cut-back method



$$\frac{S}{I} = T e^{-\alpha L}$$

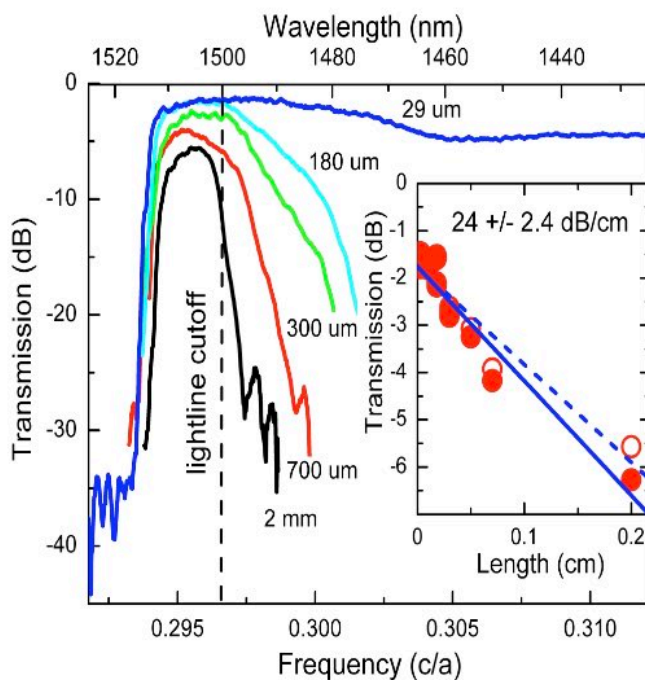
$$\text{Ln}\left(\frac{S}{I}\right) = \text{Ln}(T) - \alpha L$$

$$\left(\frac{S}{I}\right)_{dB} = 10 \cdot \log_{10}(T) - \frac{\alpha}{\text{Ln}(10)} L$$

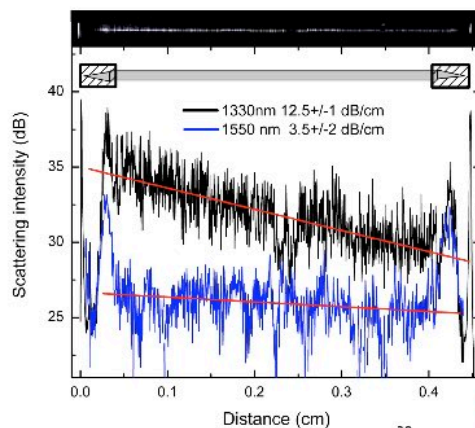
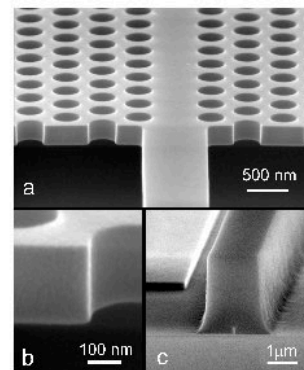
$$A_{dB/cm} = 10 \frac{\alpha_{cm^{-1}}}{\text{Ln}(10)} = 4.34 \alpha_{cm^{-1}}$$

Measurement of R,T and propagation losses

Cut-back method, examples

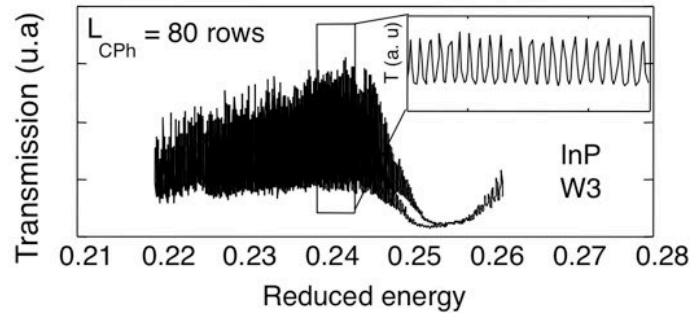


SOI



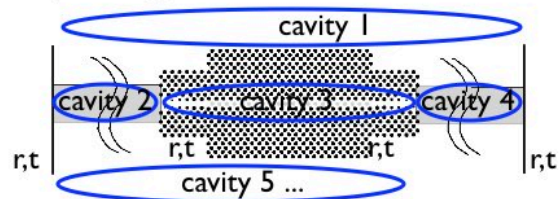
End-Fire

Transmission spectrum, parasitic reflections



Due to internal reflections and cavity fringes :

- at the cleaved facets
- at the tapers
- inside the PhC structure
- ...



Undesirable for the device performance but let's make use of them for characterisation

Measurement of R,T and propagation losses

Hakki-Paoli method

Fabry-Perot cavity

fringes equally spaced in energy

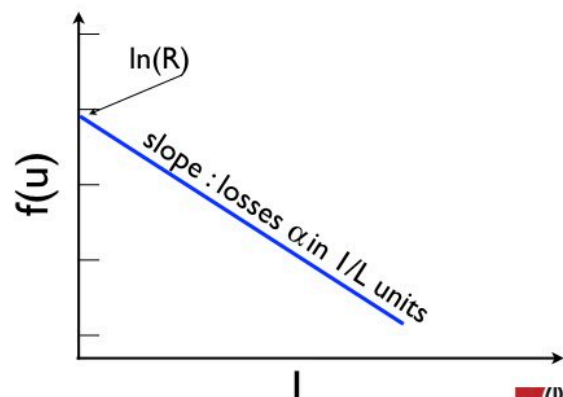
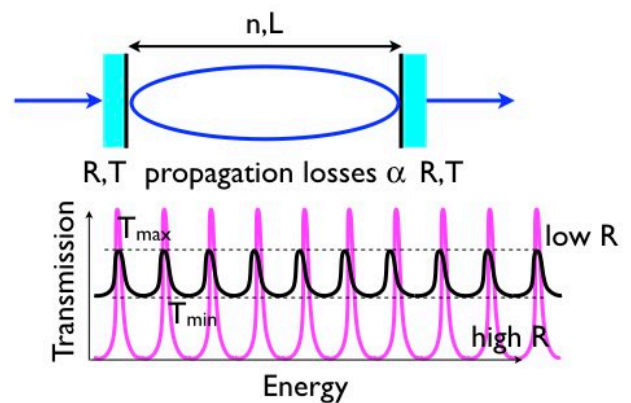
$$T_{FP} = \frac{T^2 e^{-\alpha L}}{1 + R^2 e^{-2\alpha L} - 2R e^{-\alpha L} \cos\left(\frac{4\pi n L}{\lambda}\right)}$$

$$T_{\min} = \frac{T^2 e^{-\alpha L}}{(1 + R e^{-\alpha L})^2} \quad T_{\max} = \frac{T^2 e^{-\alpha L}}{(1 - R e^{-\alpha L})^2}$$

$$u = \sqrt{\frac{T_{\min}}{T_{\max}}} = \sqrt{\frac{P_{\min}}{P_{\max}}}$$

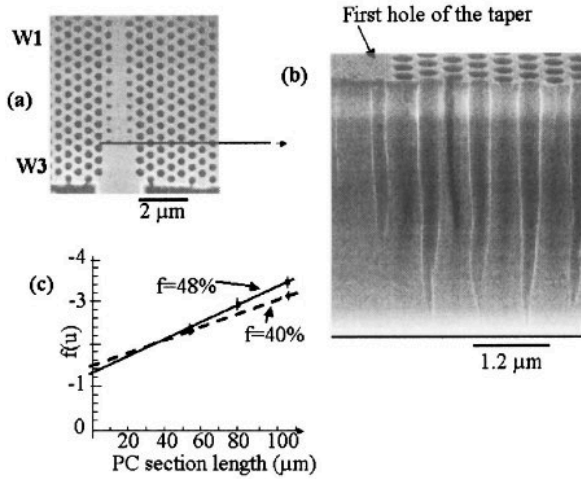
- $u^2 =$ inverse of the fringe contrast P_{\max}/P_{\min}
- does not require quantitative measurement

$$f(u) = \ln\left(\frac{1-u}{1+u}\right) = \ln(R) - \alpha L$$



Measurement of R,T and propagation losses

Example



InP

A. Talneau et al., Appl. Phys. Lett., 82, 2577, (2003)
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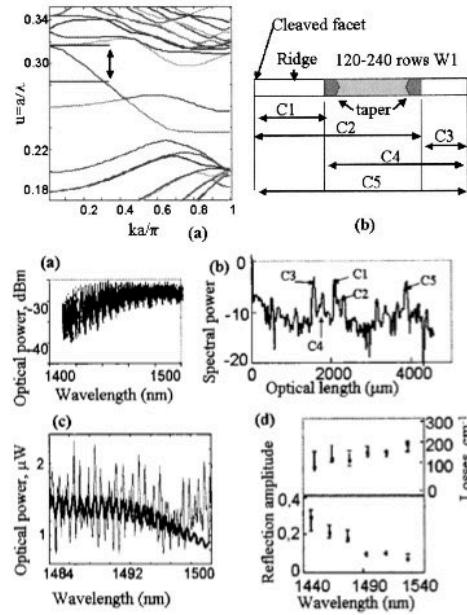


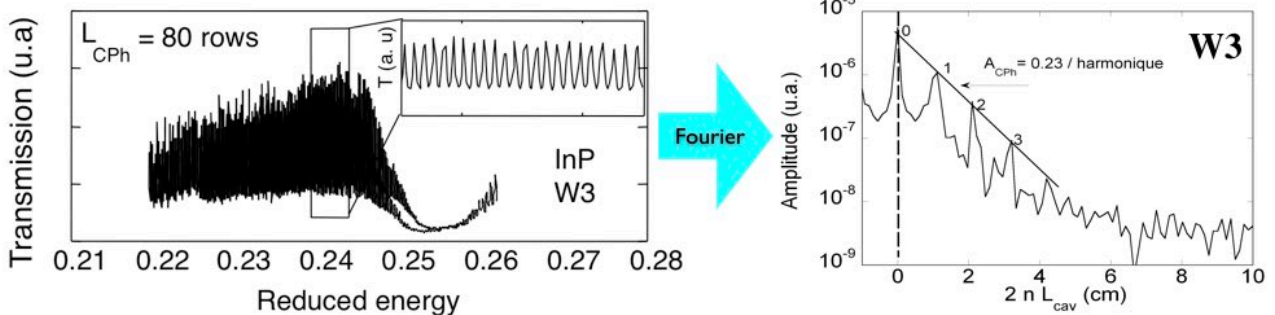
FIG. 3. 120 rows long W1-PCW with taper access: (a) transmitted power spectrum, (b) spectral power on the 1484–1500 nm window, (c) unfiltered (thin line) and filtered (bold line) transmitted power with a filter suited to C1 cavity, and (d) taper reflection and propagation losses as a function of wavelength.

The method has also been used in the case of several coupled cavities with Fourier filtering
Exact theoretical proof of validity is missing

Measurement of R,T and propagation losses

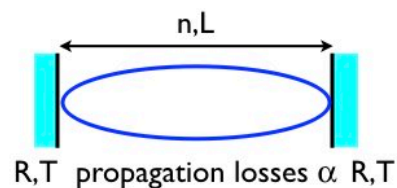
Hofstetter method

the Hofstetter method generalises the Hakki-Paoli method to the higher orders of the Fourier transform of the transmission spectrum



Amplitude decay of the harmonic n
 A_r = attenuation after n single passes

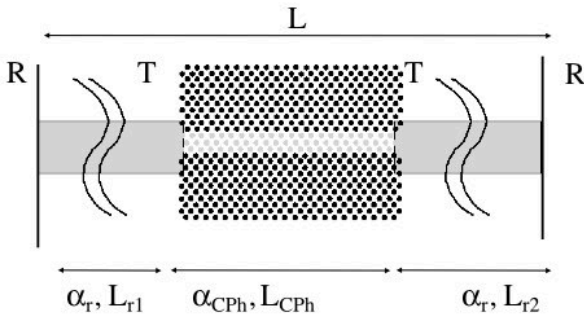
$$A_{r,n} = R^n e^{-\alpha n L}$$



D. Hofstetter et al., Opt. Lett., 22, 1381, (1997) and IEEE J. Quant. Elect., 34, 1914, (1998)
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Measurement of R,T and propagation losses

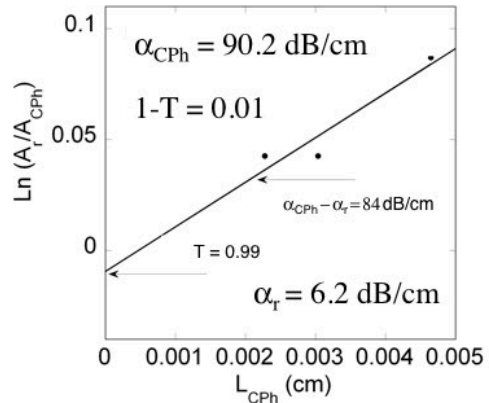
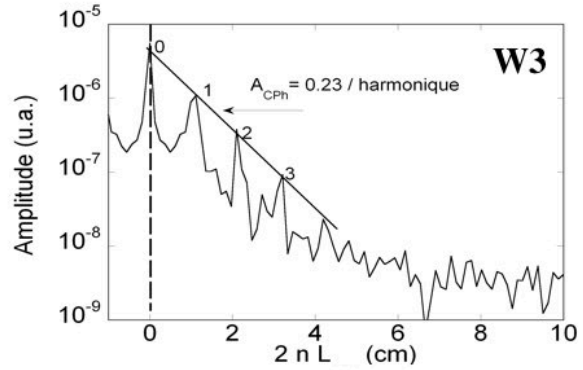
Hofstetter method



$$A = R.T^2 e^{-\alpha_{CPh}L_{CPh}} e^{-\alpha_R(L_{r1}+L_{r2})}$$

after division by a reference waveguide

$$\ln(A_r/A_{CPh}) = -\ln T^2 + (\alpha_{CPh}-\alpha_r)L_{CPh}$$



D. Hofstetter et al., Opt. Lett., 22, 1381, (1997) and IEEE J. Quant. Elect., 34, 1914, (1998)

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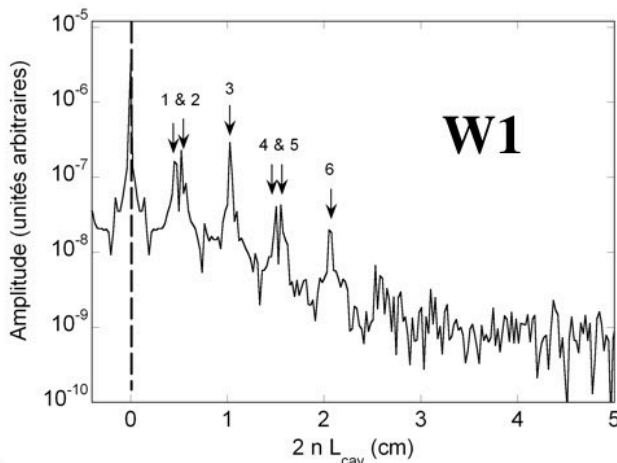
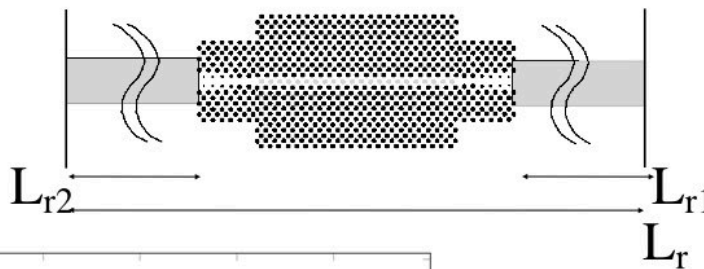
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Measurement of R,T and propagation losses

Hofstetter method

Internal reflections lead to multiple cavities



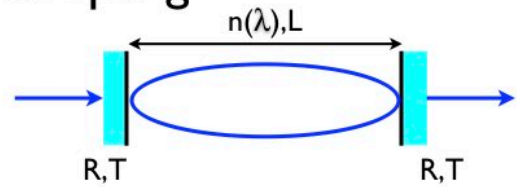
- harmonics 1 and 4 : L_{r1}
- harmonics 2 and 5 : L_{r2}
- harmonics 3 and 6 : L_r



Dispersion curve

Fabry-Perot fringes and k-space sampling

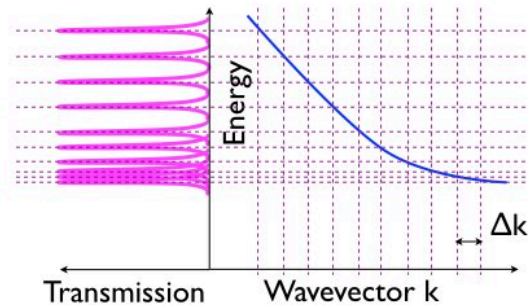
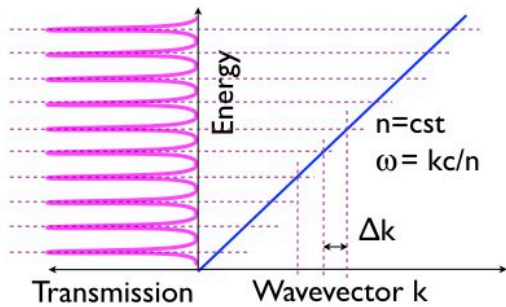
Fabry-Perot fringes equally spaced in energy ?



$$T_{FP} = \frac{T^2}{1 + R^2 - 2R \cos\left(\frac{4\pi nL}{\lambda}\right)}$$

$$T_{FP} = \frac{T^2}{1 + R^2 - 2R \cos(2kL)}$$

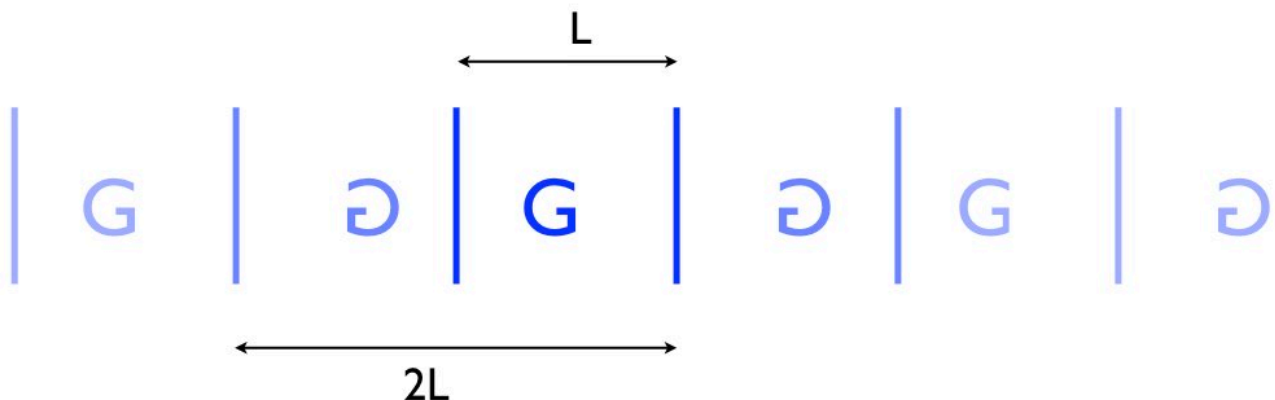
resonances equally spaced in k $\Delta k = \pi/L$



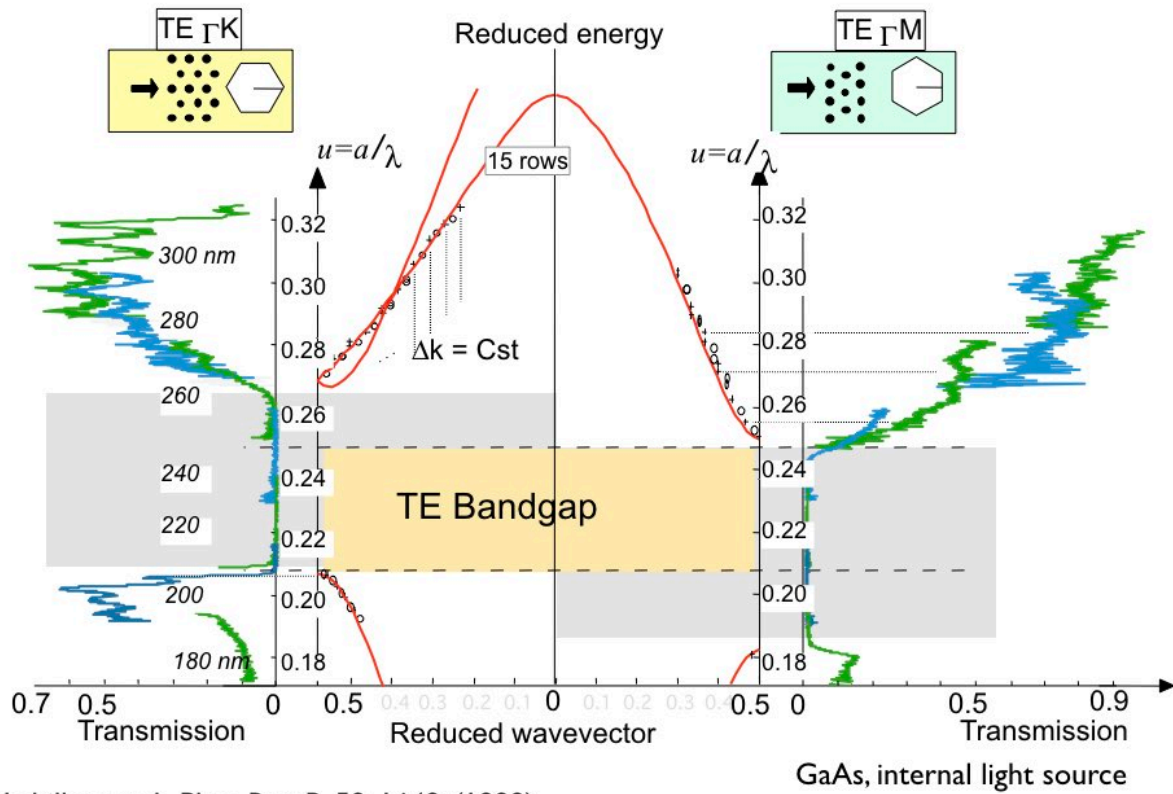
Note: sampling in Δk , exact k values are more difficult to determine

Sampling

A simple way to see that, consists in unfolding the images from both mirrors. This leads to a periodic structure with period $2L$ and a $2\pi/2L = \pi/L$ periodicity in k-space



Dispersion curve measurement



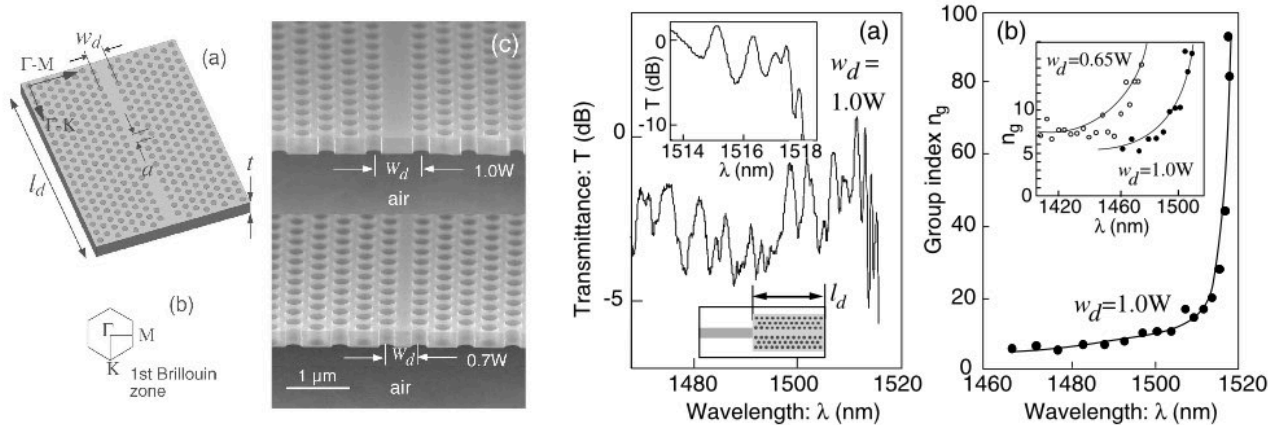
D. Labilloy et al., Phys. Rev. B, 59, 1649, (1999)

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Dispersion curve measurement



Si membrane

M. Notomi et al., Phys. Rev. Lett., 87, 253902, (2001)

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Dispersion curve measurement

Mach-Zehnder interferometer

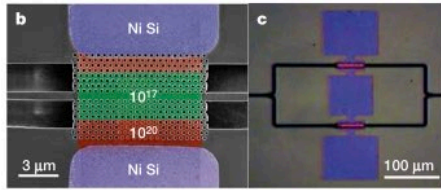


Figure 3 | Active electrically tunable MZI with lateral electrical contacts to photonic crystal waveguides. a, Time averaged magnetic field energy

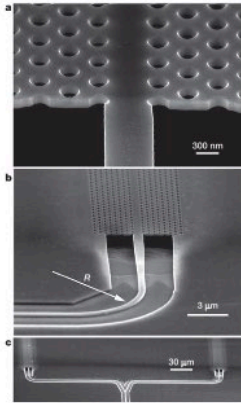
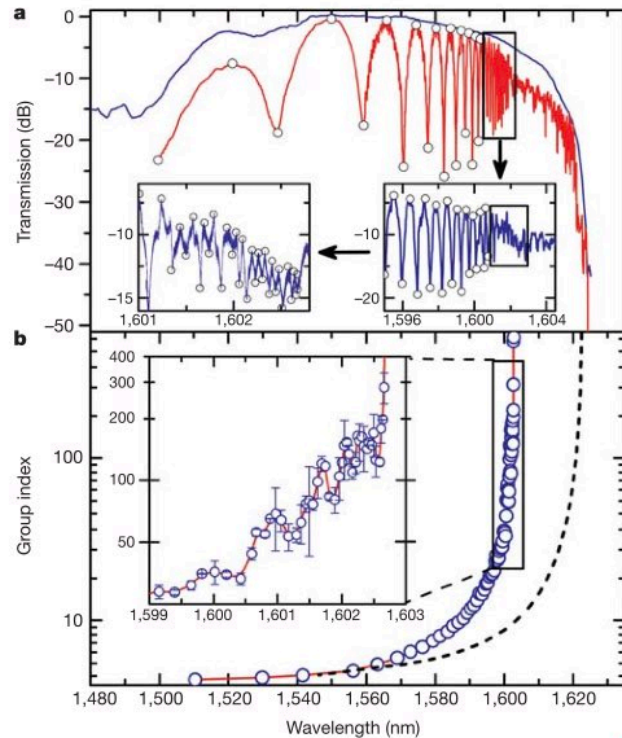


Figure 1 | SEM images of a passive unbalanced Mach-Zehnder interferometer using photonic crystal waveguides. a, Input section of the

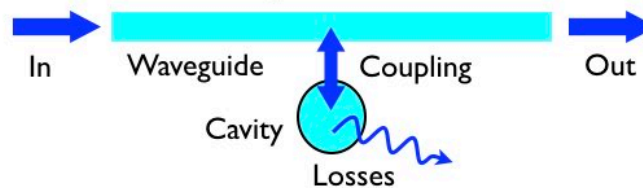
Y.Vlasov et al., Nature, 438, 65, (2005)

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Optical cavities, high quality factor

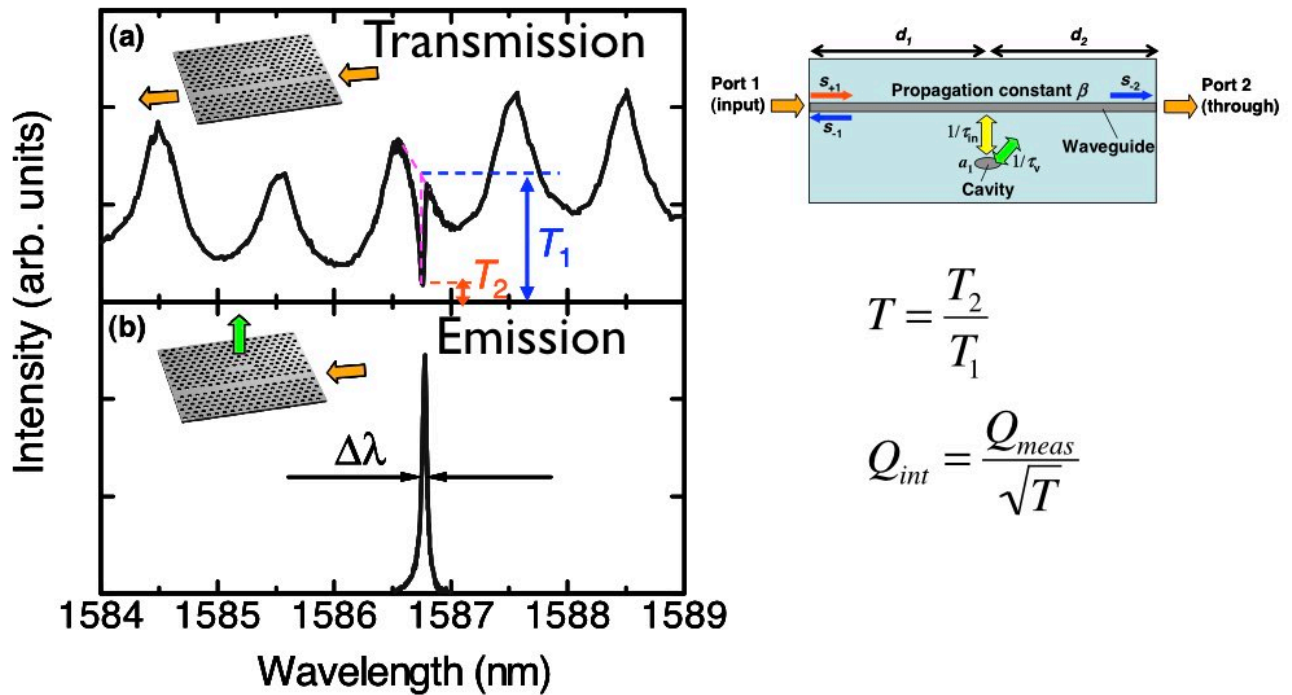
Measurement of the cavity requires coupling to a probe which affect the Q



- Intrinsic $Q = Q_{int}$, unloaded cavity, coupling only to free space radiation and material losses, defects
- Coupling $Q = Q_{probe}$, additional losses due to the measurement
- Measured $Q = Q_{meas}$, loaded cavity

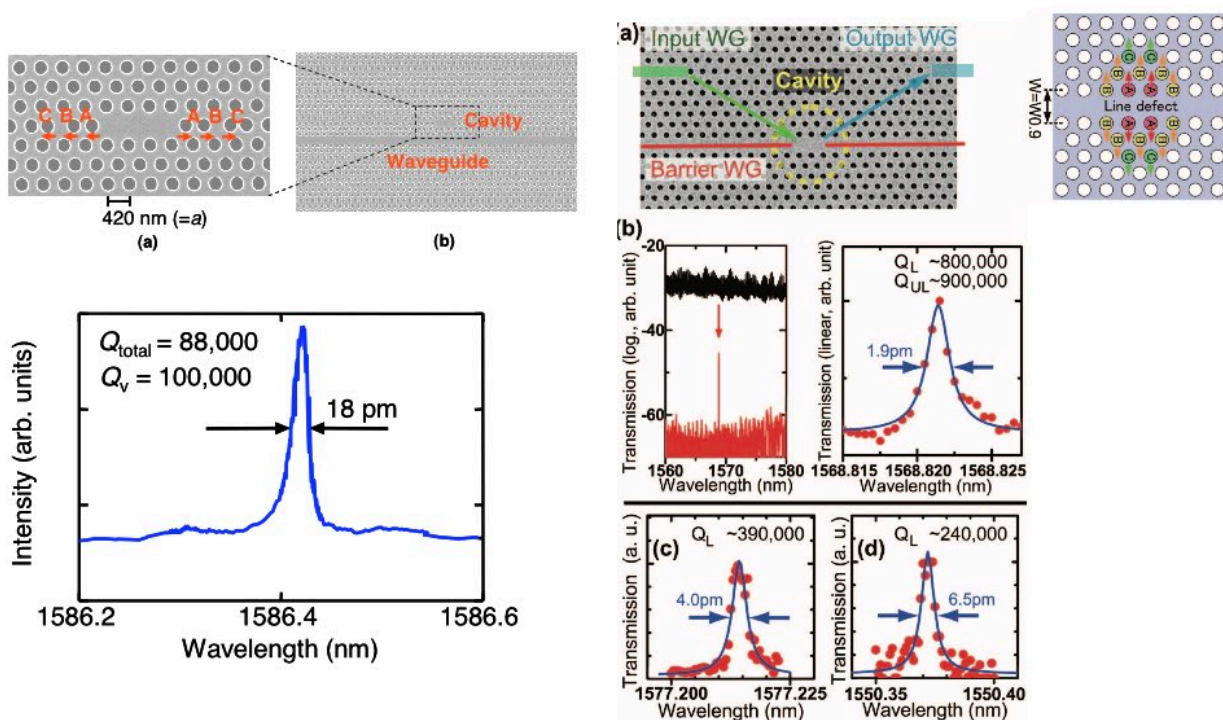
$$\frac{1}{Q_{meas}} = \frac{1}{Q_{int}} + \frac{1}{Q_{probe}}$$

Optical cavities, high quality factor



Y.Akahane et al., Opt. Exp., 13, 1202, (2005)
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Optical cavities, high quality factor



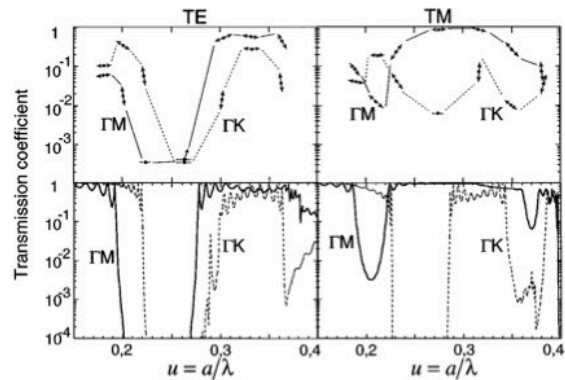
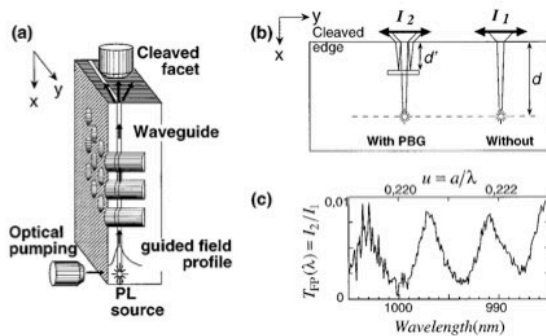
Y.Akahane et al., Opt. Exp., 13, 1202, (2005)
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E. Kuramochi et al., Appl. Phys. Lett., 88, 041112, (2006)
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Internal source ILS

Goal, a versatile technique that:

- does not require the full fabrication of device with access waveguides etc...
- allows the light source to be injected where needed
- allows quantitative measurements



D. Labilloy et al., Phys. Rev. Lett., 79, 4147, (1997)
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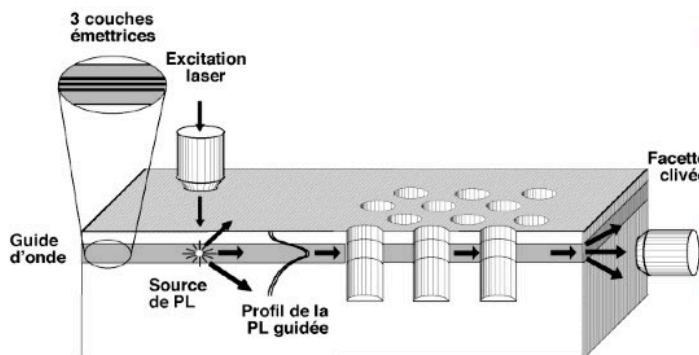
Historically, among the first actually quantitative transmission measurements on 2D PhC



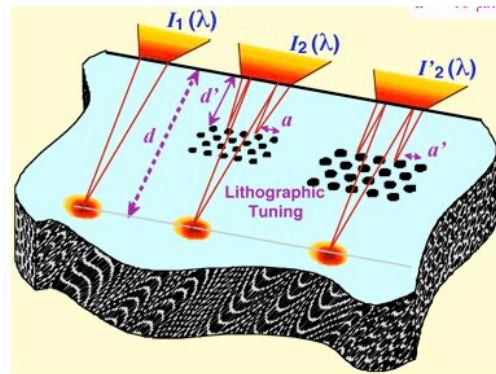
ILS

Principle: Insert light emitters inside the planar waveguide

- Quantum wells
- "bad" quantum dots (large emission band)



D. Labilloy PhD dissertation

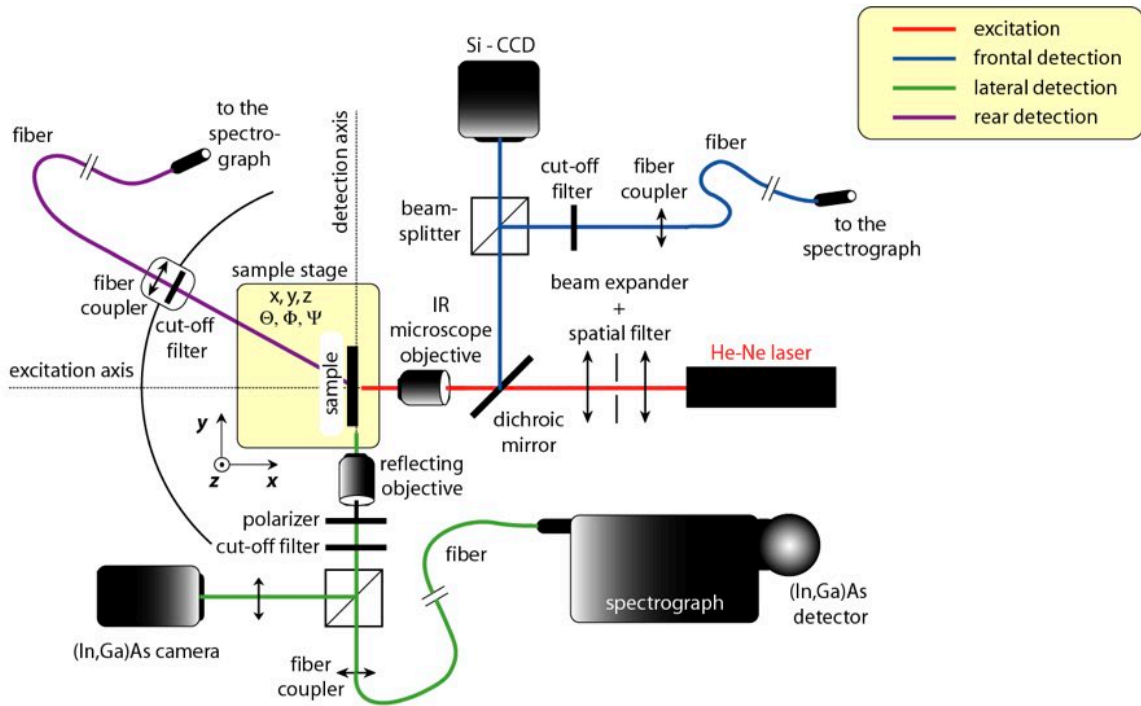


$$T_a(\lambda) = \frac{I_2(\lambda)}{I_1(\lambda)} \rightarrow T(u = \frac{a}{\lambda})$$

And make use of lithographic tuning



Experimental set-up

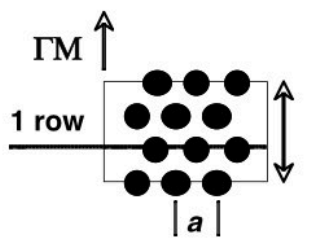


R. Ferrini et al., J. Quantum Electron., 38, 786, (2002)

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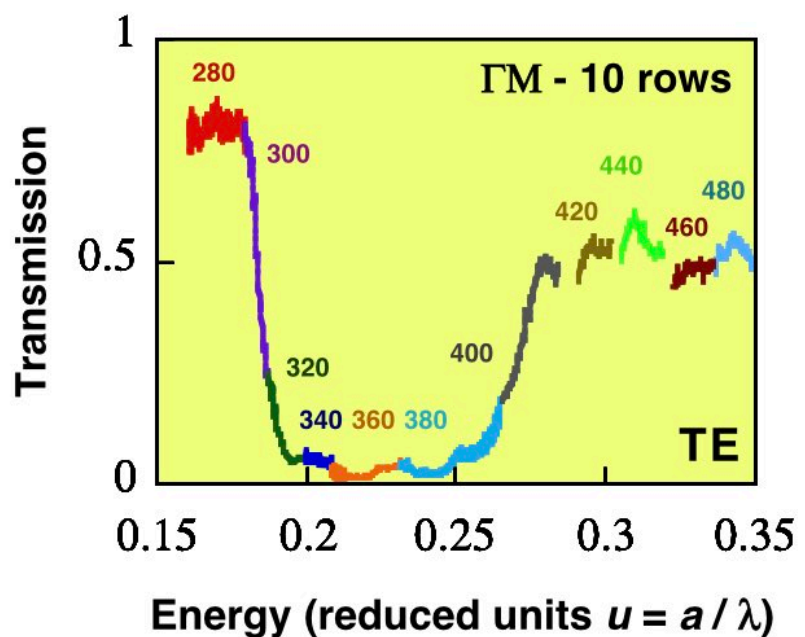
Transmission spectrum

Examples



TE polarization

InP/(Ga,In)(As,P) QW
 $\lambda = 1.55 \mu\text{m}$ $f = 30\%$

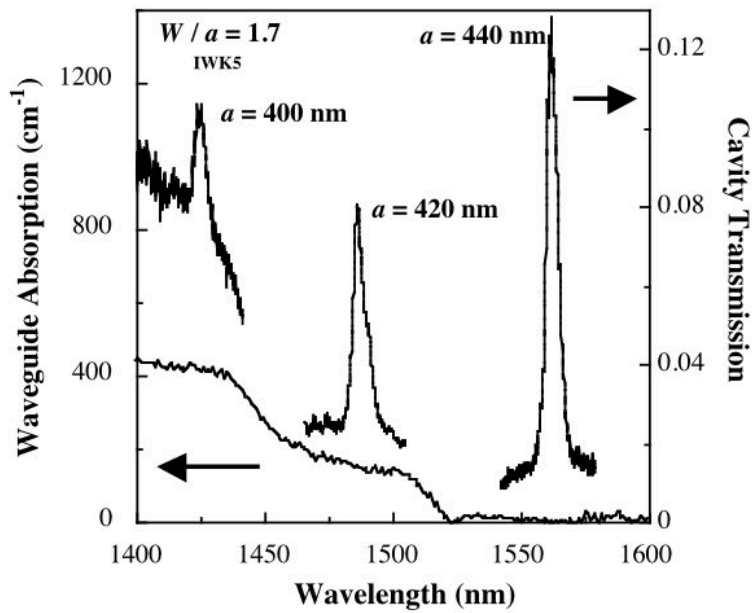


R. Ferrini et al., J. Quantum Electron., 38, 786, (2002)

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Limitation

QW or QD absorption in the waveguide

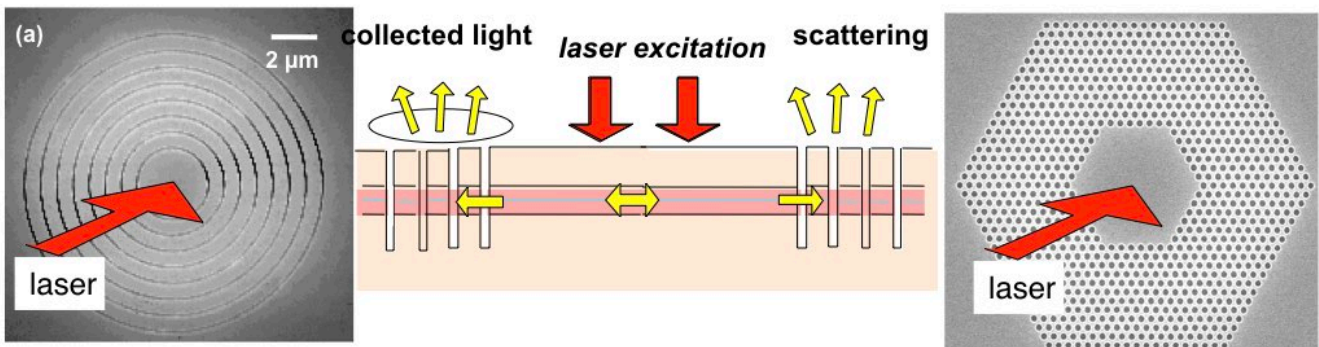


Photoluminescence

Light source inside the PhC structure

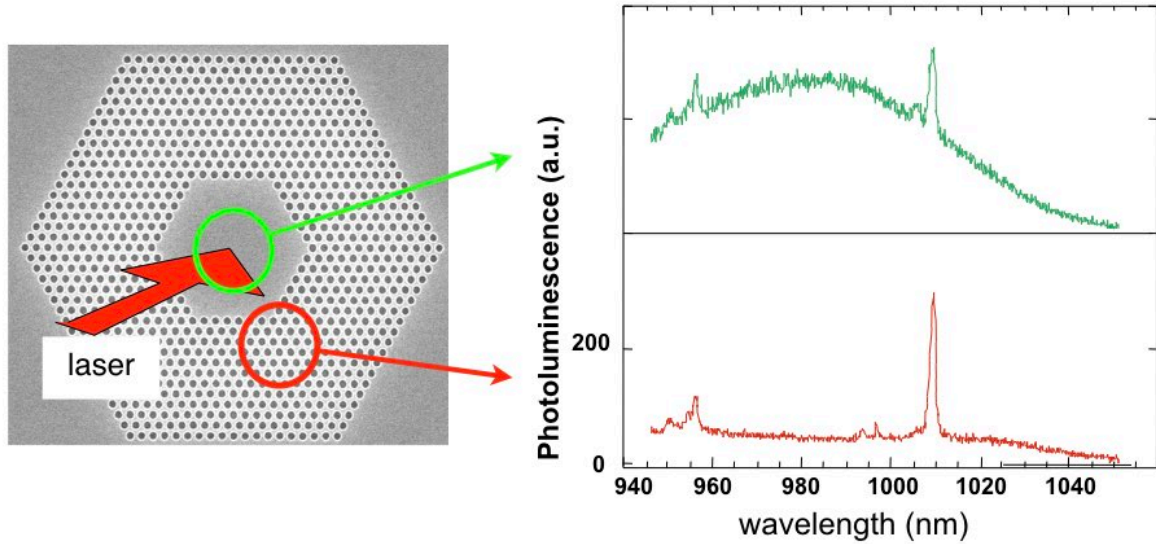
- PhC defect
 - Point defect, optical cavity

Front photoluminescence emission



Photoluminescence

Mode spectroscopy



C.J.M. Smith et al., JOSA B, 17, 2043, (2000)

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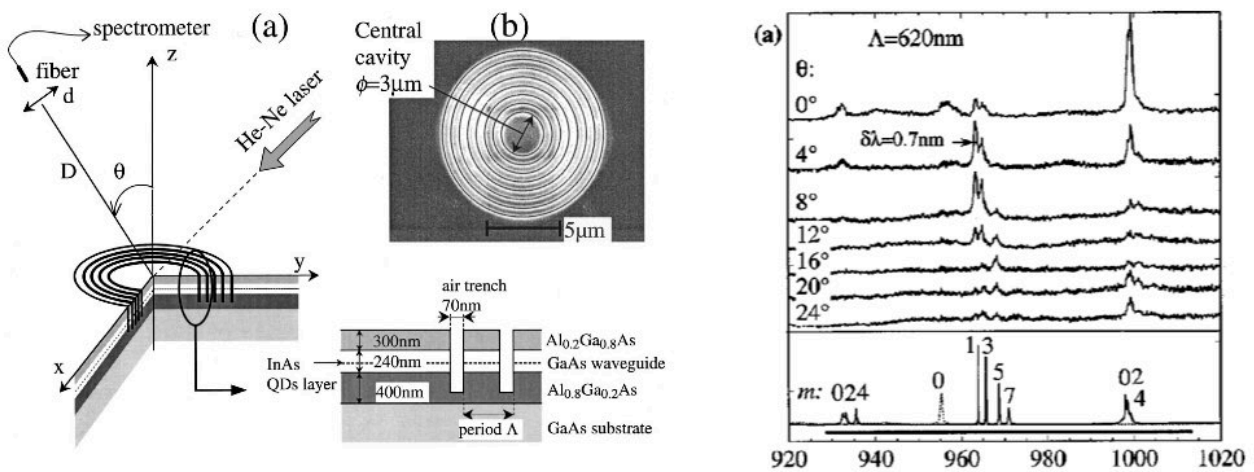
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Photoluminescence

Mode spectroscopy

Coupled with angular resolution



D. Ochoa et al., Phys. Rev. B, 61, 4806, (2000)

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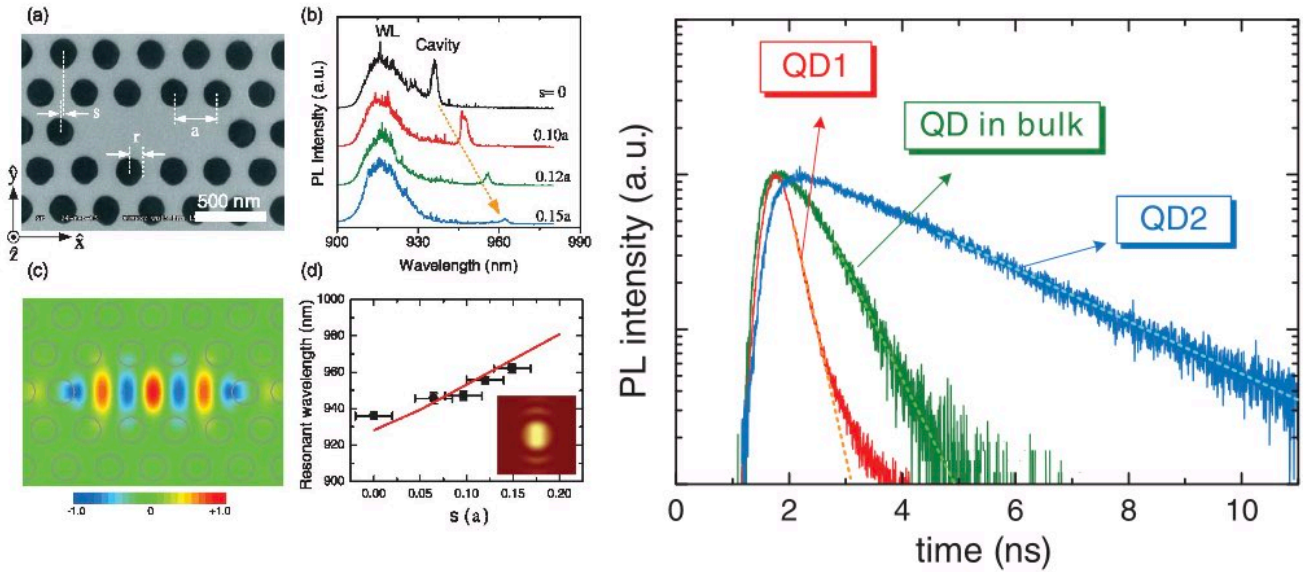
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Photoluminescence

Time resolved

Life time modification, Purcell effect, emission enhancement and inhibition



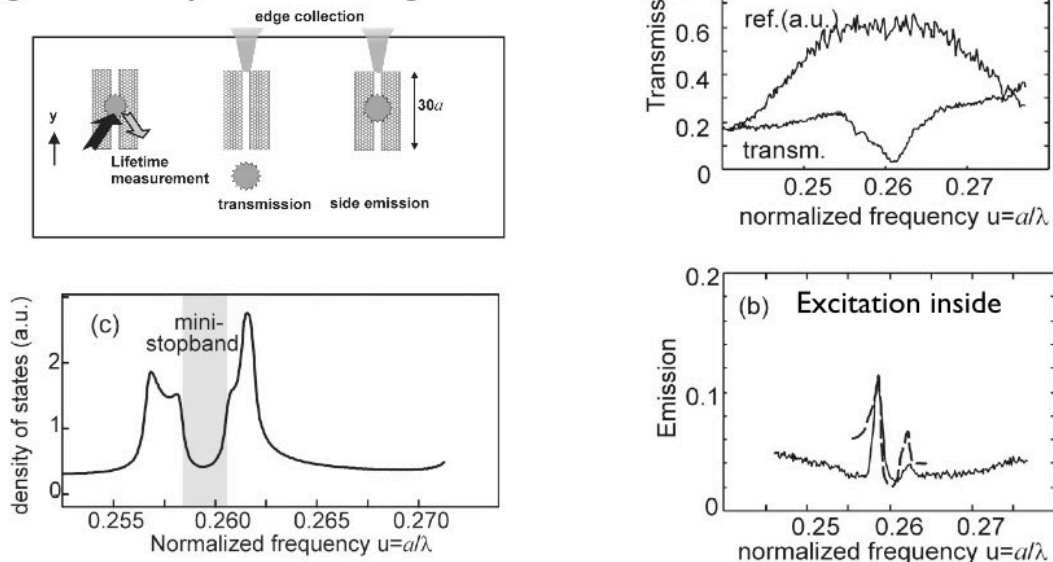
Wen-Hao Chang et al., Phys. Rev. Lett. 96, 117401, (2006)
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Photoluminescence

Light source inside the PhC structure

- PhC defect
- Line defect, waveguide

Probing the density of states singularities



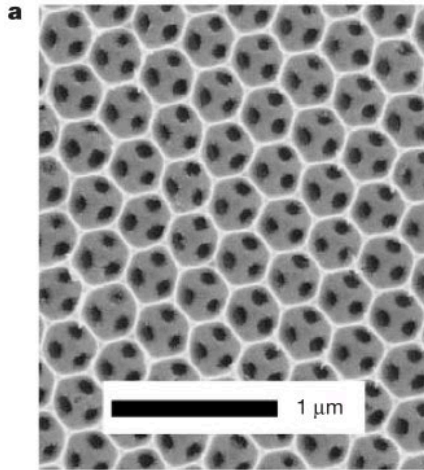
E. Viasnoff-Schwob et al., Phys. Rev. Lett., 95, 183901, (2005)
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Photoluminescence

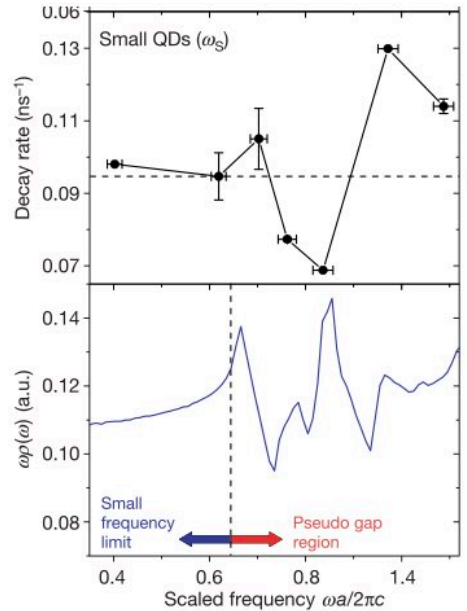
Light source inside the PhC structure

- Bulk 3D PhC

Probing the local density of states singularities, lifetime modification



CdSe nanocrystals in inverted opals



P. Lodahl et al., Nature, 430, 654, (2004)

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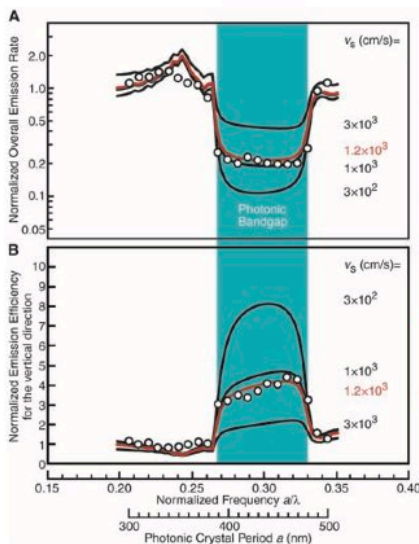


Photoluminescence

Light source inside the PhC structure

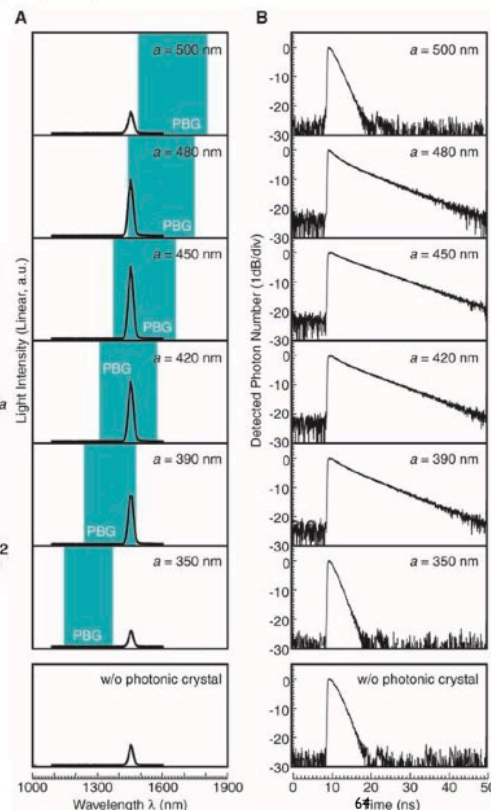
- Bulk 2D PhC

Probing the local density of states singularities, lifetime modification



M. Fujita et al., Science, 308, 1296, (2005)

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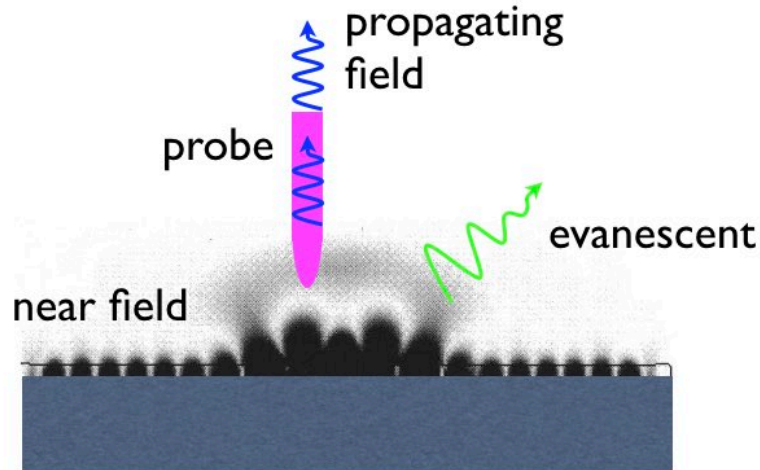


Advanced techniques

Local probes, SNOM

Principle

Probe the near field electromagnetic field with a local probe

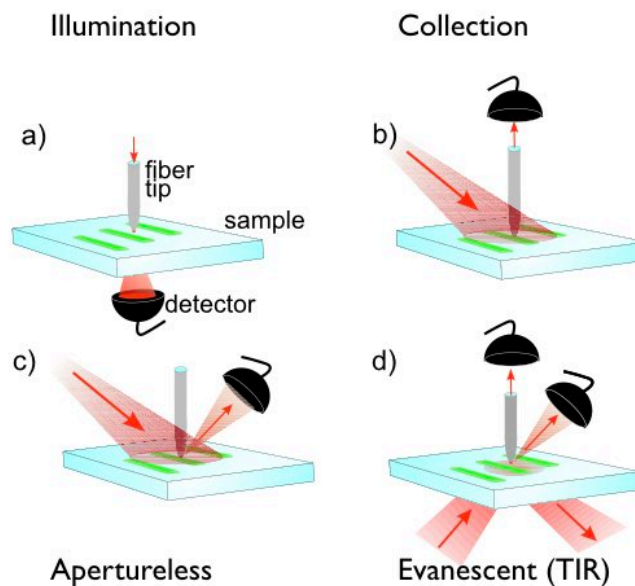


Advanced techniques

Local probes, SNOM

Principle

Different configurations

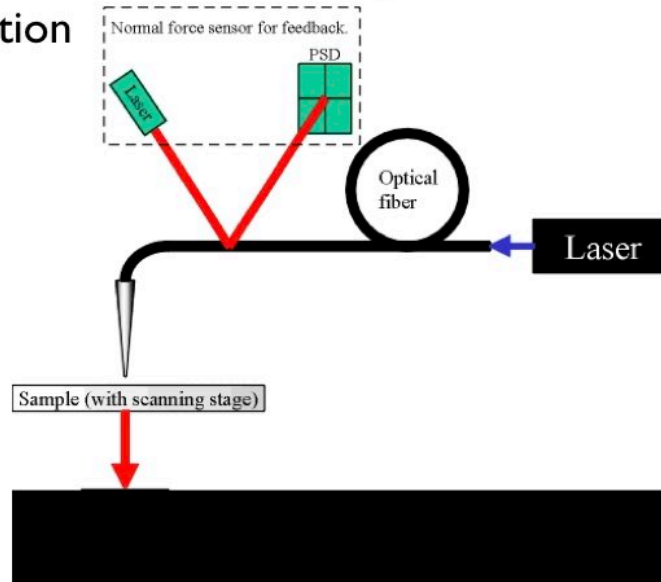


Advanced techniques Local probes, SNOM

Principle

Tricks are in :

- Tip position control, as in STM, AFM
- Tip fabrication

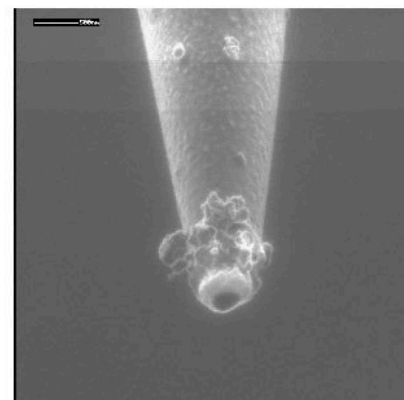
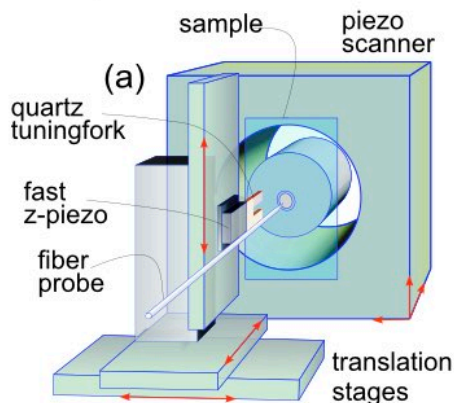


Advanced techniques Local probes, SNOM

Principle

Tricks are in :

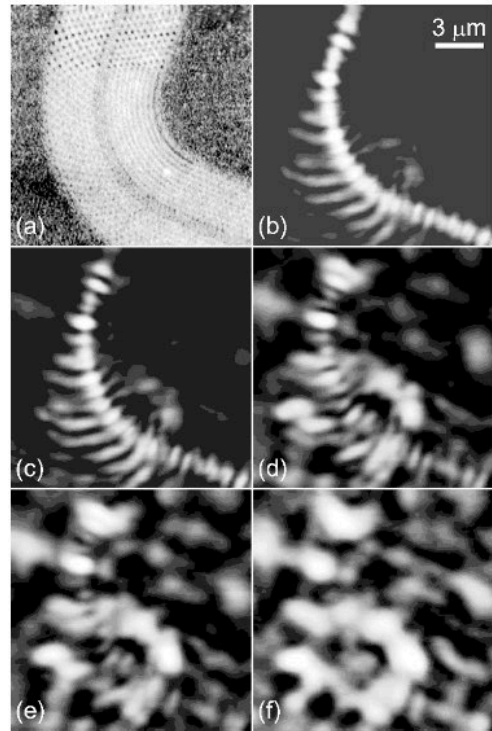
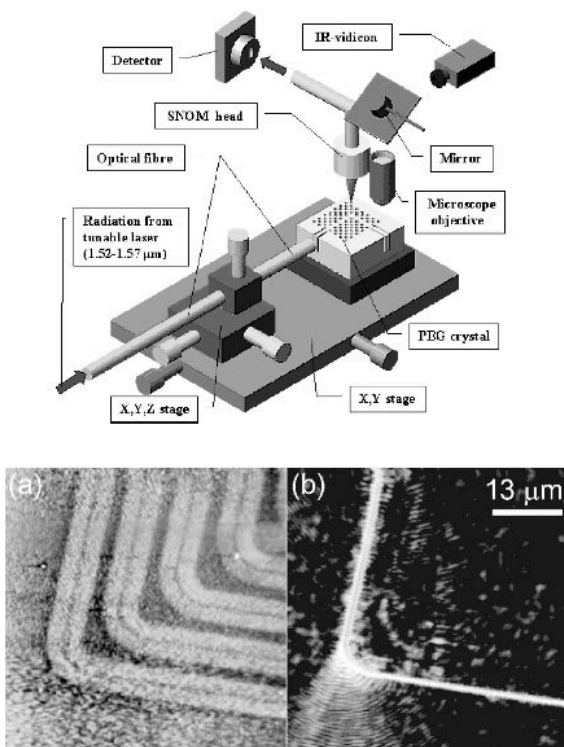
- Tip position control, as in STM, AFM
- Tip fabrication



Metallized tapered fibre tip. SEM, H. Gersen

SNOM

Examples, bends

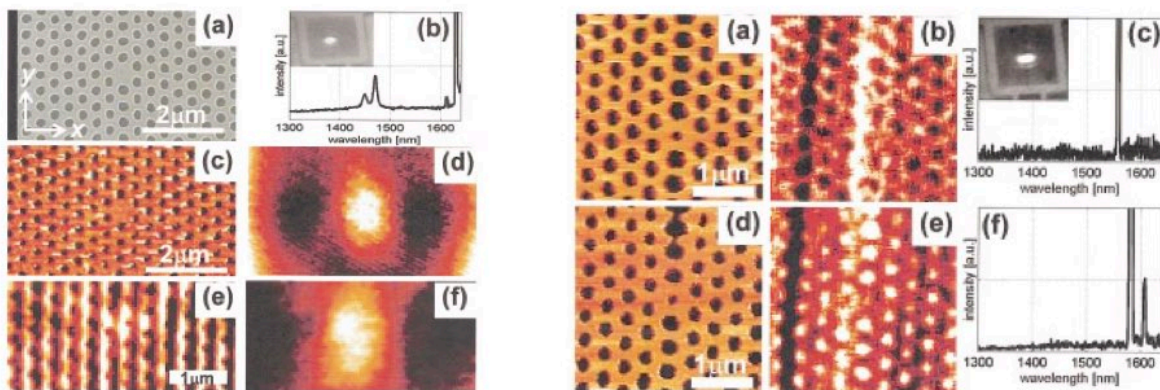
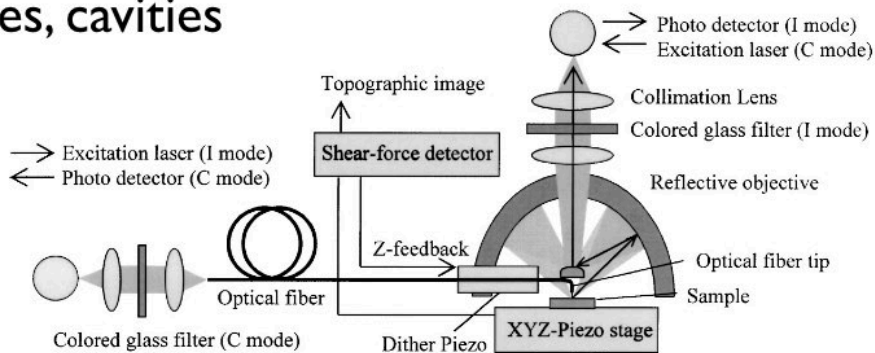


with increasing shear force feedback (increasing tip distance)

S.I. Bozhevolnyi et al., Phys. Rev. B, 66, 235204, (2002)
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Examples, cavities

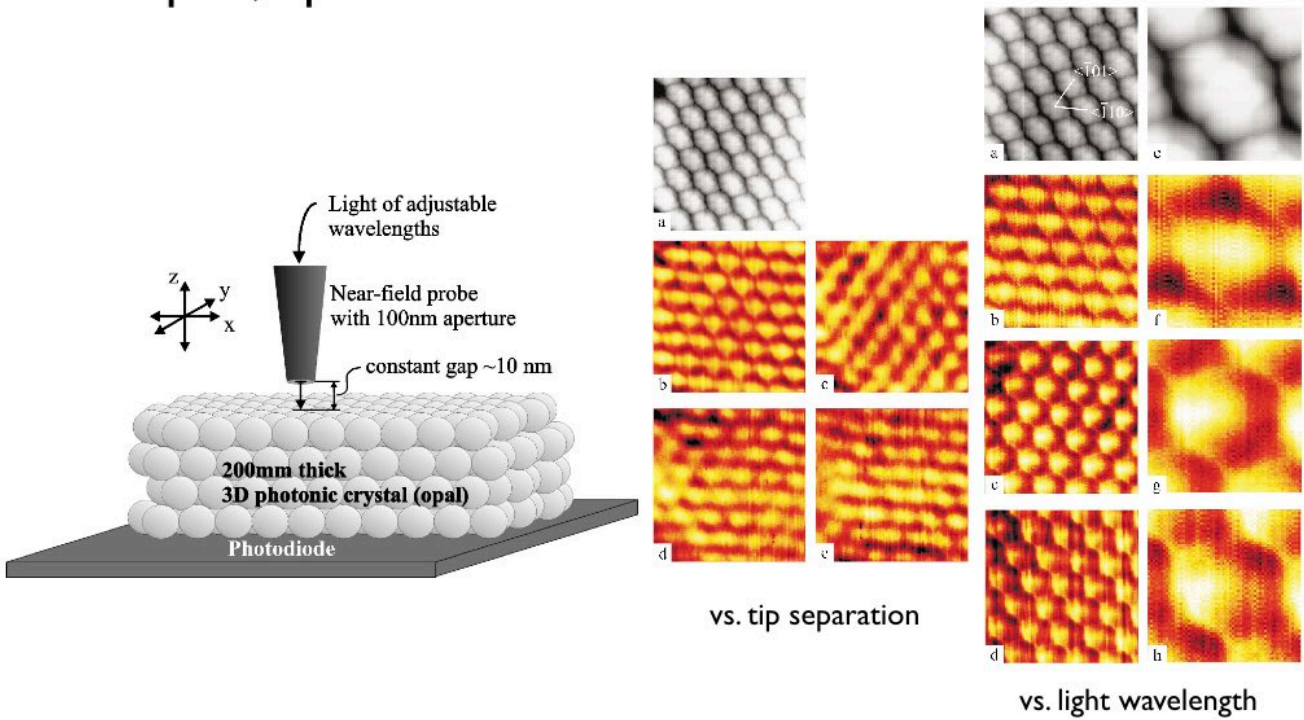


K. Okamoto et al., Appl. Phys. Lett., 82, 1676, (2003)

Nice images, but difficult to be quantitative

SNOM

Examples, opals



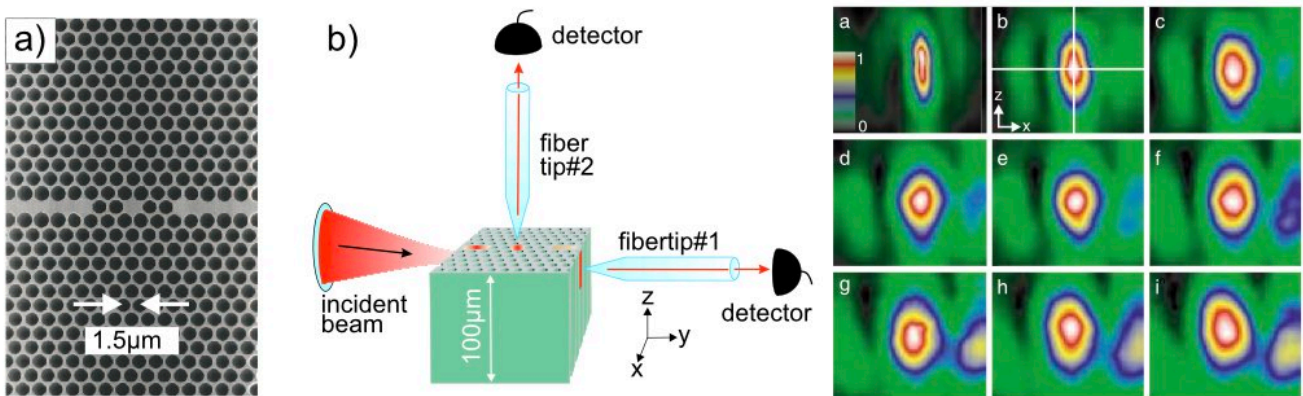
vs. tip separation

vs. light wavelength

E. Flück et al., Phys. Rev. E, 68, 015601R, (2003)
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SNOM

Examples, 2D macroporous PhC

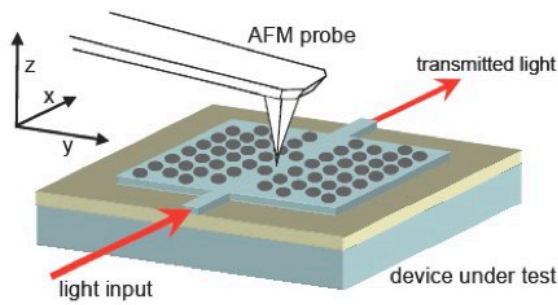


vs. tip | distance

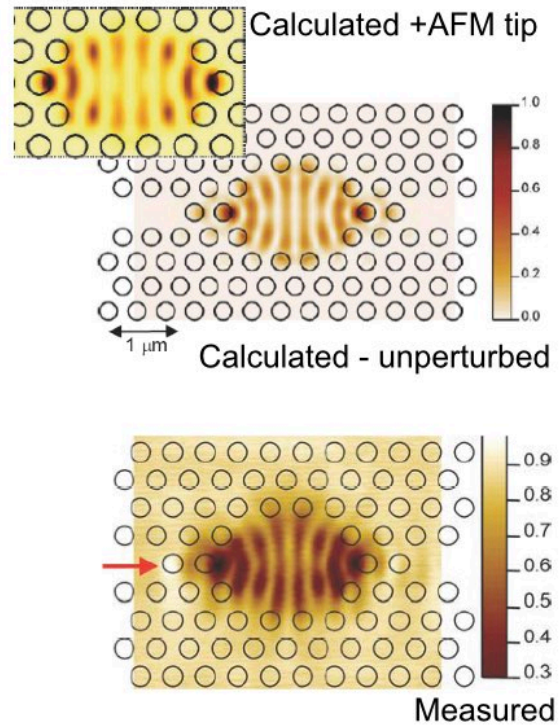
V. Sandogdhar et al., Phys. Rev. Lett., 92, 113903, (2004)
 Ecole doctorale photonique, Photonic crystals, PHYS-605, Romuald Houdré, Summer semester 2017

T-SNOM

Mode field pattern mapping or modification with AFM tip



- scanning tip smaller, lower perturbation
- for small high Q cavities
- tip – change in Q factor or resonance wavelength

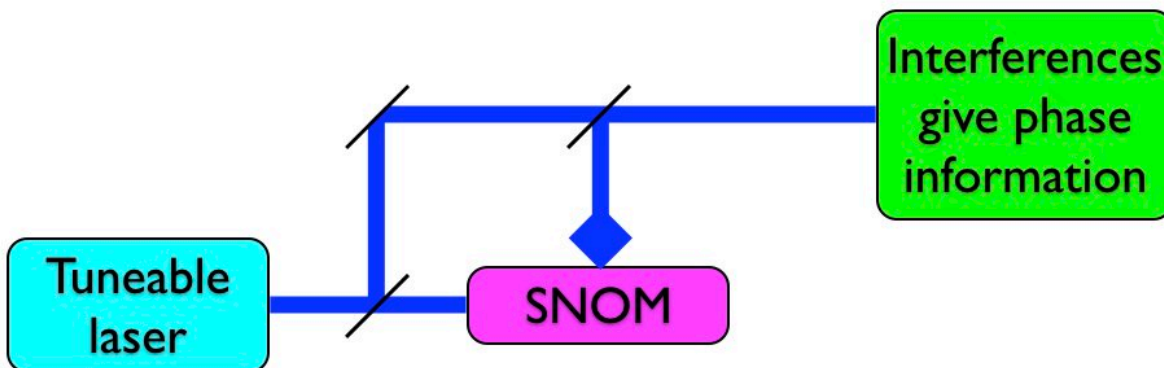


R. De Ridder, Twente, ECIO 2007 and Opt. Exp., 14, 8745 (2006)
Ecole doctorale photonique, Photonic crystals, PHYS-605, Romuald Houdré, Summer semester 2017

Advanced techniques "Heterodyne" SNOM

Usual SNOM measures intensity, what about amplitude ?
(i.e. intensity and phase)

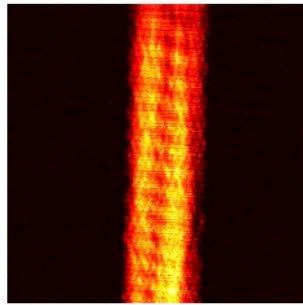
Insert the SNOM set-up in an interferometer (e.g. Mach-Zender)



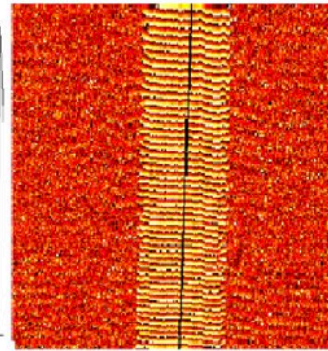
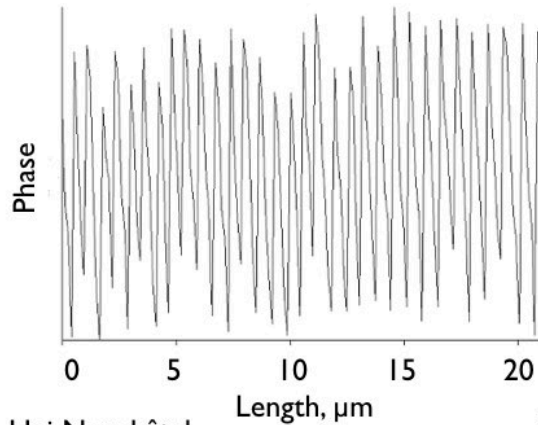
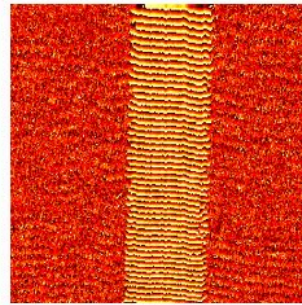
Note : amplitude information is necessary e.g. for numerical Fourier transform

Advanced techniques Heterodyne SNOM

Amplitude



Phase



scan area of $35 \times 35 \mu\text{m}^2$

Courtesy I. Märki, Uni Neuchâtel

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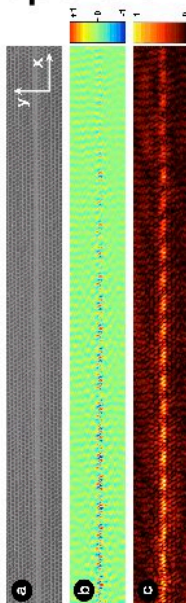
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Heterodyne SNOM

Once *amplitude* is known, Fourier transform gives information on the Bloch wave

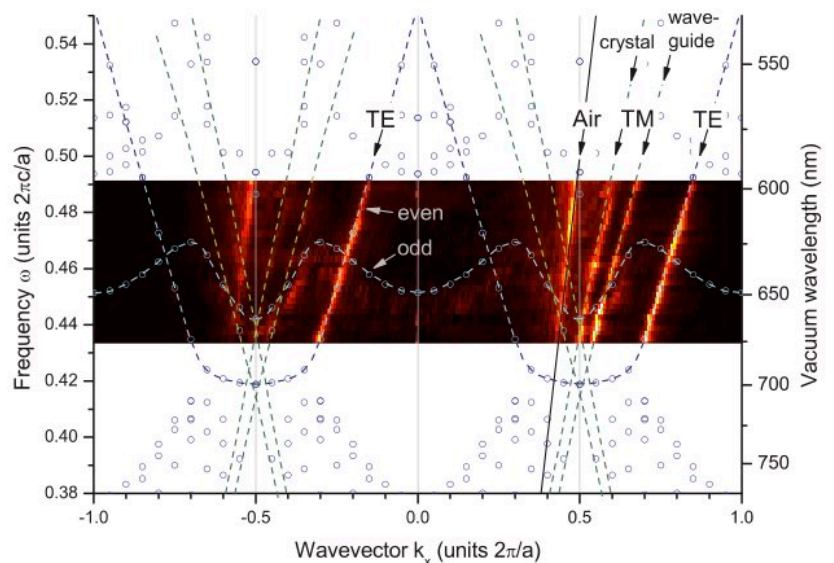
- Dispersion curves



$$A \cdot \cos(\phi) |A|$$

R.J.P. Engelen et al., *Opt. Exp.*, 13, 4457, (2005)

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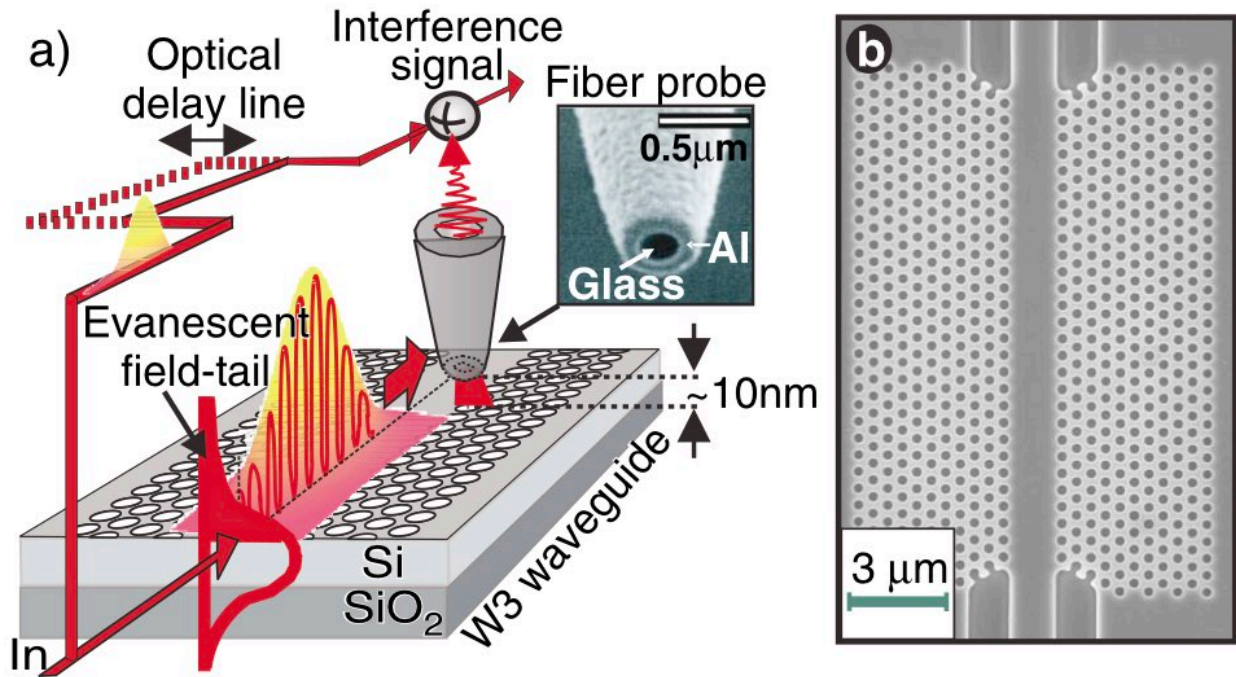
Fourier transform

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Advanced techniques

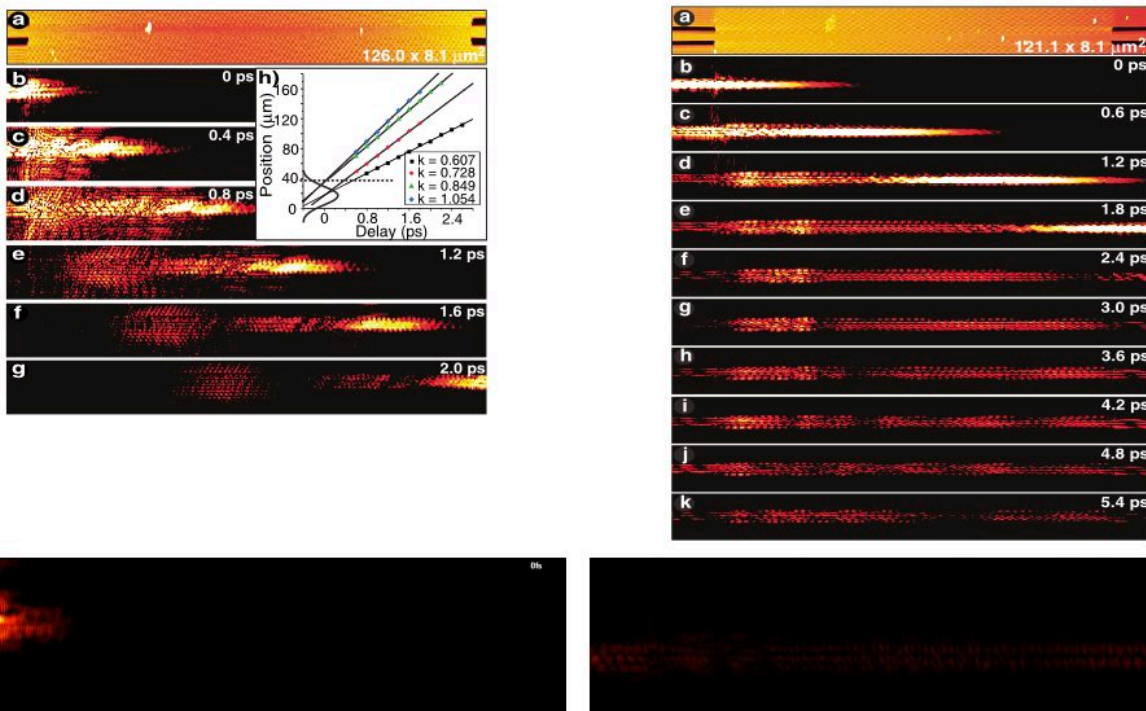
Time resolved SNOM



H. Gersen et al., Phys. Rev. Lett., 94, 073903, (2005)
Ecole doctorale photonique, Photonic crystals, PHYS-605, Romuald Houdré, Summer semester 2017

Advanced techniques

Time resolved SNOM

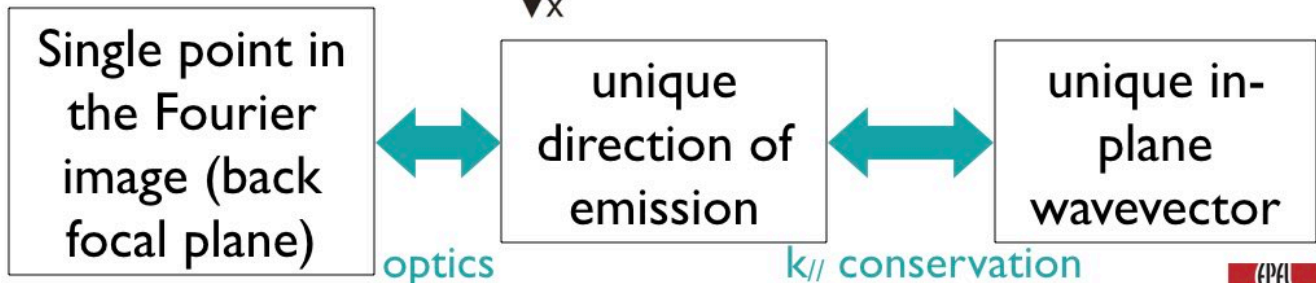
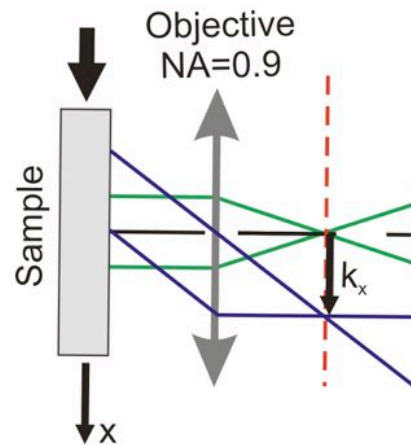


H. Gersen et al., Phys. Rev. Lett., 94, 073903, (2005)
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Advanced techniques

High Numerical Aperture Fourier Space Imaging of Planar Photonic Crystals

Principle



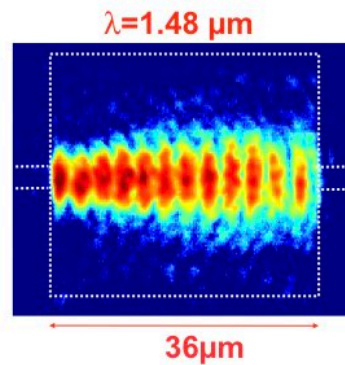
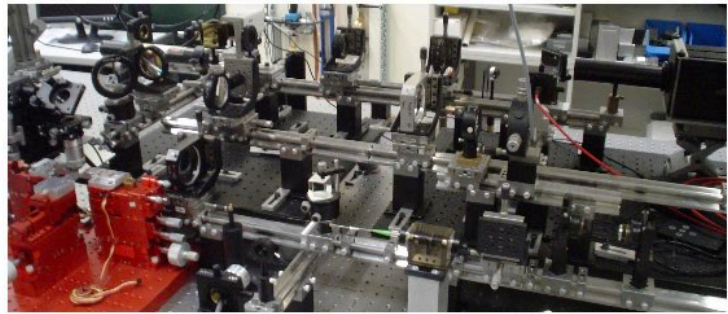
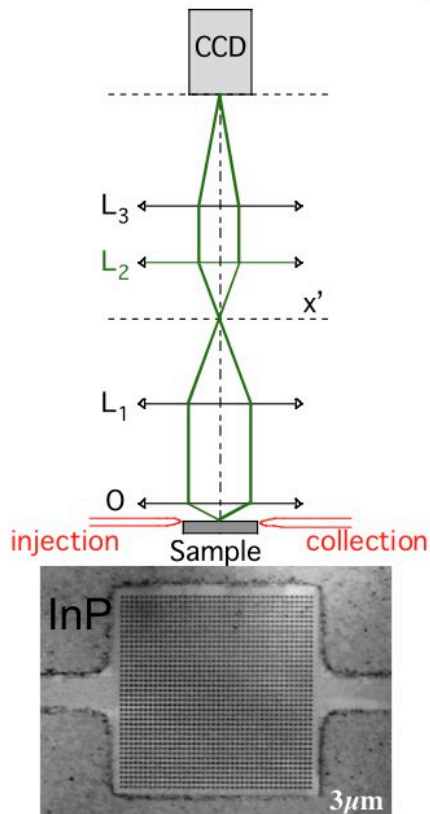
Fourier imaging

Principle

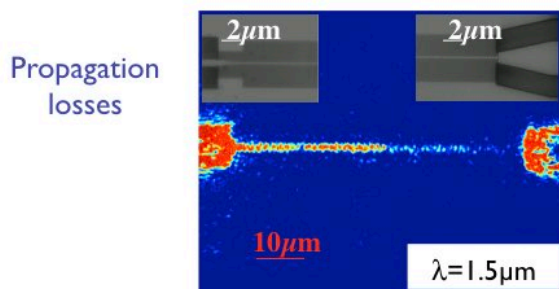
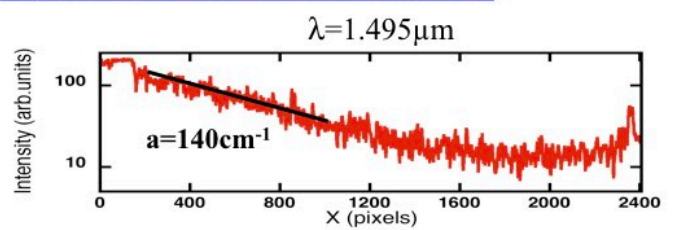
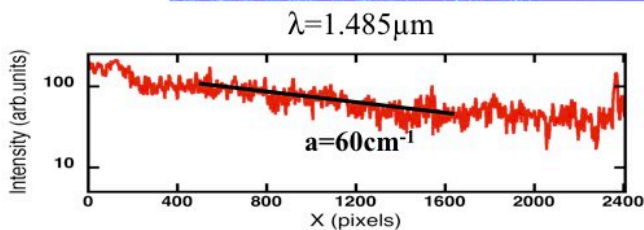
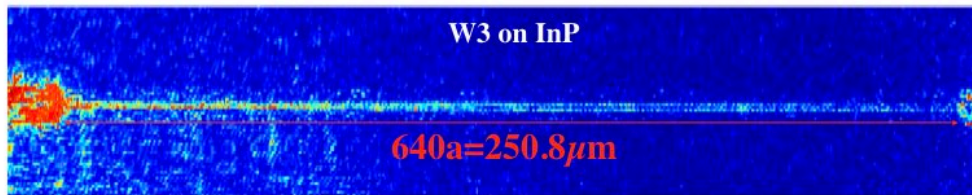
Make use of the light scattered off the propagation axis or plane

- * intrinsically (above the light line)
- * via imperfections / defects (below the light line)
- * additional probe structures

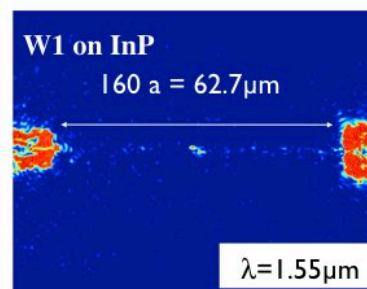
Real space imaging of Bloch Waves propagating in PhCs



Imaging of the scattered light Propagation losses and defect characterization



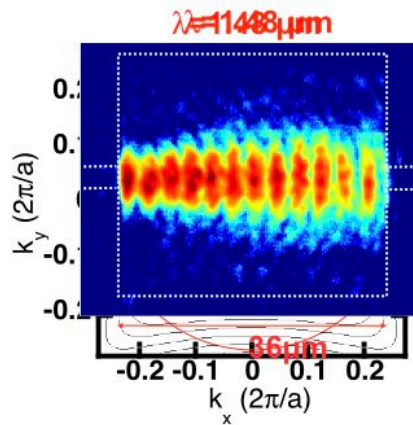
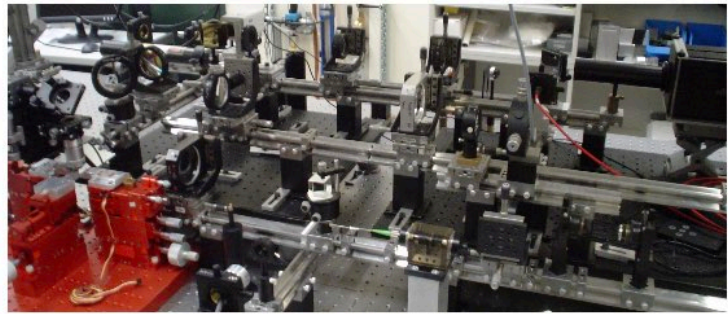
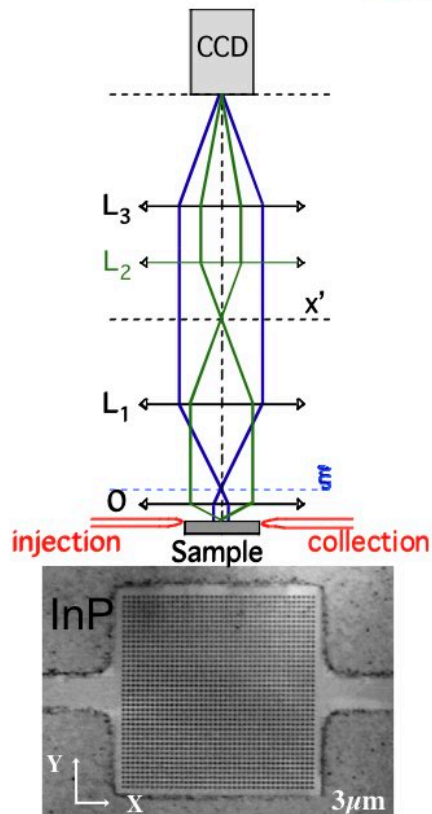
$u = 0.261$



$u = 0.253$

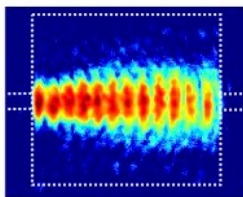
Defect

Fourier space imaging of Bloch wave emission diagram

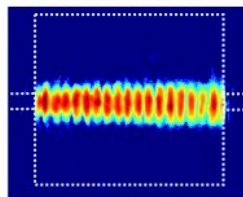


Equi-Frequency surfaces mapping in PhCs

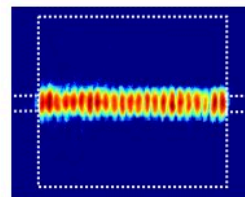
Real space



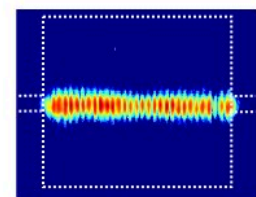
$\lambda = 1.48 \mu\text{m}$



$\lambda = 1.51 \mu\text{m}$

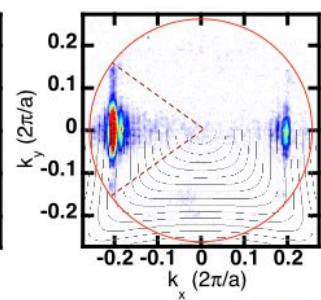
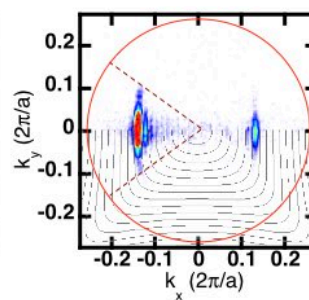
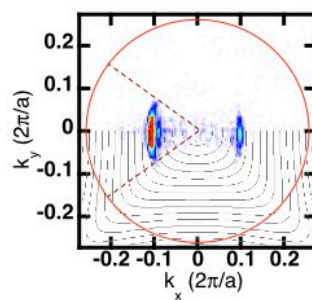
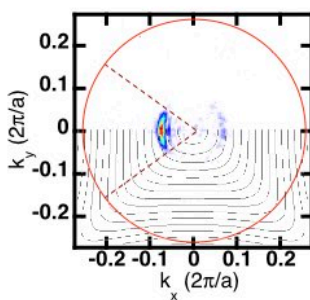


$\lambda = 1.55 \mu\text{m}$

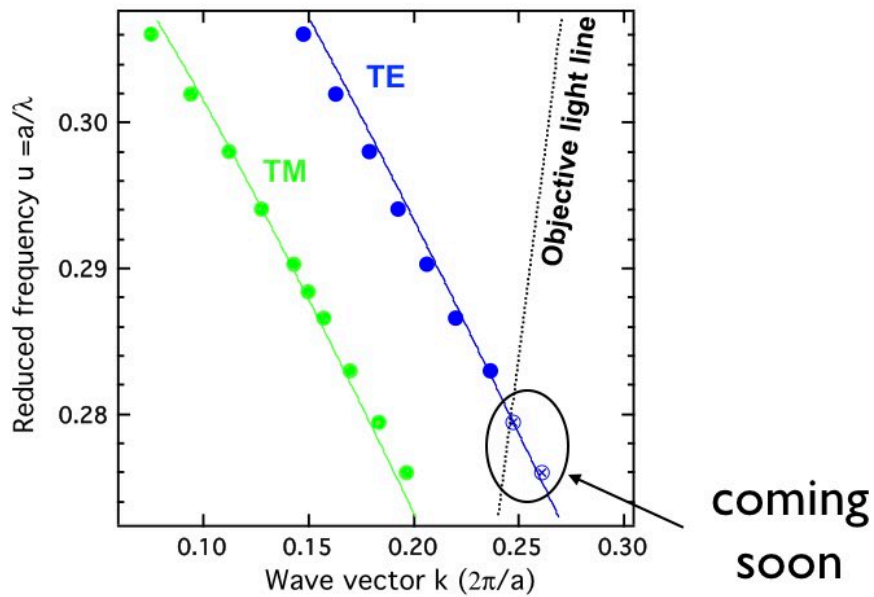


$\lambda = 1.63 \mu\text{m}$

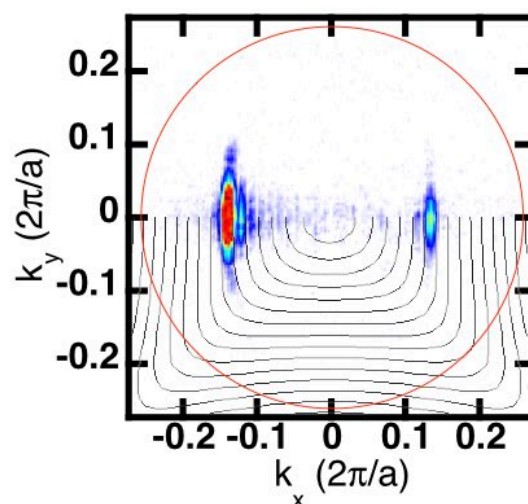
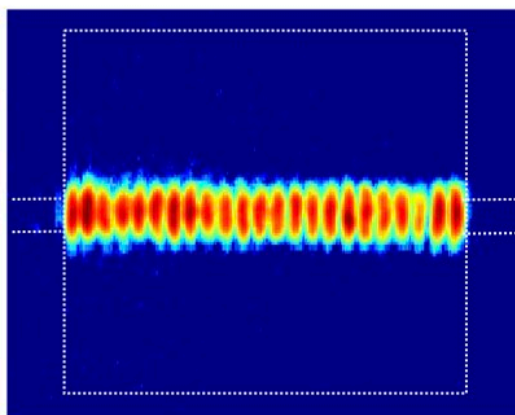
Fourier space



Dispersion curves



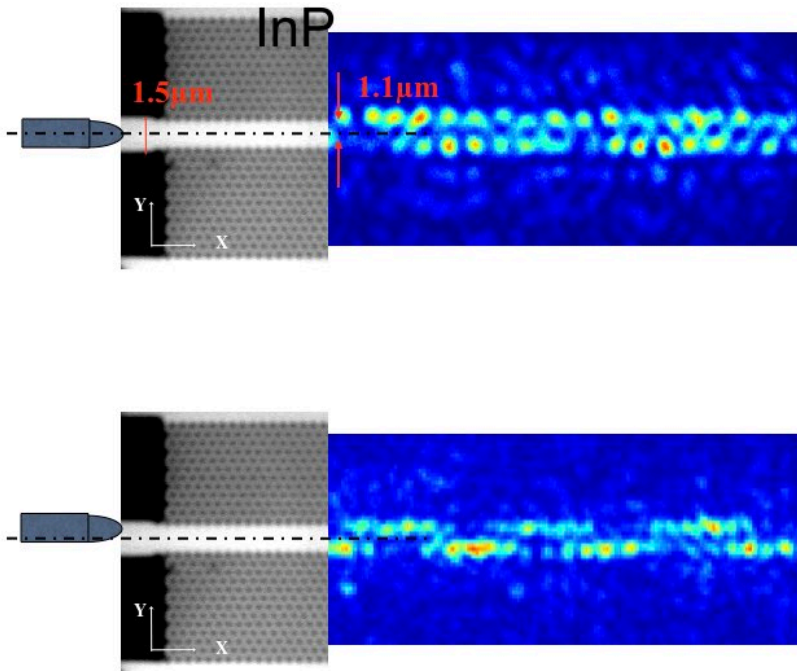
Misinterpretation



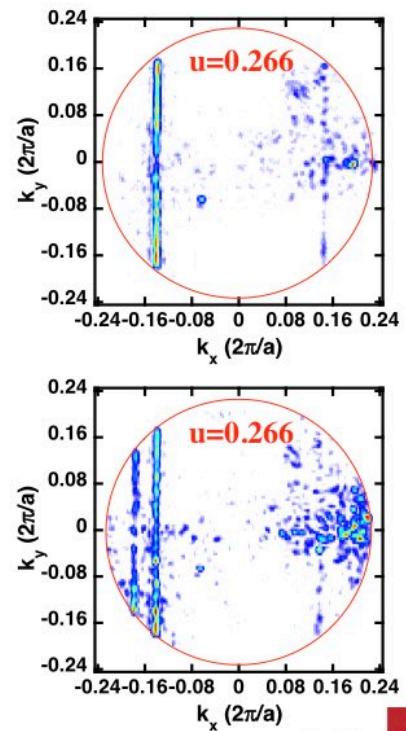
- The fringes are *not* an image of the Bloch mode.
- They originate from the interference between the forward and backward propagating mode, which are different modes at $+k+mG$ and $-k+mG$

Imaging of W3 PhC waveguide

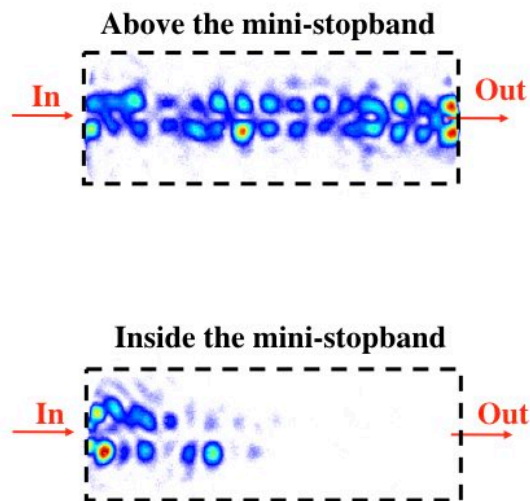
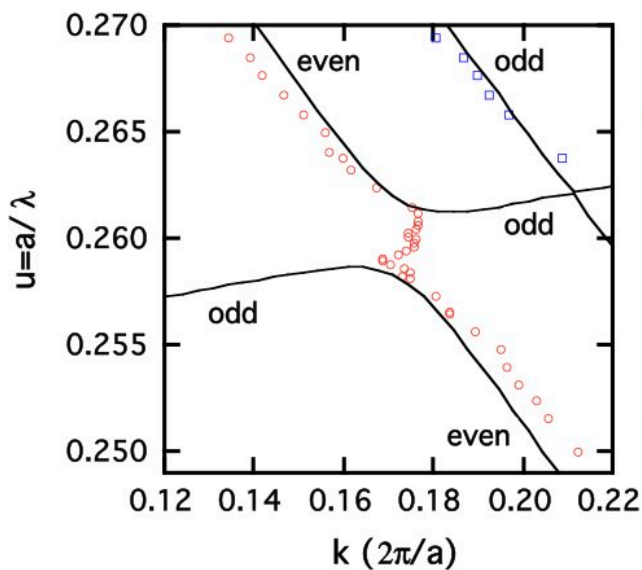
Real space



Fourier space



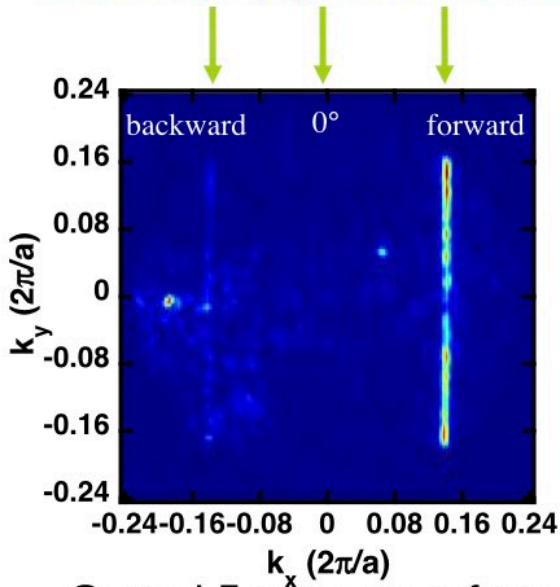
Experimental dispersion curves of a W3 PhC waveguide



Optical and numerical FFT

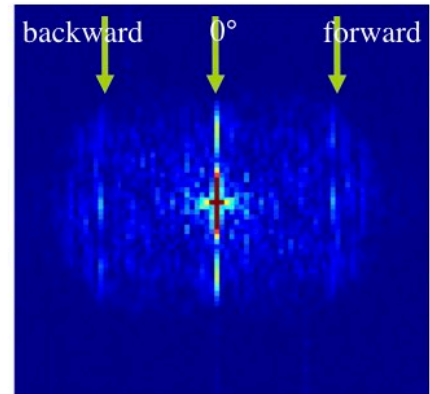
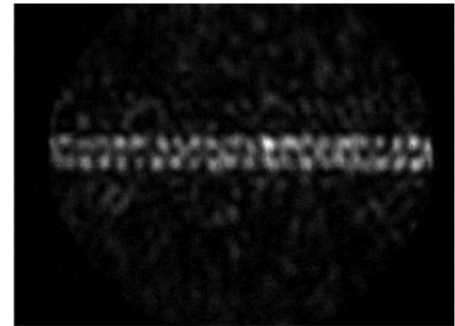


Because the phase information is still present during the formation of the Fourier image, there is no DC component and forward and backward propagation can be distinguished.



Optical Fourier transform

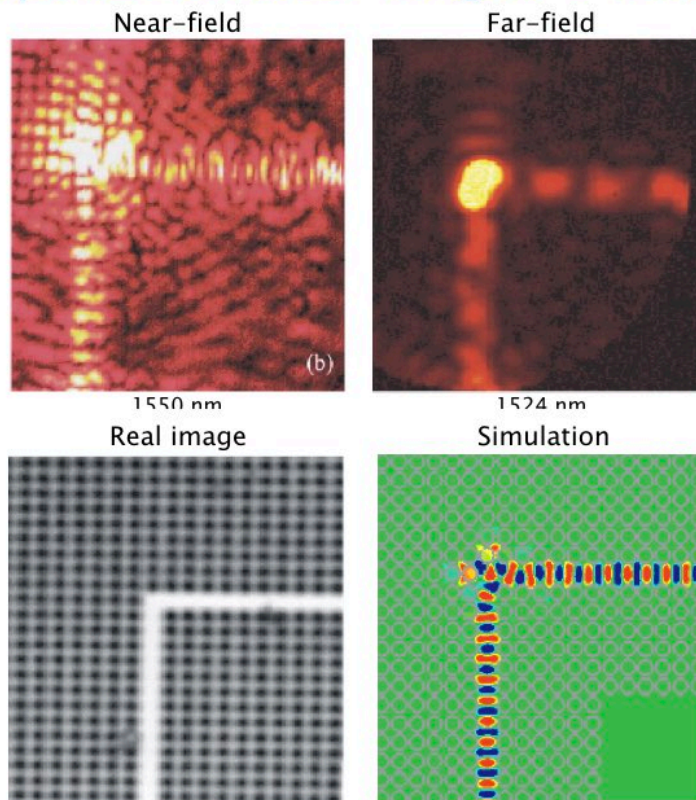
Ecole doctorale photonique, Photonic crystals, PHYS-605, Romuald Houdré, Summer semester 2017



Numerical 2D-FFT

89 / 109 EPFL ÉCOLE POLYTECHNIQUE FÉDÉRALE DE LAUSANNE

Comparison SNOM high NA imaging

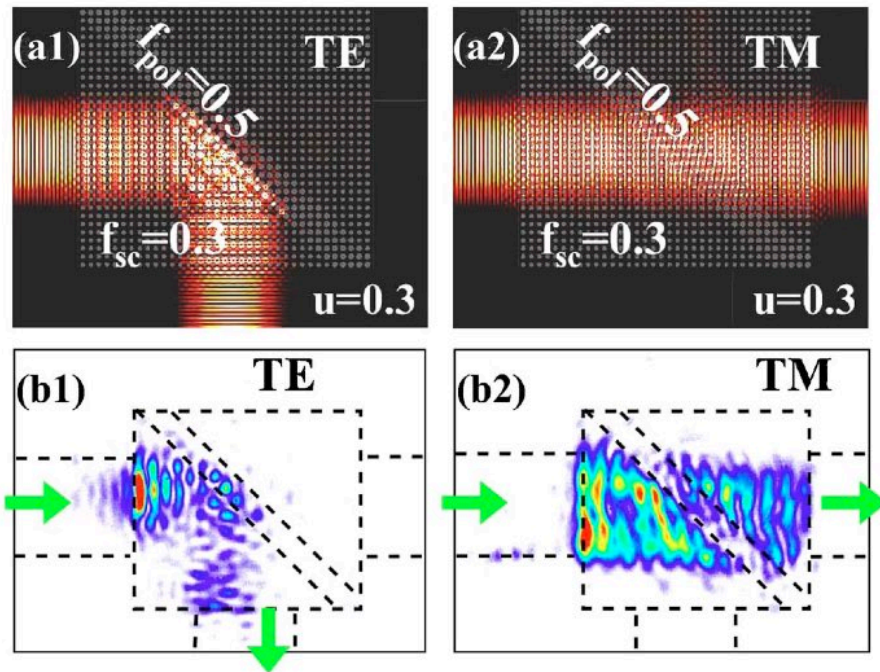


Courtesy I. Märki, Uni Neuchâtel

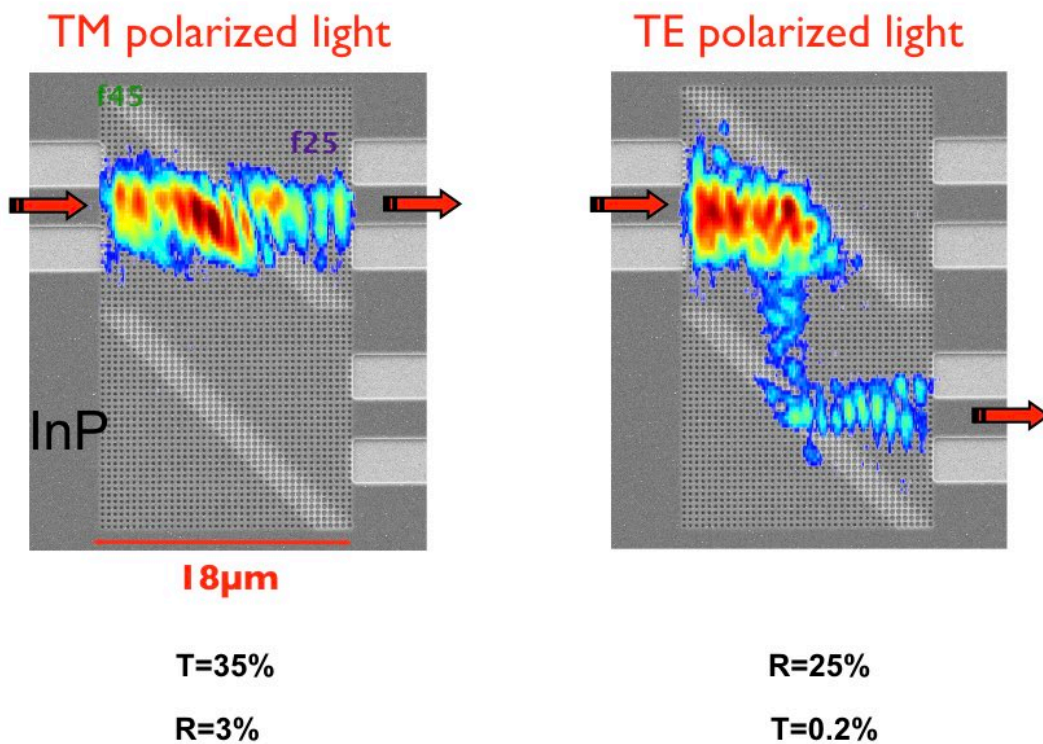
Ecole doctorale photonique, Photonic crystals, PHYS-605, Romuald Houdré, Summer semester 2017

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In-situ characterization of a polarization splitter

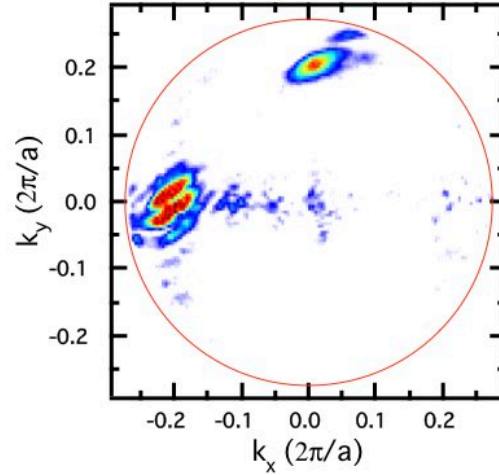
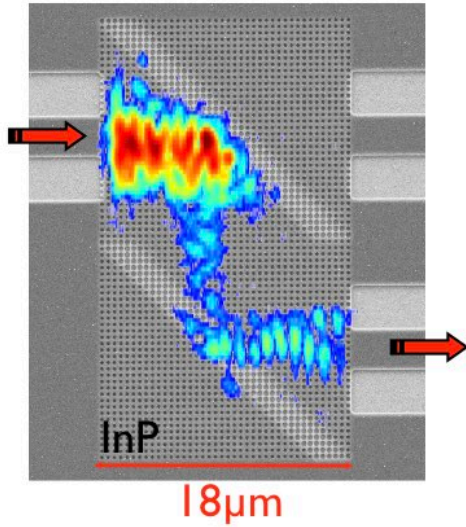


In-situ characterization of a polarization splitter



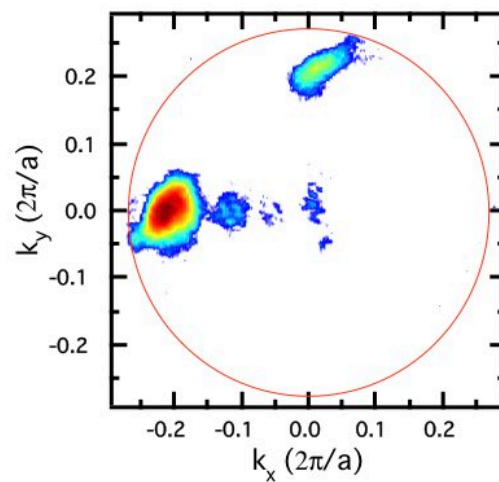
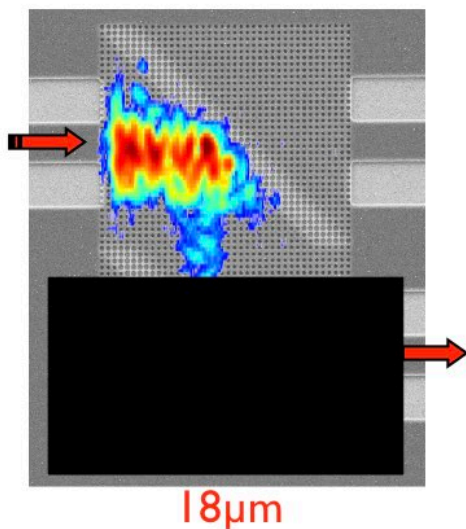
In-situ characterization of a polarization splitter

TE polarized light

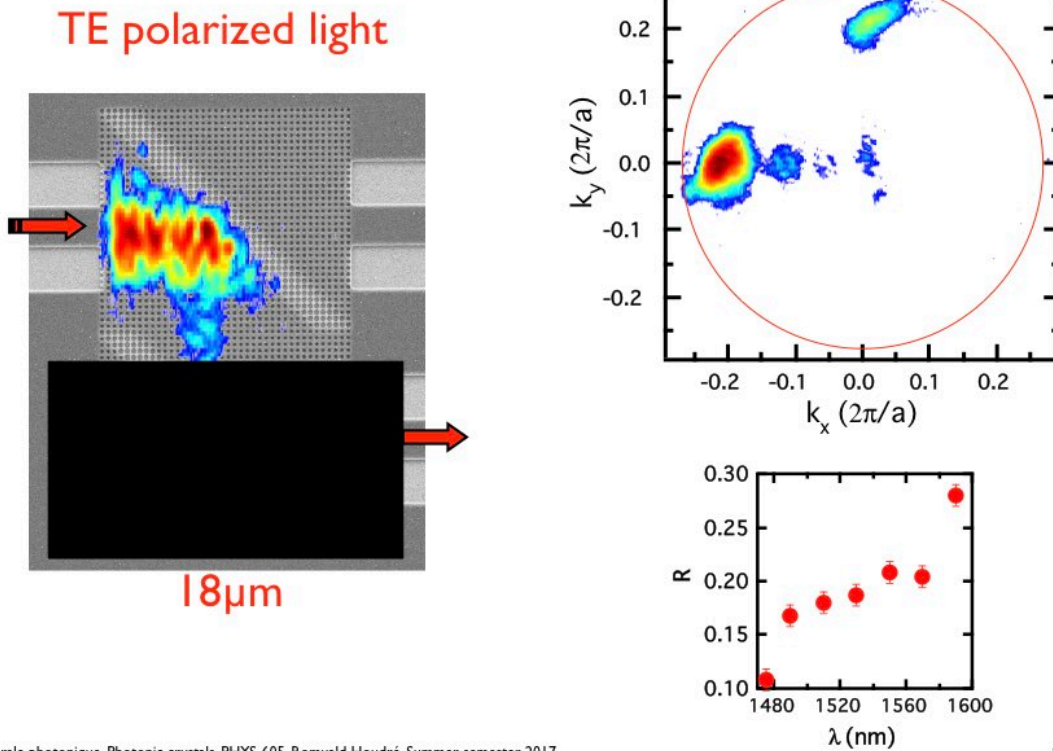


Fourier space imaging with filtering in real space

TE polarized light



Fourier space imaging with filtering in real space



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but ...

Problem: most of the interesting structures work below the light line

How to go beyond the light cone limit or how to convert evanescent waves into propagating waves for imaging ?

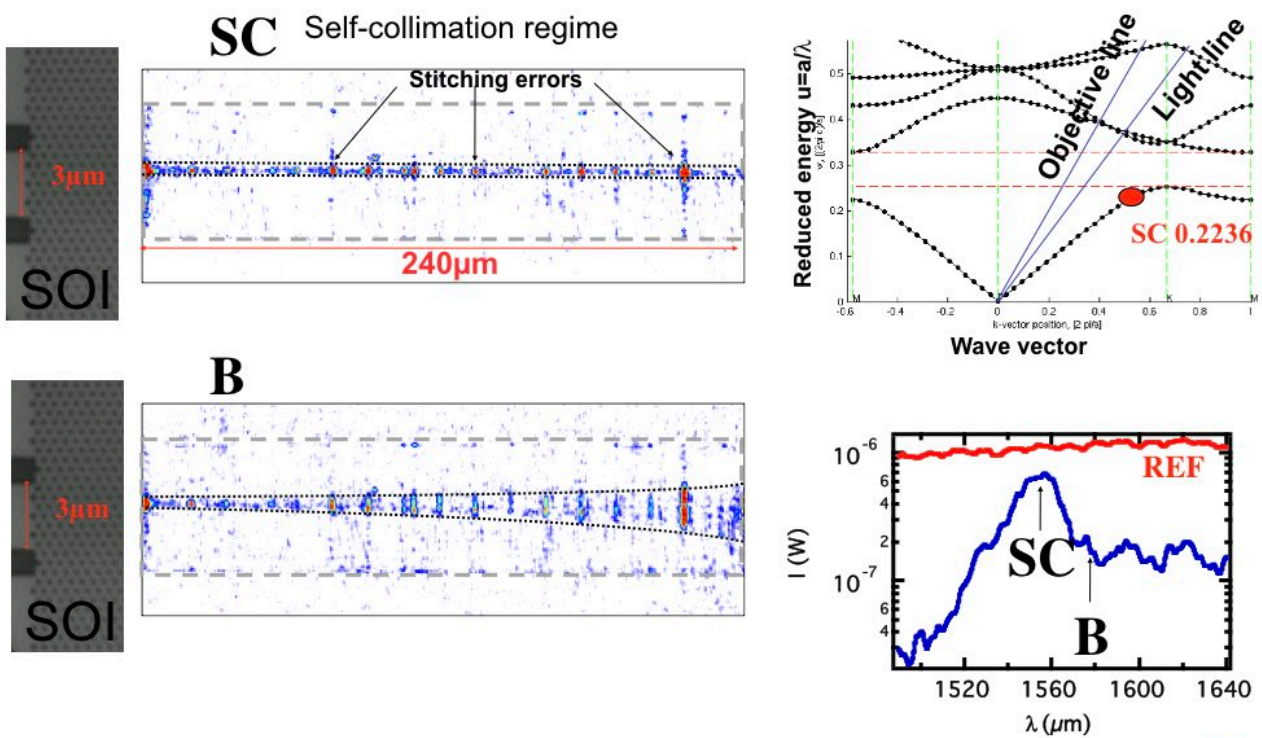
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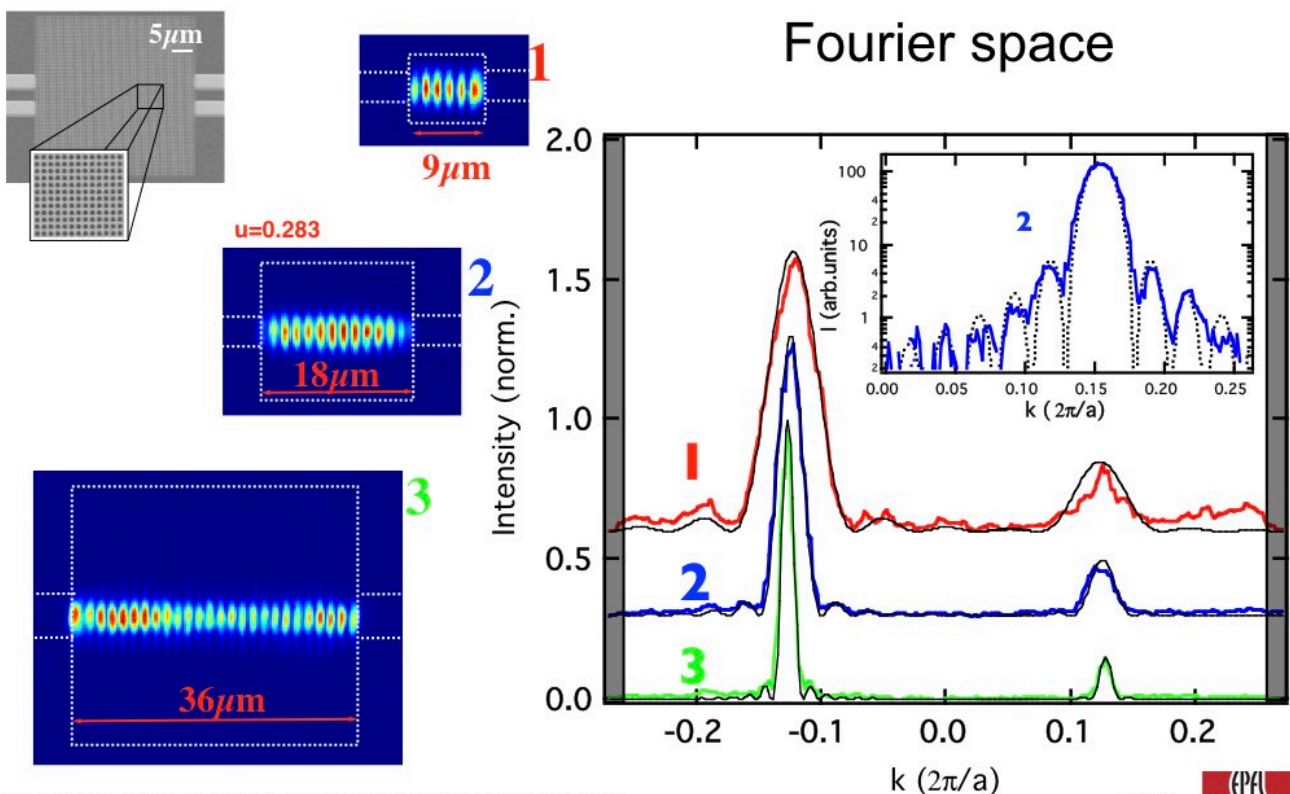
I Make use of fabrication imperfections

Imaging of Bloch wave propagating below the light cone

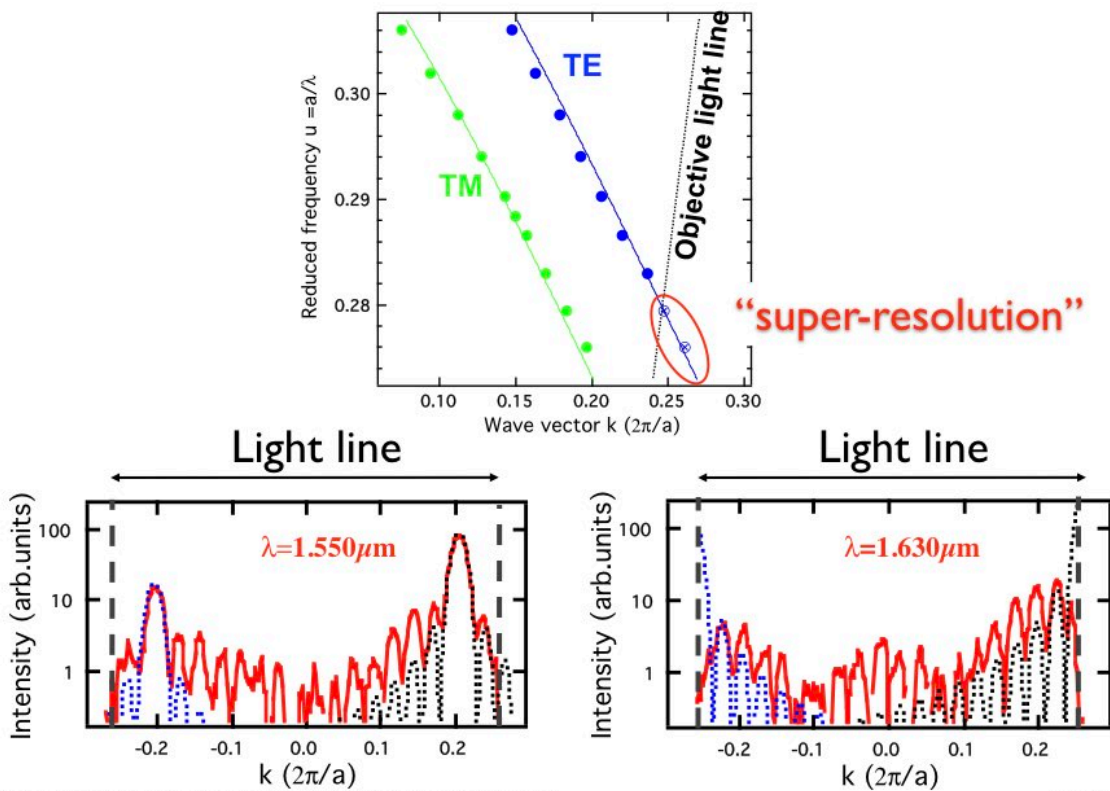


2 Make use of finite size effects

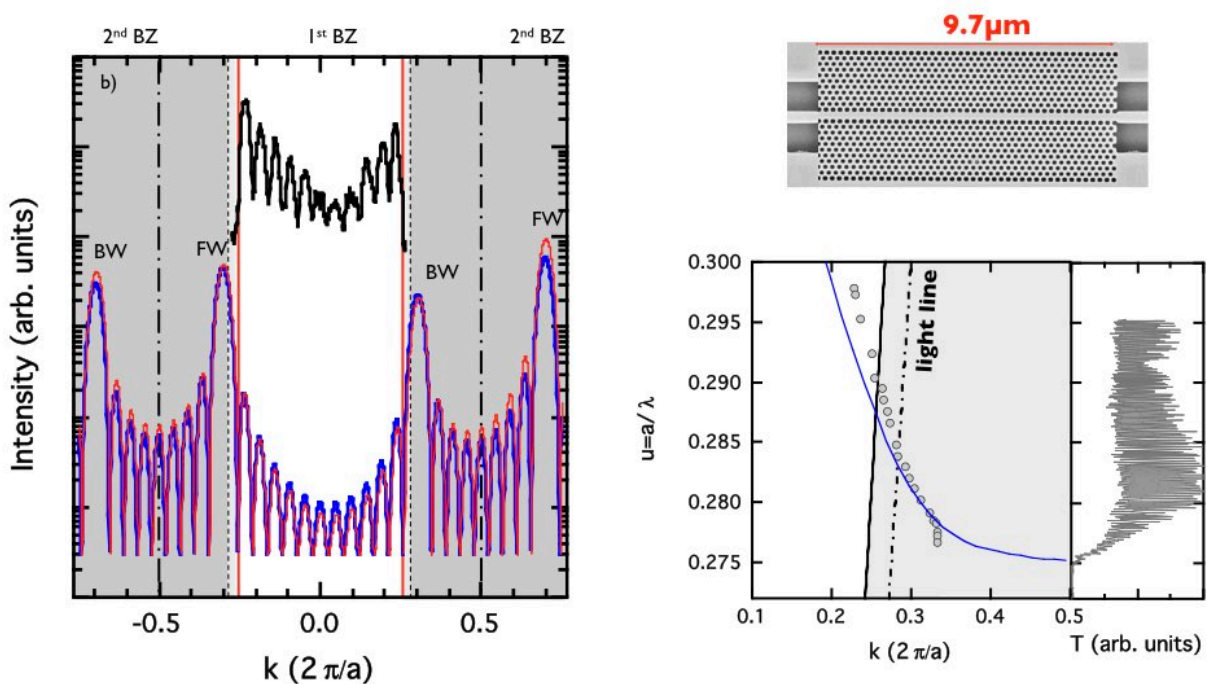
Dispersion curves and super-resolution: Size effect



Dispersion curves and super-resolution: Size effect



Dispersion curves and super-resolution: Size effect and analytical prolongation

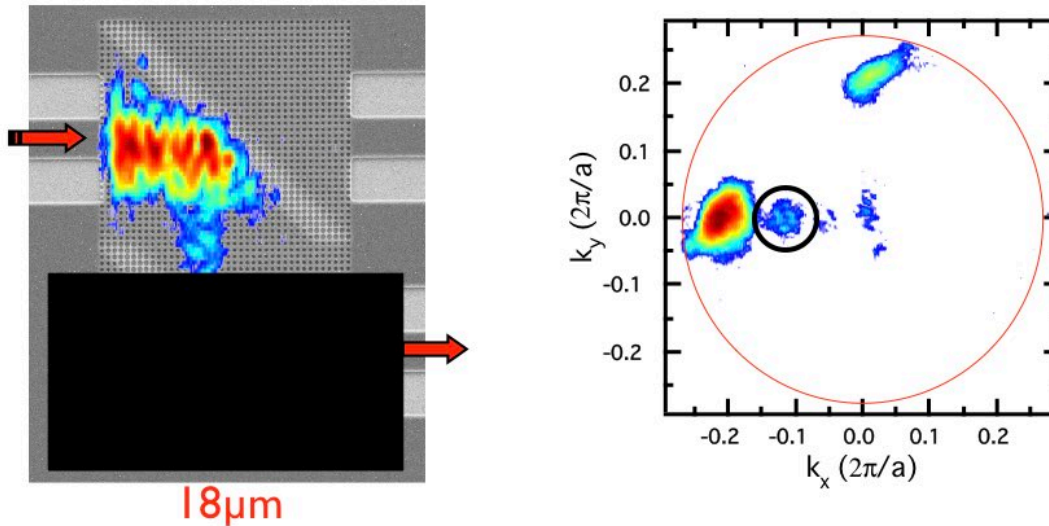


Effective NA = 2.5

Fourier space imaging with filtering in real space

Characterisation below the light cone

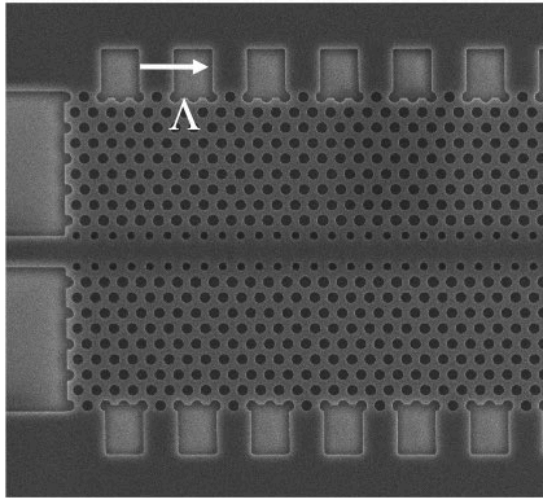
TE polarized light



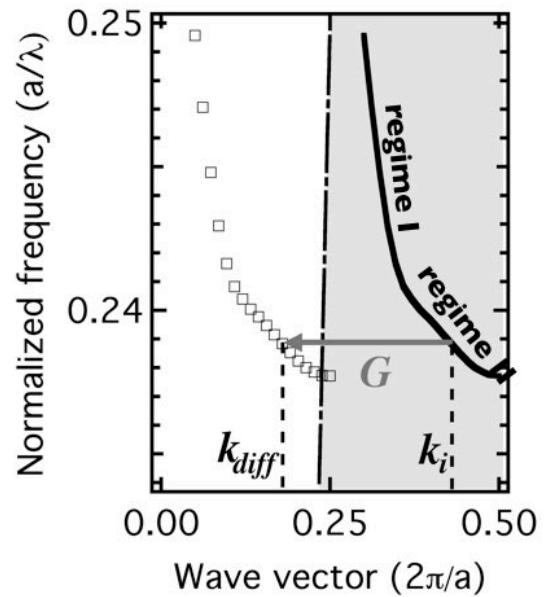
3 Fold back the band structure into the light cone with an extra periodicity

just a small amount to enable measurement

Imaging of dispersion curve below the light cone

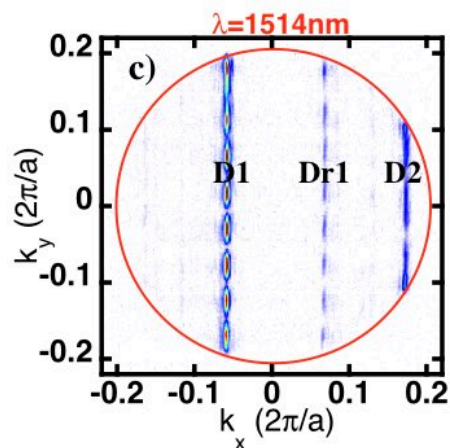
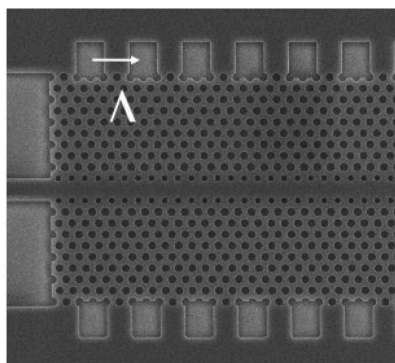
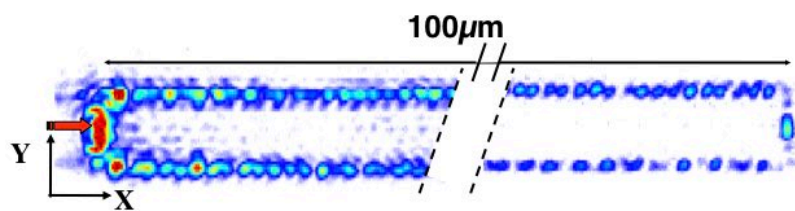


$$G = \frac{2\pi}{\Lambda}$$



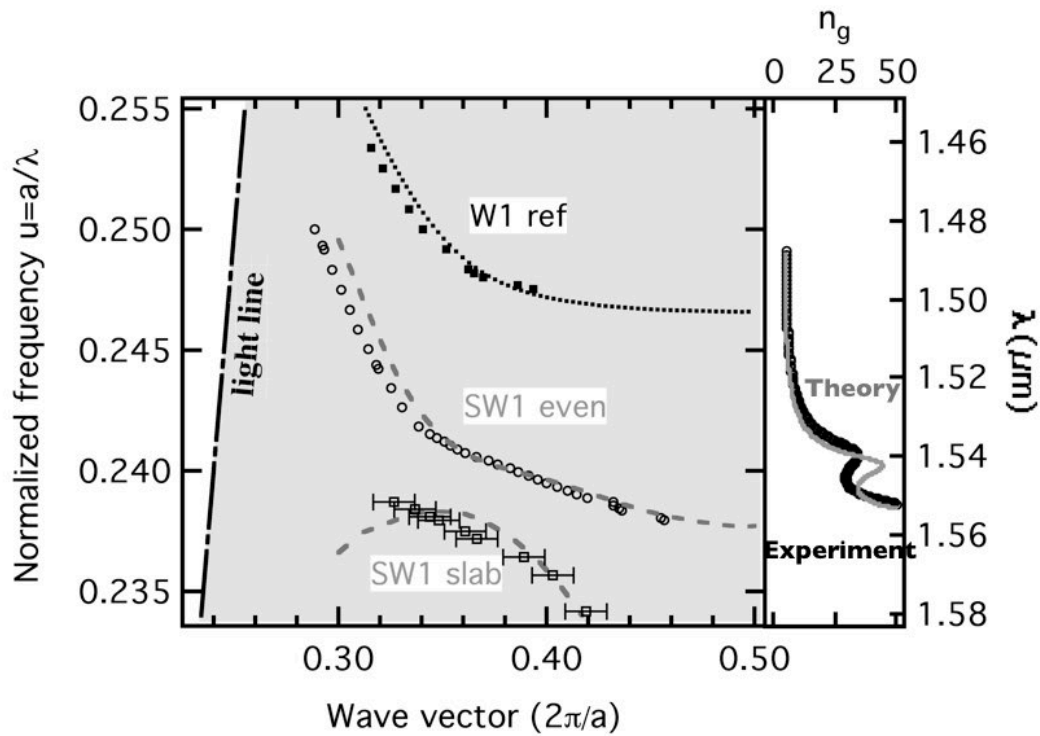
N. Le Thomas et al., Phys. Rev. B 76, 035103 (2007)
Ecole doctorale photonique, Photonic crystals, PHYS-605, Romuald Houdré, Summer semester 2017

Imaging of dispersion curve below the light cone



N. Le Thomas et al., Phys. Rev. B 76, 035103 (2007)
Ecole doctorale photonique, Photonic crystals, PHYS-605, Romuald Houdré, Summer semester 2017

Imaging of dispersion curve below the light cone



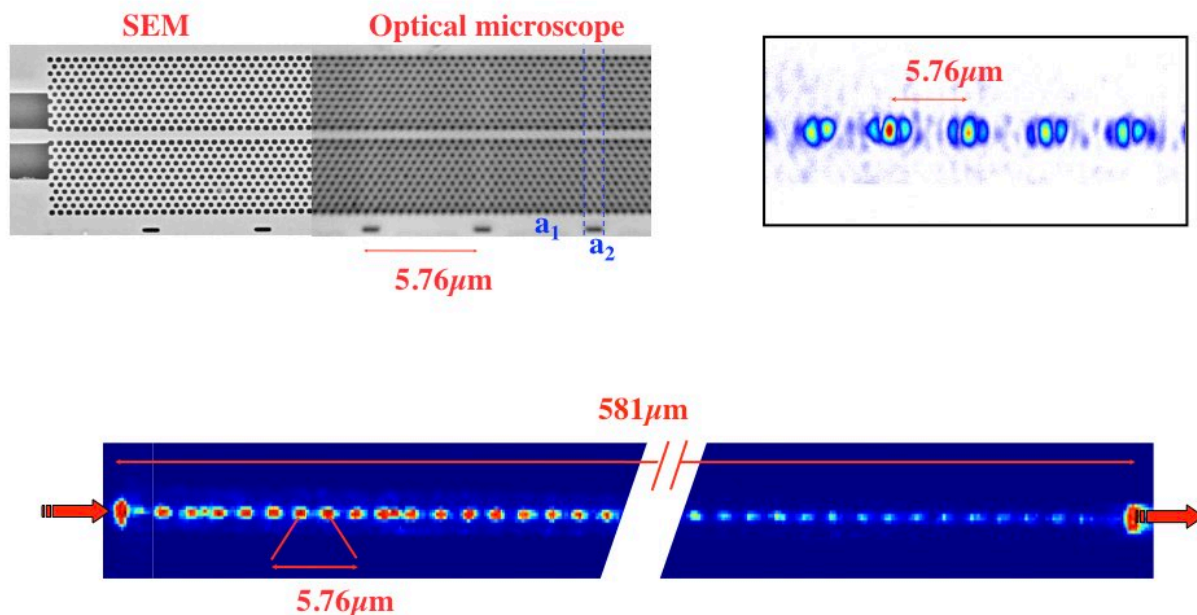
N. Le Thomas et al., Phys. Rev. B 76, 035103 (2007)

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Imaging of Coupled Cavities based Waveguides



Imaging of Coupled Cavities based Waveguides

