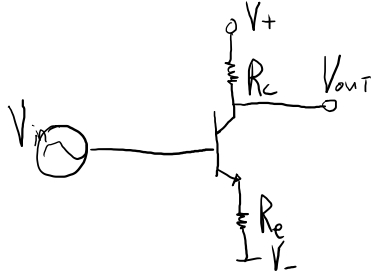


# Day 3: Differential amplifiers to op-amps

A transistor amplifier:



$$\text{Gain: } G = \frac{V_{out}}{V_{in}} \approx \frac{I_c R_c}{I_e R_e} \approx \frac{R_c}{R_e}$$

How does this work?

1.  $V_{in}$  controls  $V_e$ , changing emitter current.

$$I_e = \frac{V_{in} - V_-}{R_e}$$

2. Due to the large current gain of transistor, ( $\beta$ ), the current drawn from  $V_+$  through  $R_c$ :

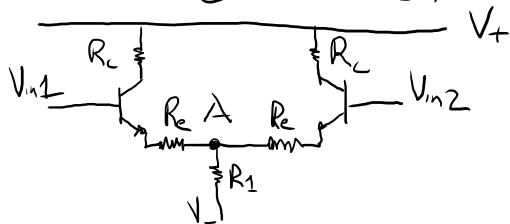
$$I_c = \frac{V_+ - V_{out}}{R_c} \rightarrow V_{out}$$

Often we're more interested in a voltage difference than voltage signal.



How do we build such an amplifier?

Use 2 transistors!



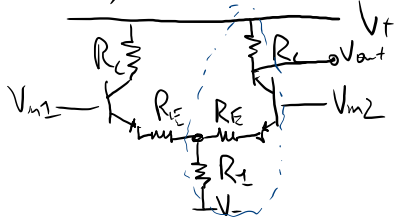
Suppose both  $V_{in1}$  &  $V_{in2}$  are the same.

- The voltage at A will vary with the applied voltage @  $V_{in1}$  &  $V_{in2}$

"Common-mode"

Then we can calculate the gain:  $G_{cm} = \frac{R_c}{(R_E + 2R_E)}$

Now, consider the case  
Signal,  $V_{in1} = -V_{in2}$



where we apply a perfectly asymmetric

What is the voltage at point A? 0!  
by symmetry. Both  $\Delta V$ 's cancel out.

What is the gain?  
 "Differential"

$$G_{diff} = \frac{R_c}{2R_E}$$

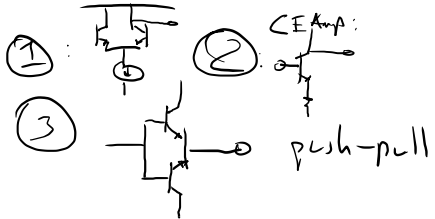
From symmetry of voltage fluctuations.

How well does this amp reject the common mode?

$$\frac{G_{diff}}{G_{cm}} = \frac{R_c}{2R_E} \frac{(R_E + 2R_1)}{R_c} \approx \left( \frac{R_1}{R_E} \right) \text{ when } R_1 \gg R_E$$

↳ "Common mode rejection ratio" CMRR.

On to OP-amps:



Op-amps have a lot of gain.  
They use negative feedback.  $\Rightarrow$  often incredible  
consistent performance.

Why negative feedback?

— Build in an excess of gain: feed that signal  
into the inputs so as to decrease the  
excess gain & stabilize the amp's performance.

Feedback will close the loop unlike our transistor  
amplifiers, which are in open-loop.

The excess gain is enormous. Open-loop gain of LF411  
is typically 200,000.

## "Golden rules" for op-amp operation:

1. The output does whatever it can to make the voltage difference at the input 0.

2. The inputs draw no current.

↳ Supply is different:  $V_+$ ,  $V_-$ .  
must be powered to work.

n.b. these rules only apply when op-amp is used with negative feedback.

\* A follower:



estimate: What is the input impedance,  $R_{in}$ ?

What is the voltage offset:  $v_{out} - v_{in}$ ?

! Compare to emitter follower!

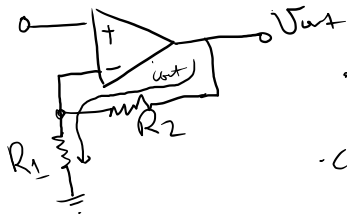
What is the output impedance,  $R_{out}$ ?



① Apply  $\Delta v \downarrow$

② High-gain op-amp senses the change (all feedback loop, and for errors with cores)

\* Non-inverting amplifier:



What is the gain of this amplifier?

- Apply 1V to "+" input;
- @ port A,  $V = 1V$ .
- Current to ground is  $\frac{1V}{R_1}$ .

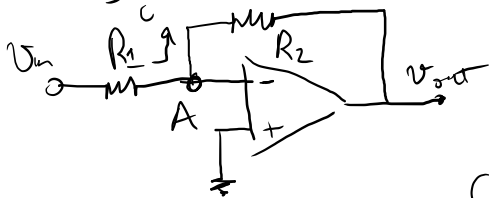
$$\circ \frac{V_{out} - 1V}{R_2} = \frac{1V}{R_1}$$

$$\rightarrow V_{out} = 1 + \frac{R_2}{R_1} \Rightarrow G = 1 + \frac{R_2}{R_1}$$

- Amplifier when  $R_2 > R_1$ .
- What is  $R_{in}$ ?  $\infty$ .
- What is  $R_{out}$ ? very low ( $\sim 0$ ).



\* Inverting amplifier



Apply 1V @ input.  
 What is  $V_A$ ? (0V, =)  
 "virtual ground"

Current is  $\frac{1V}{R_1}$ .

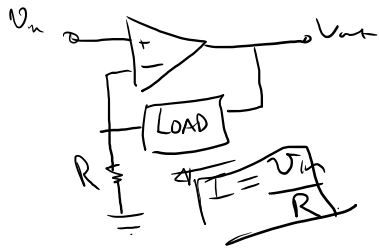
This current also goes through  $R_2$ :

$$v_{out} = i R_2 = \frac{1V R_2}{R_1} = \frac{R_2}{R_1}$$

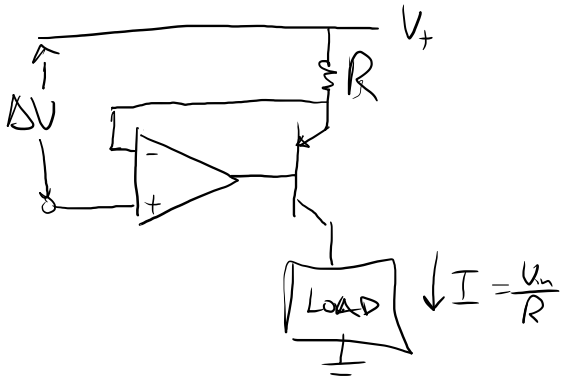
$$G = \frac{v_{out}}{v_{in}} = \frac{R_2}{R_1}$$

\* What is  $R_{in}$ ?  $\frac{R_2}{R_1}$ . It's not "huge". In fact,  $R_1$ .

\* Current Source:



not an ideal current source, b/c  $V @$  inverting input is not 0.



Op amp improves transistor behavior. The load is connected to ground.

\* Schmitt Trigger: very stable switch, where switch is set programmatically.

\* Trans-impedance amplifier: Amplifies current sources.

\* Integrators & differentiators, filters etc