

A flat, very long panel is composed of two layers: a thin film ($k_{\text{film}} = 0.025 \text{ W/mK}$, thickness = 0.25 mm) and a substrate ($k_{\text{substrate}} = 0.05 \text{ W/mK}$, thickness = 1 mm). A heat flux q (W/m^2) is applied to the back of the substrate, while the film is subject to cooling by a forced convection air flow. The back of the substrate is maintained at $T_1 = 90 \text{ }^\circ\text{C}$ while the free surface of the film is exposed to air at $T_{\text{air}} = 20 \text{ }^\circ\text{C}$ and an average, unknown convection heat transfer coefficient h ($\text{W/m}^2\text{K}$). Also, it is required that the temperature T_2 between the film and the substrate must be equal to $60 \text{ }^\circ\text{C}$. Determine the heat flux q to be applied to the substrate and the convection heat transfer coefficient of the air flow.

Heat Flux q , Fourier's Law applied to the substrate

$$q = k_{\text{substrate}}/t_{\text{substrate}} * (T_1 - T_2) = 1500 \text{ W/m}^2$$

Temperature T_3 of the free surface of the thin film cooled by the forced convection air flow

$$q = k_{\text{film}}/t_{\text{film}} * (T_2 - T_3)$$

$$T_3 = T_2 - q * t_{\text{film}} / k_{\text{film}} = 45 \text{ }^\circ\text{C}$$

Convection heat transfer coefficient

$$q = h * (T_3 - T_{\text{air}})$$

$$h = q / (T_3 - T_{\text{air}}) = 60 \text{ W/m}^2\text{K}$$

A shell-and-tube exchanger (two shells, four tube passes) is used to cool down 100 kg/h of pressurized water from 87 to 47 °C with 200 kg/h of methyl alcohol (methanol, $c_{p_{\text{methanol}}}=2672$ J/kgK) entering the exchanger at 27 °C. If the overall heat transfer coefficient is 300 W/m²K, determine the outlet temperature of the methanol and the required heat exchanger area.

Mass flow rates and specific heats

$$m_{\text{water}}=0.0278 \text{ kg/s}$$

$$c_{p_{\text{water}}}=4189 \text{ J/kgK}$$

$$m_{\text{methanol}}=0.0556 \text{ kg/s}$$

$$c_{p_{\text{methanol}}}=2672 \text{ J/kgK}$$

Energy balance on the water side

$$Q = m_{\text{water}} * c_{p_{\text{water}}} * (T_{\text{water,in}} - T_{\text{water,out}}) = 4.6544e+3 \text{ W}$$

Energy Balance on the methanol side

$$Q = m_{\text{methanol}} * c_{p_{\text{methanol}}} * (T_{\text{methanol,out}} - T_{\text{methanol,in}})$$

$$T_{\text{methanol,out}} = T_{\text{methanol,in}} + Q / (m_{\text{methanol}} * c_{p_{\text{methanol}}}) = 58.4 \text{ °C}$$

Heat Capacities

$$C_{\text{water}} = 116.36 \text{ W/K} = C_{\text{min}}$$

$$C_{\text{methanol}} = 148.4 \text{ W/K} = C_{\text{max}}$$

$$C_{\text{min}} / C_{\text{max}} = 0.78$$

Effectiveness

$$\epsilon = (T_{\text{water,in}} - T_{\text{water,out}}) / (T_{\text{water,in}} - T_{\text{methanol,in}}) = 0.667$$

NTU

$$NTU = UA / C_{\text{min}} = 1.8$$

$$A = NTU * C_{\text{min}} / U = 0.7 \text{ m}^2$$

Atmospheric air enters a 10-m-long, 150-mm-diameter uninsulated heating duct at 60 °C and 0.04 kg/s. The duct surface temperature is approximately constant at $T_{\text{wall}} = 15$ °C. What are the outlet air temperature, the heat rate q , and pressure drop p for these conditions?

Also, assuming that the tube wall is thin, an air flow at $T_{\text{out}} = 0$ °C flows over the whole tube with a velocity of 4 m/s. Determine the outer heat transfer coefficient and the overall heat transfer coefficient.

Thermophysical properties (internal flow, $T_{\text{film}} = 310$ K)

$\rho = 1.139$ kg/m³; $c_p = 1007$ J/kgK; $\nu = 1.659 \times 10^{-5}$ m²/s;
 $k = 0.02684$ W/mK; $Pr = 0.709$;

Reynolds number (internal flow)

$u = 4 \cdot m / (\pi \cdot D^2) / \rho = 1.99$ m/s;
 $Re = u \cdot D / \nu = 1.7968 \times 10^4$ (turbulent)

Friction factor and pressure drop (internal flow)

$f = (.79 \cdot \log(Re) - 1.64)^{-2} = 0.0269$;
 $D_p = f \cdot L / D \cdot \rho \cdot (u^2) / 2 = 4.03$ Pa;

Nusselt Number and heat transfer coefficient (internal flow)

$$Nu_D = \frac{(f/8) (Re_D - 1000) Pr}{1 + 12.7 \sqrt{f/8} (Pr^{2/3} - 1)}$$

for $2300 \leq Re_D \leq 5 \times 10^6$.

$Nu = 47.6$;
 $h = 8.52$ W/m²K;

Air outlet temperature (internal flow)

$$\frac{T_{b_{\text{out}}} - T_{b_{\text{in}}}}{T_w - T_{b_{\text{in}}}} = 1 - \exp\left(-\frac{\bar{h}PL}{\dot{m}c_p}\right)$$

$T_{\text{air_out}} = T_{\text{air_in}} + (T_{\text{wall}} - T_{\text{air_in}}) \cdot (1 - \exp(-h \cdot \pi \cdot D \cdot L / \dot{m} \cdot c_p)) = 31.6$ °C;

Heat rate

$Q = \dot{m} \cdot c_p \cdot (T_{\text{air_out}} - T_{\text{air_in}}) = -1.1435 \times 10^3$ W;

Thermophysical properties (external flow, $T_{\text{film}} = 280$ K)

$\rho = 1.261$ kg/m³; $\nu = 1.385 \times 10^{-5}$ m²/s; $k = 0.02473$ W/mK; $Pr = 0.711$;

Reynolds number (external flow)

$$Re = u \cdot D / \nu = 4.3321e+04$$

Nusselt Number and heat transfer coefficient (external flow)

$$\overline{Nu}_D = 0.3 + \frac{0.62 Re_D^{1/2} Pr^{1/3}}{[1 + (0.4/Pr)^{2/3}]^{1/4}} \left[1 + \left(\frac{Re_D}{282,000} \right)^{5/8} \right]^{4/5}$$

$$Nu = 112.3;$$

$$h = 18.52 \text{ W/m}^2\text{K};$$

Overall heat transfer coefficient

$$U = (h^{-1} + h_{out}^{-1})^{-1} = 5.84 \text{ W/m}^2\text{K};$$

A long, thin-walled horizontal tube 100 mm in diameter is maintained at uniform temperature $T_{tube} = 120 \text{ }^\circ\text{C}$ by the passage of steam through its interior. The tube is diffuse and it can be considered a gray surface with an emissivity $\epsilon = 0.8$. The tube is located into a big chamber, which can be considered a blackbody at a temperature $T_{wall} = 35 \text{ }^\circ\text{C}$ for the purpose of the radiative heat exchange. In the chamber, stagnant air is also present at $T_{air} = 35 \text{ }^\circ\text{C}$. Determine the total heat loss of the tube for unit tube length.

Thermophysical properties (350 K)

$$\rho = 1.008 \text{ kg/m}^3; \quad \nu = 2.073e-5 \text{ m}^2/\text{s}; \quad \alpha = 2.931e-5 \text{ m}^2/\text{s};$$

$$k = 0.02984 \text{ W/mK}; \quad Pr = 0.707;$$

Rayleigh number

$$\overline{Nu}_D = \left\{ 0.60 + 0.387 \left[\frac{Ra_D}{[1 + (0.559/Pr)^{9/16}]^{16/9}} \right]^{1/6} \right\}^2$$

$$Ra = 9.81 \cdot (1/T_{wall_air}) \cdot (T_{tube} - T_{wall_air}) \cdot (D^3) / \nu / \alpha = 4.4536e+06;$$

Nusselt number and heat transfer coefficient

$$Nu = 22.28;$$

$$h = Nu \cdot k / D = 6.65 \text{ W/m}^2\text{K}$$

Heat rates unit tube length

$$Q_{radiation} = \pi \cdot D \cdot \epsilon \cdot \sigma \cdot (T_{tube}^4 - T_{wall_air}^4) = 212 \text{ W/m};$$

$$Q_{convection} = \pi \cdot D \cdot h \cdot (T_{tube} - T_{wall_air}) = 177.5 \text{ W/m};$$

$$Q_{tot} = Q_{radiation} + Q_{convection} = 389.5 \text{ W/m}$$