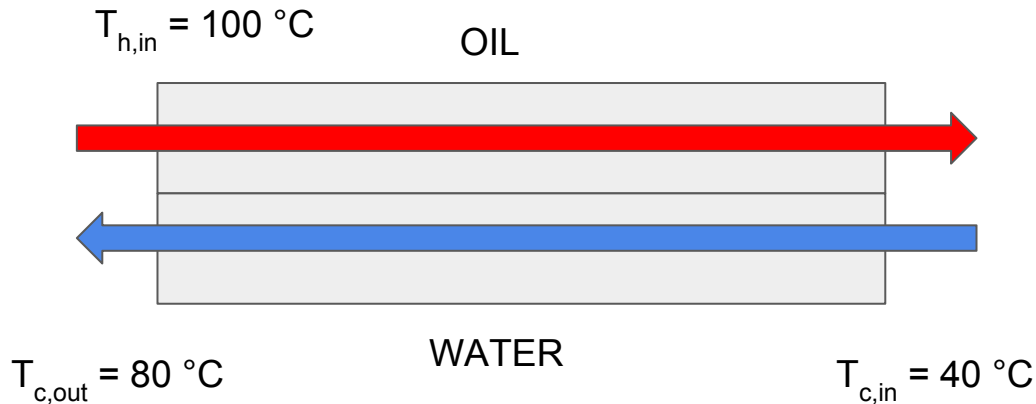


3.5

A cross-flow heat exchanger with both fluids unmixed is used to heat water ($c_p = 4.18$ kJ/kg·K) from 40°C to 80°C , flowing at the rate of 1.0 kg/s. What is the overall heat transfer coefficient if hot engine oil ($c_p = 1.9$ kJ/kg·K), flowing at the rate of 2.6 kg/s, enters at 100°C ? The heat transfer area is 20 m². (Note that you can use either an effectiveness or an LMTD method. It would be wise to use both as a check.)



Oil

$$T_{h,in} = 100^\circ\text{C}$$

$$c_{p,h} = 1.9 \text{ kJ/kgK}$$

$$m_h = 2.6 \text{ kg/s}$$

Water

$$T_{c,in} = 40^\circ\text{C}; T_{c,out} = 80^\circ\text{C}$$

$$c_{p,h} = 4.18 \text{ kJ/kgK}$$

$$m_h = 1.0 \text{ kg/s}$$

1. Energy Balance

$$Q_{\text{cold}} = m_c \cdot c_{p,c} \cdot \Delta T_c = 167200 \text{ W}$$

$$Q_{\text{hot}} = Q_{\text{cold}}$$

$$Q_{\text{hot}} = m_h \cdot c_{p,h} \cdot \Delta T_h$$

$$T_{h,\text{out}} = T_{h,\text{in}} - Q_{\text{hot}} / m_h \cdot c_{p,h} = 66.15 \text{ }^\circ\text{C}$$

2. Effectiveness method

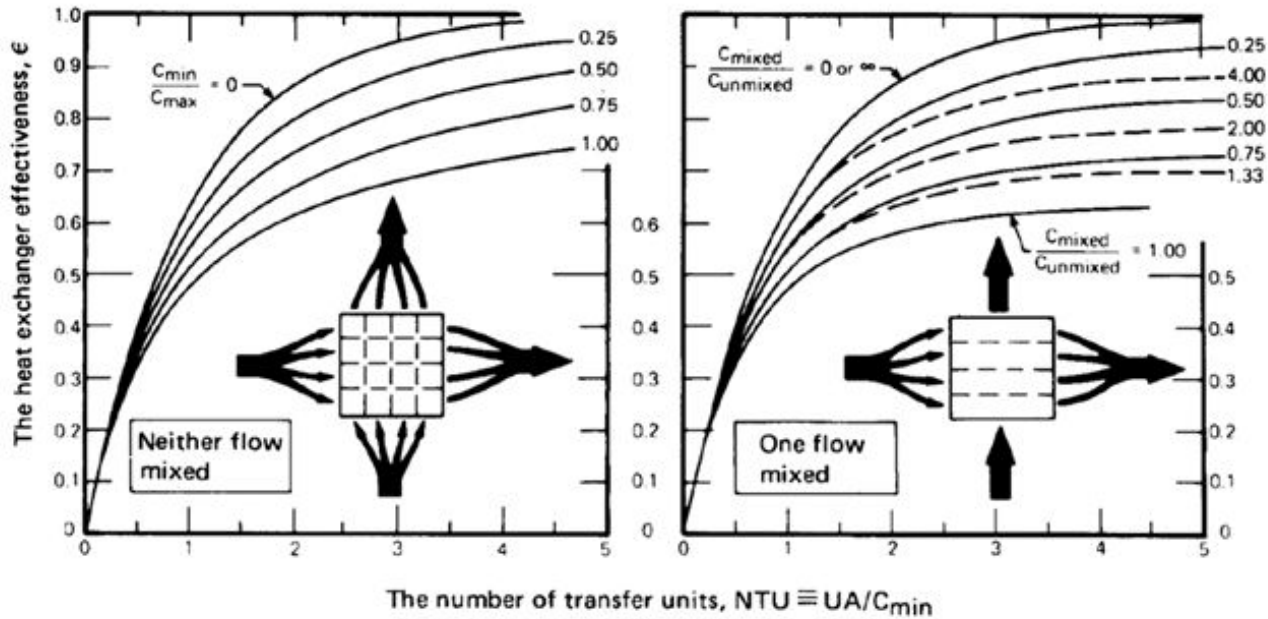
$$\varepsilon \equiv \frac{C_h (T_{h,\text{in}} - T_{h,\text{out}})}{C_{\text{min}} (T_{h,\text{in}} - T_{c,\text{in}})} = \frac{C_c (T_{c,\text{out}} - T_{c,\text{in}})}{C_{\text{min}} (T_{h,\text{in}} - T_{c,\text{in}})}$$

$$\varepsilon = f(C_{\text{min}}/C_{\text{max}}, \text{NTU}) = 0.67$$

$$C_c = m_c \cdot c_{p,c} = 4180 \text{ W/K} = C_{\text{min}}$$

$$C_h = m_h \cdot c_{p,h} = 4940 \text{ W/K} = C_{\text{max}}$$

$$C_{\text{min}}/C_{\text{max}} = 0.85$$



a.) Cross-flow exchanger, neither fluid mixed

b.) Cross-flow exchanger, one fluid mixed

$$NTU = UA/C_{min} = 2.2$$

$$U = C_{min} \cdot NTU/A = 460 \text{ W/m}^2\text{K}$$

3. LMTD method

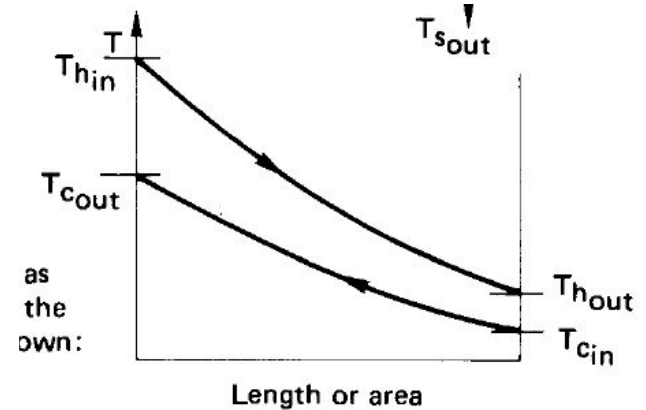
$$Q = UA(\text{LMTD}) \cdot F \left(\underbrace{\frac{T_{t_{\text{out}}} - T_{t_{\text{in}}}}{T_{s_{\text{in}}} - T_{t_{\text{in}}}}}_P, \underbrace{\frac{T_{s_{\text{in}}} - T_{s_{\text{out}}}}{T_{t_{\text{out}}} - T_{t_{\text{in}}}}}_R \right) \quad (3.14)$$

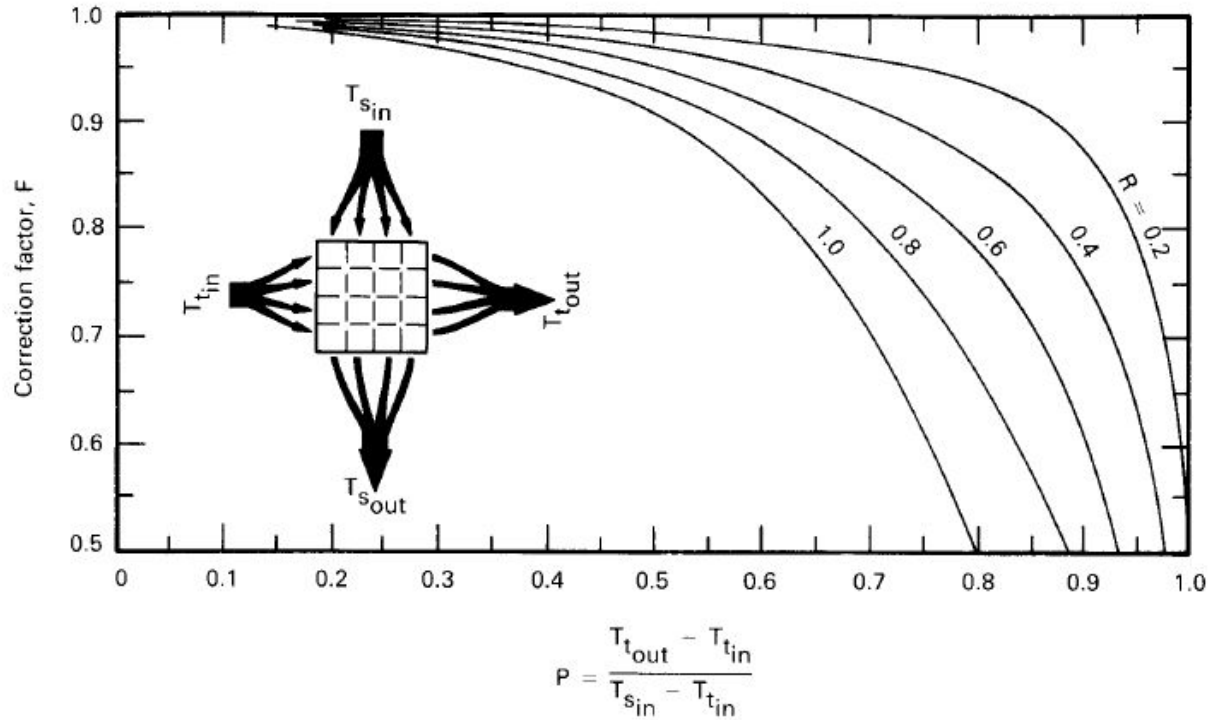
The factor F is defined in such a way that *the LMTD should always be calculated for the equivalent counterflow single-pass exchanger with the same hot and cold temperatures*. This is explained in Fig. 3.13.

$$F(P, R) = F(PR, 1/R) \quad (3.15)$$

Thus, if R is greater than one, we need only evaluate F using PR in place of P and $1/R$ in place of R .

$$\text{LMTC} = \frac{(T_{h_{\text{in}}} - T_{c_{\text{out}}}) - (T_{h_{\text{out}}} - T_{c_{\text{in}}})}{\ln \frac{T_{h_{\text{in}}} - T_{c_{\text{out}}}}{T_{h_{\text{out}}} - T_{c_{\text{in}}}}}$$





$P = 0.67$



$F = 0.80$

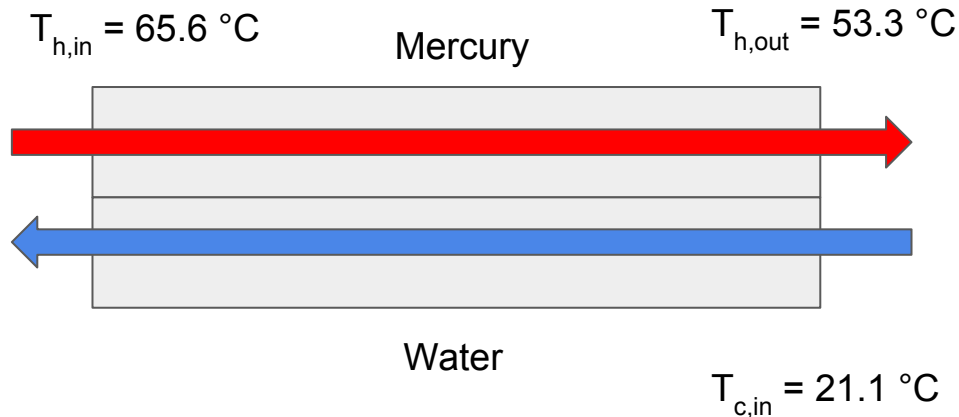


$U = 455 \text{ W/m}^2\text{K}$

$R = 0.85$

3.7

Consider a counterflow heat exchanger that must cool 3000 kg/h of mercury from 150°F to 128°F. The coolant is 100 kg/h of water, supplied at 70°F. If U is 300 W/m²K, complete the design by determining reasonable value for the area and the exit-water temperature.
 [A = 0.147 m².]



Mercury

$$T_{h,in} = 65.6 \text{ }^{\circ}\text{C}; T_{h,out} = 53.3 \text{ }^{\circ}\text{C}$$

$$c_{p,h} = 139,4 \text{ J/kgK}$$

$$m_h = 0.83 \text{ kg/s}$$

Water

$$T_{c,in} = 21.1 \text{ }^{\circ}\text{C}$$

$$c_{p,h} = 4.18 \text{ kJ/kgK}$$

$$m_h = 0.028 \text{ kg/s}$$

1. Energy Balance

$$Q_{\text{hot}} = m_h \cdot c_{p,h} \cdot \Delta T_h = 1415 \text{ W}$$

$$Q_{\text{hot}} = Q_{\text{cold}}$$

$$Q_{\text{cold}} = m_c \cdot c_{p,c} \cdot \Delta T_c$$

$$T_{c,\text{in}} = T_{c,\text{out}} + Q_{\text{cold}} / m_c \cdot c_{p,c} = 33.2 \text{ }^\circ\text{C}$$

2. LMTD method

$$Q = UA(\text{LMTD}) \cdot F$$

$$F = 1$$

(it is a perfectly countercurrent arrangement)

$$\text{LMTD} = 32.6 \text{ K}$$

$$A = 0.145 \text{ m}^2$$

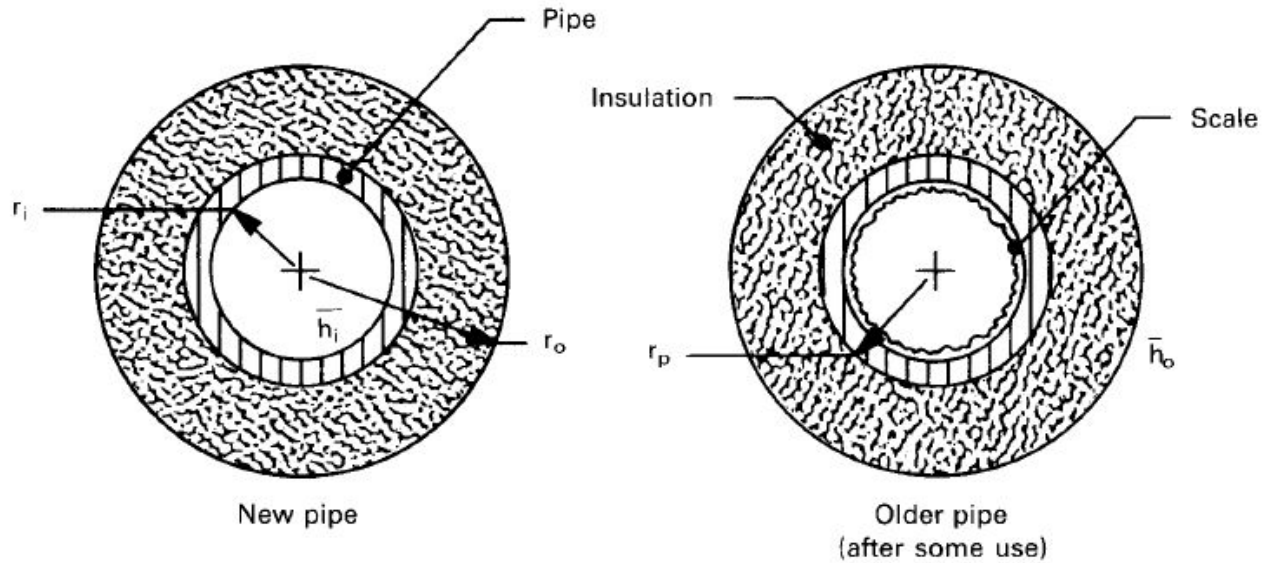


Figure 2.21 The fouling of a pipe.

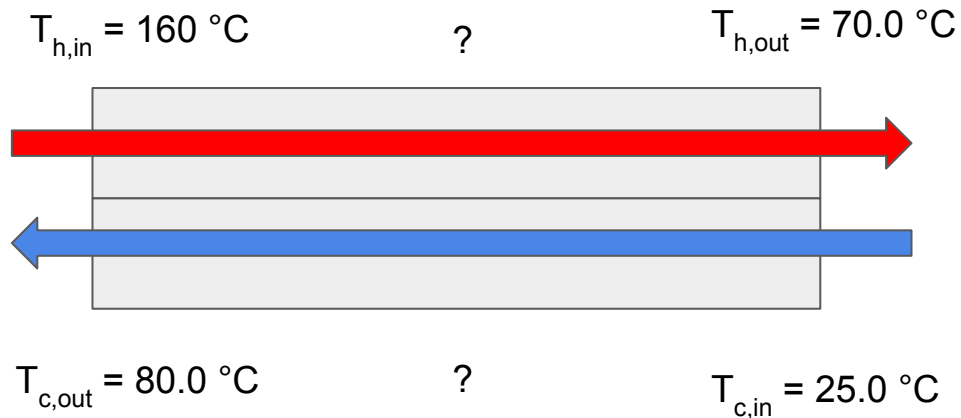
$$U_{\text{design}}^{-1} = \sum R_i$$

$$U_{\text{fouling}}^{-1} = \sum R_i + R_{\text{fouling}}$$

$$R_{\text{fouling}} = U_{\text{fouling}}^{-1} - U_{\text{design}}^{-1}$$

3.16

A particular cross-flow process heat exchanger operates with the fluid mixed on one side only. When it is new, $U = 2000 \text{ W/m}^2\text{K}$, $T_{c,in} = 25^\circ\text{C}$, $T_{c,out} = 80^\circ\text{C}$, $T_{h,in} = 160^\circ\text{C}$, and $T_{h,out} = 70^\circ\text{C}$. After 6 months of operation, the plant manager reports that the hot fluid is only being cooled to 90°C and that he is suffering a 30% reduction in total heat transfer. What is the fouling resistance after 6 months of use? (Assume no reduction of cold-side flow rate by fouling.)



Fouling condition

$$Q_{\text{fouling}} = 0.7 Q_{\text{design}}$$

$$T_{h,out,\text{fouling}} = 90^\circ\text{C}$$

1. Energy Balance

$$Q_{\text{fouling}} = 0.7 Q_{\text{design}}$$

$$mc_p(T_{\text{c,out,fouling}} - T_{\text{c,in}}) = 0.7mc_p(T_{\text{c,out}} - T_{\text{c,in}})$$

$$T_{\text{c,out,fouling}} = 0.7T_{\text{c,out}} + 0.3T_{\text{c,in}} = 63.5 \text{ }^\circ\text{C}$$

2. LMTD

$$\text{LMTD}_{\text{design}} = 60.8 \text{ K}$$

$$\text{LMTD}_{\text{fouling}} = 79.7 \text{ K}$$

3. Correction factors

$$P_{\text{design}} = 0.67$$

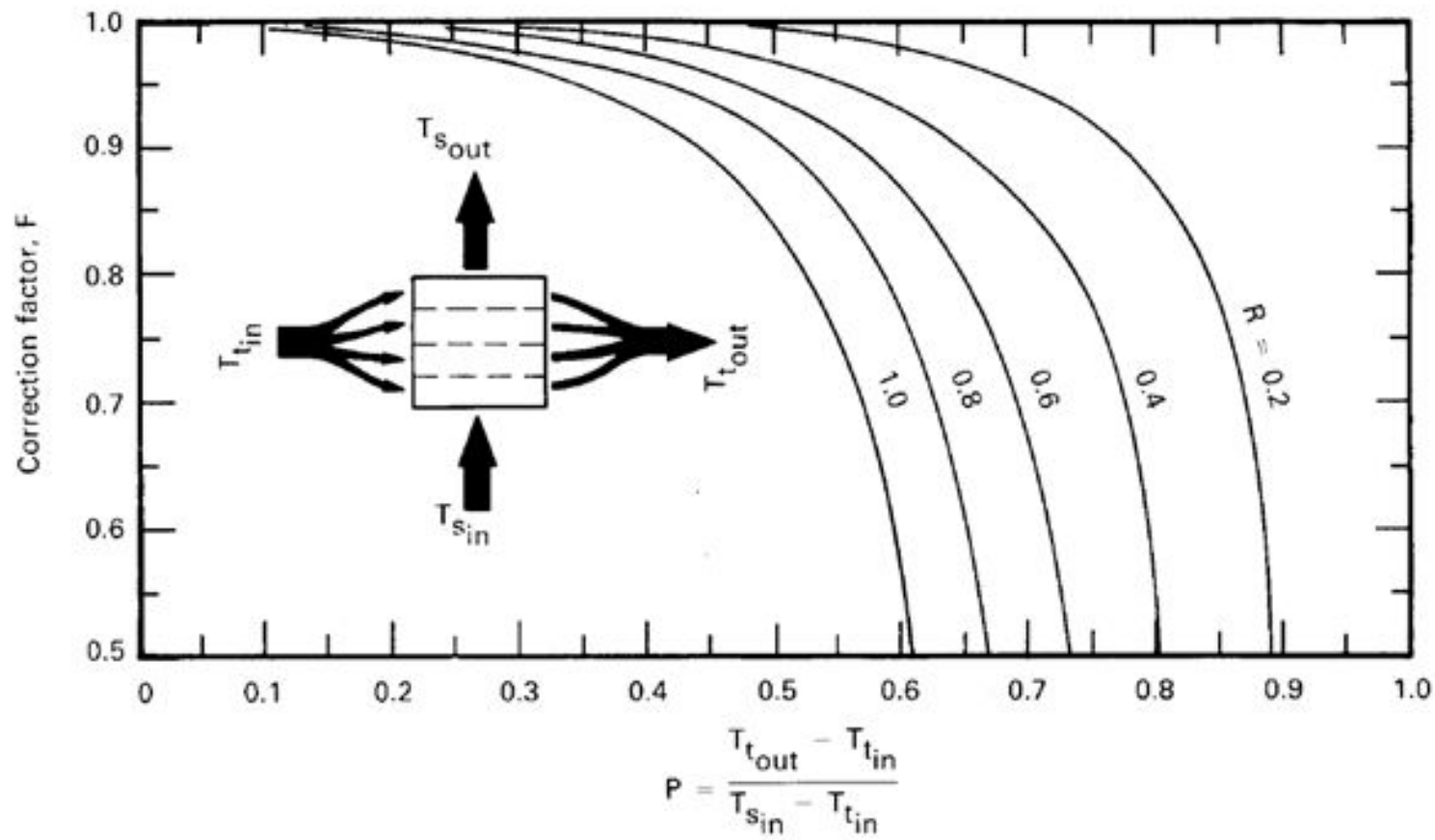
$$R_{\text{design}} = 0.61$$

$$F_{\text{design}} = 0.80$$

$$P_{\text{fouling}} = 0.52$$

$$R_{\text{fouling}} = 0.55$$

$$F_{\text{fouling}} = 0.95$$



4. Energy Balance + LMTD

$$Q_{\text{fouling}} = 0.7 Q_{\text{design}}$$

$$U_{\text{fouling}} A \text{LMTD}_{\text{fouling}} F_{\text{fouling}} = 0.7 U_{\text{design}} A \text{LMTD}_{\text{design}} F_{\text{design}}$$

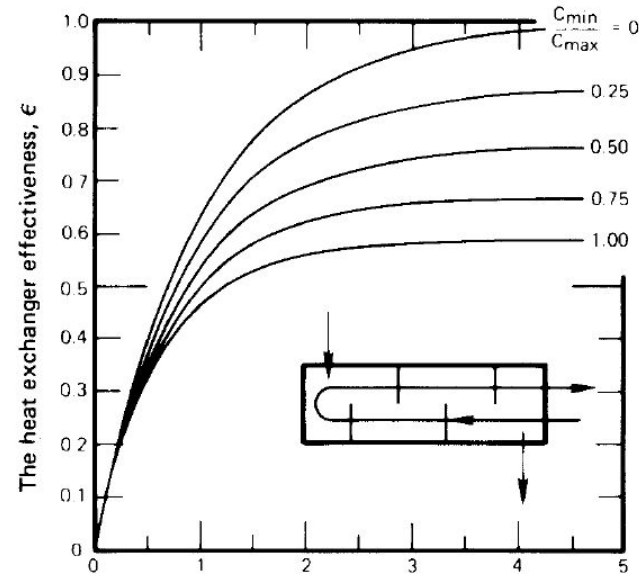
$$U_{\text{fouling}} = 0.7 U_{\text{design}} \text{LMTD}_{\text{design}} / \text{LMTD}_{\text{fouling}} F_{\text{design}} / F_{\text{fouling}} = 899 \text{ W/m}^2\text{K}$$

5. Fouling resistance

$$R_{\text{fouling}} = U_{\text{fouling}}^{-1} - U_{\text{design}}^{-1} = 6.1235\text{e-}04 \text{ m}^2\text{K/W}$$

- 3.39 Calculate the area required in a two-tube-pass, one-shell-pass condenser that is to condense 10^6 kg/h of steam at 40°C using water at 17°C . Assume that $U = 4700$ W/m²K, the maximum allowable temperature rise of the water is 10°C , and $h_{fg} = 2406$ kJ/kg. [$A = 8,112$ m²]

Water	
$T_{c,in}$	$= 17^\circ\text{C}$
$T_{c,out}$	$= 27^\circ\text{C}$
$c_{p,h}$	$= 4.18$ kJ/kgK
Steam	
$T_{h,in} = T_{h,out}$	$= 40^\circ\text{C}$
h_{lv}	$= 2406$ kJ/kg



1. Energy Balance

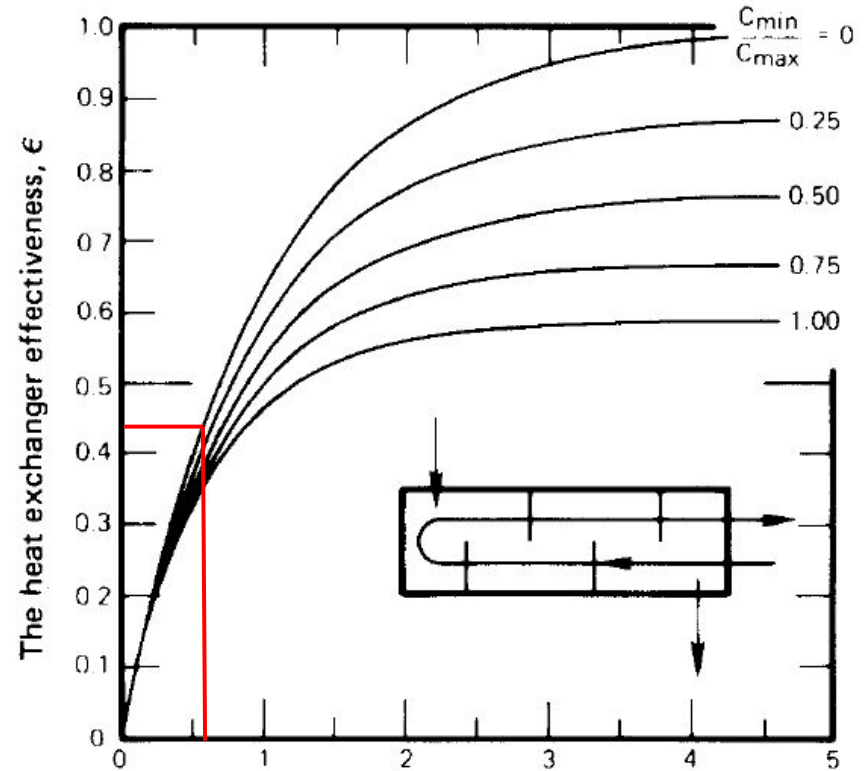
$$Q = m_{\text{steam}} h_{\text{lv}} = 6.6833\text{e}+05 \text{ kW}$$

$$m_{\text{water}} = Q / (c_p \Delta T)_{\text{water}} = 1.5989\text{e}+04 \text{ kg/s}$$

$$\varepsilon \equiv \frac{C_h (T_{h_{\text{in}}} - T_{h_{\text{out}}})}{C_{\text{min}} (T_{h_{\text{in}}} - T_{c_{\text{in}}})} = \frac{C_c (T_{c_{\text{out}}} - T_{c_{\text{in}}})}{C_{\text{min}} (T_{h_{\text{in}}} - T_{c_{\text{in}}})}$$

2. Effectiveness

$$\varepsilon = \Delta T_{\text{water}} / \Delta T_{\text{max}} = 0.43478$$



$$NTU = UA/C_{\text{min}} = 0.57$$

$$A = C_{\text{min}} \cdot NTU/U = 8105.4 \text{ m}^2$$